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# **Transformations**

Return to Table of Contents A transformation of a geometric figure is a mapping that results in a change in the position, shape, or size of the figure. In the game of dominoes, you often move the dominoes by sliding them, turning them or flipping them. Each of these moves is a type of transformation. translation - slide rotation - turn reflection - flip

In a transformation, the original figure is the <u>preimage</u>, and the resulting figure is the <u>image</u>.

In the examples below, the preimage is green and the image is pink.



Some transformations (like the dominoes) preserve distance and angle measures. These transformations are called <u>rigid motions</u>.

To preserve distance means that the distance between any two points of the image is the same as the distance between the corresponding points of the preimage.

To preserve angles means that the angles of the image have the same measures as the corresponding angles in the preimage.



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A transformation maps every point of a figure onto its image and may be described using arrow notation ( $\rightarrow$ ).

**Prime notation** (') is sometimes used to identify image points.



**Note:** You list the corresponding points of the preimage and image in the same order, just as you would for corresponding points in congruent figures or similar figures.

1 Does the transformation appear to be a rigid motion? Explain.

 $\bigcirc$  Yes, it preserves the distance between consecutive points.

No, it does not preserve the distance between consecutive points.





Image



- 2 Does the transformation appear to be a rigid motion? Explain.
  - Yes, distances are preserved.
  - $\bigcirc$  Yes, angle measures are preserved.
  - $\bigcirc$  Both A and B.
  - $\bigcirc$  No, distance are not preserved.



Answer



3 Which transformation is not a rigid motion?

 $\bigcirc$  Reflection

 $\bigcirc$  Translation

 $\bigcirc$  Rotation

O Dilation

Answer



- 4 Which transformation is demonstrated?
  - $\bigcirc$  Reflection
  - $\bigcirc$  Translation
  - $\bigcirc$  Rotation
  - O Dilation



4 Which transformation is	s demonstrates 10		
Q Reflection			
O Translation	Wer	Π	
O Rotation	Ans	D	
<ul> <li>Dilation</li> </ul>			









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# **Translations Return to Table of Contents**



You write the translation that maps  $\triangle$  ABC onto  $\triangle$  A'B'C' as T $\triangle$  ABC)  $\Rightarrow \triangle$  A'B'C'



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### Finding the Image of a Translation

What are the vertices of  $T_{<-2, 5>}$  ( $\triangle$  *DEF*)? Graph the image of  $\triangle$  *DEF*.



Draw  $\overline{DD}'$ ,  $\overline{EE}'$  and  $\overline{FF}$ . What relationships exist among these three segments? How do you know?









7 In the diagram,  $\Delta A'B'C'$  is an image of  $\Delta ABC$ . Which rule describes the translation?

 $\bigcirc A \quad T_{<-5,-3>}(\Delta ABC)$  $\bigcirc B \quad T_{<5,3>}(\Delta ABC)$  $\bigcirc C \quad T_{<-3,-5>}(\Delta ABC)$ 

 $\bigcirc D \quad T_{<3,5>}(\Delta ABC)$ 



Answer



- 8 If  $T_{<4,-6>}$  (JKLM) = J'K'L'M', what translation maps J'K'L'M' onto JKLM?
  - $\bigcirc \mathsf{A} \quad T_{<4,-6>}(J'K'L'M')$
  - $\bigcirc \mathsf{B} \quad T_{<6,-4>}(J'K'L'M')$
  - $\bigcirc \mathbb{C}$   $T_{<-6,4>}(J'K'L'M')$
  - $\bigcirc \mathsf{D} \quad T_{{}_{<\!-4,6\!>}}(J'K'L'M')$



Answer

9  $\triangle$  RSV has coordinates R(2,1), S(3,2), and V(2,6). A translation maps point R to R' at (-4,8). What are the coordinates of S' for this translation?



 $\bigcirc$  E none of the above



## Reflections

Reflections Activity Lab (Click for link to lab)

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A <u>reflection</u> is a transformation of points over a line. This line is called the <u>line of reflection</u>. The result looks like the preimage was flipped over the line. The preimage and the image have opposite orientations.



#### **Properties**

-If a point *B* is on line *m*, then the image of *B* is itself (*B* = *B'*).

