Solving Systems Using Word Problems

Objectives

- Use reading strategies to write formulas
- Solve the equations using substitution or elimination

Steps to Follow

- 1. Identify Variables
- 2. Write 2 equations
- (Use key words and reading strategies to help)
- 3. Solve using substitution or elimination
- 4. Write answer in a complete sentence

Kevin would like to buy 10 bouquets. The standard bouquet costs \$7, and the deluxe bouquet costs \$12. He can only afford to spend \$100. How many of each type can he buy?

Define Variables: X: standard bouquet

Y: deluxe bouquet

Equation 1 Cost: 7x+12y=100

Equation 2 Bouquets : x+y=10

Solution: (4,6)

A hot air balloon is 10 meters above the ground and rising at a rate of 15 meters per minute. Another balloon is 150 meters above the ground and descending at a rate of 20 meters per minute. When will the two balloons meet?

Define Variables: x=minutes

y=height in meters

Equation 1 y=15x+10 Equation 2 y=-20x+150

Solution: (4,70)

A group of 3 adults and 10 students paid \$102 for a cavern tour. Another group of 3 adults and 7 students paid \$84 for the tour. Find the admission price for an adult ticket and a student ticket.

Define Variables: x= adult ticket price

y=student ticket price

Equation 1 3x+10y=102 Equation 2 3x+7y=84

Solution (14,6)

Melissa and Frank were jogging. Melissa had a 2 mile head start on Frank. If Melissa ran at an average rate of 5 miles per hour and Frank ran at an average rate of 8 miles per hour, how long would it take for Frank to catch up with Melissa?

Define Variables: x=hours

y=miles

Equation 1 y=5x+2 Equation 2 y=8x

Solution (2/3, 5, 1/3)

An Algebra Test contains 38 problems. Some of the problems are worth 2 points each. The rest of the questions are worth 3 points each. A perfect score is 100 points. How many problems are worth 2 points? How many problems are worth 3 points?

Define Variables: x=2 pt. questions

Equation 1 x+y=38 y=3 pt. questions

Equation 2 2x+3y=100

Solution (14,24)

Example 6 Ashley has \$9.05 in dimes and nickels. If she has a total of 108 coins, how many of each type does she have?

Define Variables x=dimes

y=nickels

Equation 1 x+y=108 Equation 2 .10x+.05y=9.05

Solution (73,35)

The perimeter of a parking lot is 310 meters. The length is 10 more than twice the width. Find the length and width. (Remember: P=2L+2W)

Define Variables L=length

W=width

Equation 1 2L+2W=310 Equation 2 L=2W+10

Best Method Substitution

Solution (106 2/3, 48 1/3)

Example 8 The sum of two numbers is 112. The smaller is 58 less than the greater. Find the numbers.

Define Variables x=smaller number

Equation 1 x+y=112

Best Method Substitution y=larger number

Equation 2 x=y-58

Solution (27,85)

The sum of the ages of Ryan and his father is 66. His father is 10 years more than 3 times as old as Ryan. How old are Ryan and his father?

Define Variables x=Ryan's age

y=Dad's age

Equation 1 x+y=66

Best Method Substitution Equation 2 y=3x+10

Solution (14,52)

A total of \$10,000 is invested in two funds, Fund A and Fund B. Fund A pays 5% annual interest and Fund B pays 7% annual interest. The combined annual interest is \$630. How much of the \$10,000 is invested in each fund?

Define Variables a=Fund A

Equation 1 a+b=10,000

Best Method Substitution b=Fund B

Equation 2 .05a+.07b=630

Solution (6500,3500)

We need to rent a large truck for one week. Rental companies charge an initial cost plus an additional cost for each mile driven. One company, Paenz, will rent a 27 foot truck for us for \$525 plus \$0.21 per mile. Another company, Opan, will rent us the same size truck for \$585 plus \$0.13 per mile.

Define Variables x=miles

Equation 1 y=0.21x+525

Best Method Substitution y=total cost

Equation 2 y=0.13x+585

Solution (750,682.50)

The larger of two numbers is 7 less than 8 times the smaller. If the larger number is decreased by twice the smaller, the result is 329. Find the two numbers.

Define Variables x=smaller number

y=larger number

Equation 1 y=8x-7 Equation 2 y-2x=329

Best Method Substitution

Solution (56,441)