

$$y = \left(\frac{3}{2}\right)^x$$

- 1) RUY $y = \left(\frac{3}{2}\right)^{-x}$
- 2) ROX $y = -\left(\frac{3}{2}\right)^{-x}$
- 3) v. shift
down 4 $y = -\left(\frac{3}{2}\right)^{-x} - 4$

Objectives:

- to write and apply exponential functions from two points
- to recognize an equation from a set of points
- create and solve doubling time and half life equations

1) Write an exponential function $y = ab^x$ whose graph passes through (1, 12) and (3, 108).

sub. x & y into $y = ab^x$

(1, 12) $x=1, y=12$
 $y = ab^x$
 $12 = ab^1$

(3, 108) $x=3, y=108$
 $y = ab^x$
 $108 = ab^3$

• solve for "a"

$a = \frac{12}{b}$

• take "a" and plug it in to the other eq.

$108 = \left(\frac{12}{b}\right)b^3$

$108 = 12b^2$

$9 = b^2$

$3 = b$

$a = \frac{12}{b}$

$a = \frac{12}{3}$

$a = 4$

$y = 4 \cdot 3^x$

$y = ab^x$

$y = 4(3)^x$

2) Write an exponential function $y = ab^x$ whose graph passes through $(3, 0.5)$ and $(-4, 64)$.

$(3, 0.5)$
 $y = ab^x$
 $0.5 = ab^3$
 $\frac{0.5}{b^3} = a$

$(-4, 64)$
 $y = ab^x$
 $64 = ab^{-4}$

$64 = \left(\frac{0.5}{b^3}\right)b^{-4}$
 $64 = \left(\frac{0.5}{b^3}\right)\left(\frac{1}{b^4}\right)$
 $64 = \frac{0.5}{b^7}$
 $64b^7 = 0.5$
 $\frac{64b^7}{64} = \frac{0.5}{64}$
 $b^7 = \frac{0.5}{64}$
 $b^7 = \frac{1}{128}$
 $b = \sqrt[7]{\frac{1}{128}}$
 $b = \frac{1}{2}$

$a = \frac{0.5}{b^3}$
 $a = \frac{0.5}{\left(\frac{1}{2}\right)^3}$
 $a = \frac{0.5}{\frac{1}{8}} = \frac{\frac{1}{2}}{\frac{1}{8}} = \frac{1}{2} \cdot \frac{8}{1} = 4$

$y = 4 \cdot \left(\frac{1}{2}\right)^x$

3) An online store begins selling a new type of basketball shoe. In week 2, 60 pairs of shoes were sold. In week 4, the store sold 240 pair.

Write an exponential model ($y = ab^x$) that relates the number of shoes (in pairs) sold to the week number.

$(\text{week}, \text{pairs})$
 $y = ab^x$

$(2, 60)$
 $(4, 240)$

$60 = ab^2$
 $240 = ab^4$

$a = \frac{60}{b^2}$
 $a = 15$

$240 = \left(\frac{60}{b^2}\right)b^4$
 $240 = 60b^2$
 $4 = b^2$
 $2 = b$

$y = 15 \cdot 2^x$

How many did they originally sell?

15 pairs

"a" - initial value

What is the growth factor?

$2 = b$ → growth factor

What is the % increase?

- what is "r"?

$1 + r = b$

$r = 1$

$r = 100\%$

How many shoes (if the trend continues) will be sold in week 6?

$$\begin{array}{r} 24 \\ \times 15 \\ \hline 320 \\ 640 \\ \hline 960 \end{array}$$

$y = 15 \cdot 2^x$

$y = 15 \cdot 2^6$

$y = 15 \cdot 64$

$y = 960$ pairs on week 6

$2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$

Determine which ordered pairs are solutions to the given function.

4) $y = -3 \left(\frac{1}{2} \right)^x$

$y = -3 \left(\frac{1}{2} \right)^x$

A) $(0, -3)$

$y = -3 \left(\frac{1}{2} \right)^x$
 $y = -3 \left(\frac{1}{2} \right)^0$

B) $(2, -0.75)$

$y = -3 \left(\frac{1}{2} \right)^2$
 $y = -3 \left(\frac{1}{4} \right)$
 $y = -\frac{3}{4}$

~~C) $(-1, 6)$~~

~~$y = -3 \left(\frac{1}{2} \right)^{-1}$
 $y = -3(2)$
 $y = -6$~~

D) $(-2, -12)$

$y = -3 \left(\frac{1}{2} \right)^{-2}$
 $y = -3(2)^2$
 $y = -3 \cdot 4$
 $y = -12$

5) For your 16th birthday, you received \$250 from your grandparents. (You have very nice grandparents.) You plan to deposit this gift in your savings account that earns 5% interest compounded annually.



Write an equation in standard exponential form for the amount in your account after x years.

$$y = a(1+r)^t$$

$$y = 250(1+.05)^x$$

$$y = 250(1.05)^x$$

y = amt in the acct
x = # of years

How much money will be in your account on your 18th birthday given no deposits or withdrawals are made?

$$y = 250(1.05)^2$$

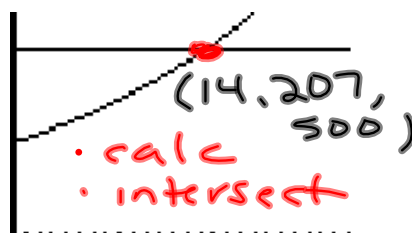
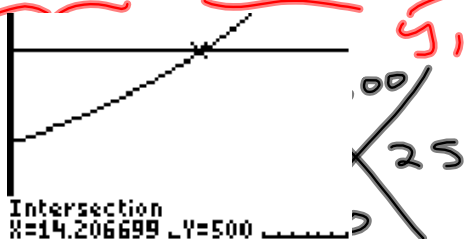
$$y = \$275.63$$

∴, on my 18th birthday, I will have \$275.63.

How many years will take to double your money?

$$y = 250(1.05)^x$$

$$500 = 250(1.05)^x$$



∴, in abt 14.207 years, I will have \$500

if your goal is to save this money to purchase a used car and the car you have in mind costs \$5210.99, how long will it take to have enough money to make the purchase?

Wksh Day 3
1, 2, 3, 5, 6-8,
11-15