-If a point C is not on line m, then m is the perpendicular bisector of  $\overline{CC'}$ 

The reflection across *m* that maps  $\triangle ABC \rightarrow \triangle A'B'C'$  can be written as  $R_m(\triangle ABC) = \triangle A'B'C$
















X•

- 11 Which point represents the reflection of X?
  - $\bigcirc\,$  point A
  - $\bigcirc$  point B
  - point C
  - point D
  - $\bigcirc$  none of the above

11 Which point represents	th	
O point A		
O point B		
○ point C		
O point D		
$\bigcirc$ none of the above		

- 12 Which point represents the reflection of X?
  - $\bigcirc$  point A
  - point B
  - point C
  - point D



 $\bigcirc$  none of the above







## 14 Is a reflection a rigid motion?

 $\bigcirc$  Yes

 $\bigcirc$  No



#### **Reflections in the Coordinate Plane**

Since reflections are perpendicular to and equidistant from the line of reflection, we can find the exact image of a point or a figure in the coordinate plane.



How do the coordinates of each point change when the point is reflected over the *y*-axis?

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#### **Reflections in the Coordinate Plane**



How do the coordinates of each point change when the point is reflected over the *y*-axis?





How do the coordinates of each point change when the point is reflected over the *x*-axis?





How do the coordinates of each point change when the point is reflected over the *x*-axis?



Count the number of diagonals from the point to the line of reflection.

HINT:

How do the coordinates of each point change when the point is reflected over the *y*-axis?







### **Reflections in the Coordinate Plane**



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# Reflect qui MNPQ ove Notation $R_{y=3}(MNPQ) = V_{x=a}(x, y) \stackrel{d}{=} (-x + 2a, y)$

 $R_{y=a}(x, y) = (-x + 2a, y)$  $R_{y=a}(x, y) = (x, -y + 2a)$ 



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- 15 The point (4,2) reflected over the x-axis has an image of \_\_\_\_\_.
  - Q (4,2)
  - (-4,-2)

  - (-4,2)(4,-2)



- 16 The point (4,2) reflected over the y-axis has an image of \_\_\_\_\_.
  - Q (4,2)
  - (-4,-2)

  - (-4,2)(4,-2)



17 B has coordinates (-3,0). What would be the coordinates of B' if B is reflected over the line x = 1?

◯ (-3,0)

**(4,0)** 

**(-3,2)** 

◯ (5,0)

17 B has coordinates (-3,0). What would be the coordinates of B' if B is reflected over the line x = 1?



- 18 The point (4,2) reflected over the line y=2 has an image of \_\_\_\_\_.
  - Q (4,2)
  - **(4,1)**
  - (2,2)
  - (4,-2)


## Line of Symmetry

A line of symmetry is a line of reflection that divides a figure into 2 congruent halves. These 2 halves reflect onto each other.

















19 How many lines of symmetry does the following have?



Answer















22 How many lines of symmetry does the following have?

-

 $\bigcirc$  none

○ one

⊖ two

 $\bigcirc$  infinitely many







 $\bigcirc$  infinitely many







# **Rotations**

Rotations Activity Lab (Click for link to lab)

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A <u>rotation</u> is a rigid motion that turns a figure about a point.

The amount of turn is in degrees.

The direction of turn is either clockwise or counterclockwise.





- The image of P is itself (P = P')
- For any other point *B*, *PB*' = *PB*

-The *m* <*BPB*' = *x* 



#### **Notation**

 $\overline{\mathbf{r}_{(x^{\circ}, P)}(\triangle ABC)} = \triangle A'B'C' \text{ for a rotation clockwise } x^{\circ} \text{about P}$  $\mathbf{r}_{(-x^{\circ}, P)}(\triangle ABC) = \triangle A'B'C' \text{ for a rotation counterclockwise } x^{\circ} \text{ about F}$  Slide 56 / 145



Slide 56 (Answer) / 145 **Drawing Rotation Images** w! What is the image of  $r_{(100^\circ, C)}$  ( $\Delta$ Answer 0 С 0 Step 3 В Locate L' and B' following steps 1 and 2. Step 4 Draw∆ L'O'B'

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#### **Rotations in the Coordinate Plane**

When a figure is rotated 90°, 180°, or 270° clockwise about the origin O in the coordinate plane, you can use the following rules.





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 $r_{(270^{\circ}, O)}(x, y) = (-y, x)$ 





 $r_{(360^\circ, 0)}(x, y) = (x, y)$ 

Note:

 $\overline{\mathbf{r}_{(-90^\circ, O)}(x, y)} = \mathbf{r}_{(270^\circ, O)}(x, y)$ 

and

 $\mathbf{r}_{(-270^{\circ}, O)}(x, y) = \mathbf{r}_{(90^{\circ}, O)}(x, y)$ 





Answer

25 Square ABCD has vertices A(3,3), B(-3,3), C(-3, -3), and D(3, -3). Which of the following images is A?

- $\bigcirc \mathsf{A} \quad r_{(90^\circ, 0)}(C)$
- $\bigcirc \mathsf{B} \quad r_{(180^\circ, O)}(D)$
- $\bigcirc C \quad r_{(90^\circ,0)}(B)$
- $\bigcirc D r_{(270^\circ,0)}(C)$

25 Square ABCD has vertices A(3,3), B(-3,3), C(-3, -3), and D(3, -3). Which of the following images is A?



26 PQRS has vertices P(1,5), Q(3, -2), R(-3, -2), and S(-5, 1). What are the coordinates of Q' after  $r_{(270^{\circ},0)}(Q)$ ?

Q (-2, -3)

- (2,3)
- **(-3, 2)**
- (-3, -2)

Answer



### **Identifying a Rotation Image**

A regular polygon has a center that is equidistant from its vertices. Segments that connect the center to the vertices divide the polygon into congruent triangles. You can use this fact to find rotation images of regular polygons.



PENTA is a regular pentagon with center O.

**a)** Name the image of *E* for a 72° rotation counterclockwise about *O*.

Ε

**b)** Name the image of *P* for a 216° rotation clockwise about *O*.

c) Name the image of  $\overline{AP}$  for a 144° rotation counterclockwise about O.


27 MATH is a regular quadrilateral with center R. Name the image of M for a 180° rotation counterclockwise about R.

ΩΜ



ΟΤ



Answer

ΟΗ



28 MATH is a regular quadrilateral with center R. Name the image of  $\overline{HT}$  for a 270° rotation clockwise about R.





29 HEXAGO is a regular hexagon with center M. Name the image of G for a 300° rotation counterclockwise about M.

М

Ε

Х

Н

G

0

ΟΧ

 $\bigcirc A$ 

ΟE

Ο Η

00

Answer



х

Answer

30 HEXAGO is a regular hexagon with center M. Name the image of OH for a 240° rotation clockwise about M.





## **Rotational Symmetry**

A figure has rotational symmetry if there is at least one rotation less than or equal to 180° about a point so that the preimage is the image.



This figure has rotational symmetry at 120 °

A circle has infinite rotational symmetry.

### Do the following have rotational symmetry? If yes, what is the degree of rotation?



С.













Answer

31 Does the following figure have rotational symmetry? If yes, what degree?

S

- $\bigcirc$  yes, 90°
- $\bigcirc$  yes, 120°
- $\bigcirc$  yes, 180°
- 🔾 no



- 32 Does the following figure have rotational symmetry? If yes, what degree?
  - $\bigcirc$  yes, 90°
  - $\bigcirc$  yes, 120°
  - ◯ yes, 180°



🔾 no



33 Does the following figure have rotational symmetry? If yes, what degree?



Answer

🔾 no



Answer

34 Does the following figure have rotational symmetry? If yes, what degree?



34 Does the following figure have rotational symmetry? If yes, what degree?
9 yes, 18°
9 yes, 36°
9 yes, 72°
0 no

# **Composition of Transformations**

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# When an image is used to as the preimage for a second transformation it is called a <u>composition of transformations</u>.

An **isometry** is transformation that preserves distance, or length.

The transformations below are isometries.









The composition of two or more isometries is an isometry.

#### **Glide Reflections**

If two figures are congruent and have opposite orientations (but are not simply reflections of each other), then there is a translation and a reflection that will map one onto the other. A <u>glide reflection</u> is the composition of a glide (translation) and a reflection across a line parallel to the direction of translation.

 $\triangle ABC$  is translated 1 unit to the right and then reflected over the line y = -2.





1.) R<sub>x-axis</sub> 0 T<sub><-2, 0></sub> (△*ABC*)



Answer

2.) R<sub>y-axis</sub> 0 T<sub><0, -3></sub> (△ABC)









1.) R<sub>x-axis</sub> 0 T<sub><-2, 0></sub> (△*ABC*)



Answer

2.) R<sub>y-axis</sub> 0 T<sub><0, -3></sub> (△ABC)









1.) R<sub>x-axis</sub> 0 T<sub><-2, 0></sub> (△*ABC*)



Answer

2.) R<sub>y-axis</sub> o T<sub><0, -3></sub> (△ABC)







## **Composition of Reflections**



Translate  $\triangle XYZ$  by using a composition of reflections. Reflect over x = -3 then over x = 4. Label the first image  $\triangle X'Y'Z'$  and the second  $\triangle X''Y''Z''$ .

1.) What direction did  $\triangle XYZ$  slide? How is this related to the lines of reflection?

2.)How far did ∆XYZ slide? How is this related to the lines of reflection?

# Answer

#### Make a conjecture.







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# Rotations can be done as a composition of reflections over intersecting lines.



The amount of rotation is twice the acute,or right, angle formed by the lines of reflection.

The direction of rotation is clockwise because rotating from m to n across the acute angle is clockwise. Had the triangle reflected over n then m, the rotation would have been counterclockwise.



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38 If the image of  $\triangle ABC$  is the composite of reflections over e then f, what is the angle of rotation?





Answer

39 What is the direction of the rotation if the image of  $\triangle$ ABC is the composite of reflections first over e then f?

Clockwise ()e ○ Counterclockwise Β **40**°



40 If the image of △ABC is the composite of reflections over f then e, what is the angle of rotation?





e

Answer

41 What is the direction of rotation if the image of  $\triangle ABC$  is the composite of reflections first over f then e?

Β

Q Clockwise

○ Counterclockwise



42 If the image of △ABC is the composite of reflections over e then f, what is the angle of rotation?





43 What is the direction of the rotation if the image of △ABC is the composite of reflections first over e then f?





### **Congruence Transformations**

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#### **Congruent Figures**

Two figures are <u>congruent</u> if and only if there is a sequence of one or more rigid motions that maps one figure onto another.

The composition  $R_m \circ T_{<2, 3>} (\triangle ABC) = (\triangle DEF)$ 

Since compositions of rigid motions preserve angle measures and distances the corresponding sides and angles have equal measures. **Fill in the blanks below.** 



	Slide 97 (Answer) / 145
Congruent Figures	
$\overline{AB} = \overline{DE}$ $\overline{BC} = \overline{EF}$ $\overline{AC} = \overline{DF}$ $m\# A = m\# D$ $m\# B = m\# E$ $m\# C = m\# F$ $\overline{AC} = \_\_$ $m\# A = m\# \_\_$ $m\# A = m\# \_\_$ $m\# B = m\# \_\_$ $m\# B = m\# \_\_$ $m\# C = m\#$	congruent Figures nd only if there is a sequence of one some figure onto another. $c_{2,3>}(\triangle ABC) = (\triangle DEF)$ $A' = A' =$
$\overline{AC} = \overline{DF}$ $m\# A = m\# D$ $m\# B = m\# E$ $m\# C = m\# F$ $\overline{AC} = \_$ $m\#A = m\# \_$ $m\#B = m\# \_$ $m\#C = m\# \_$	C = C + C + C + C + C + C + C + C + C +

#### **Identifying Congruence Transformations**

Because compositions of rigid motions take figures to congruent figures, they are also called <u>congruence transformations</u>.

What is the congruence transformation that maps  $\triangle XYZ$  to  $\triangle ABC$ ?



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#### Use congruence transformations to verify that $\triangle ABC \# \triangle DEF$ .







# To show that $\triangle ABC$ is an equilateral triangle, what congruence transformation can you use that maps the triangle onto itself? Explain.





#### 44 Which congruent transformation maps $\triangle ABC$ to $\triangle DEF$ ?

 $\bigcirc A \quad T_{<-5,5>}$  $\bigcirc B \quad r_{<180^{\circ},O>}$  $\bigcirc C \quad R_{x-axis} \circ T_{<5,0>}$  $\bigcirc D \quad R_{y-axis} \circ r_{<90^{\circ},O>}$ 







## 45 Which congruence transformation does not map $\triangle$ ABC to $\triangle$ DEF?








46 Which of the following best describe a congruence transformation that maps  $\triangle ABC$  to  $\triangle DEF$ ?

 $\bigcirc$  a reflection only

 $\bigcirc$  a translation only





Answer

 $\bigcirc$  a translation followed by a reflection

 $\bigcirc$  a translation followed by a rotation



47 Quadrilateral ABCD is shown below. Which of the following transformations of  $\Delta AEB$  could be used to show that  $\Delta AEB$  is congruent to  $\Delta DEC$ ?



 $\bigcirc$  a reflection over line n



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# **Dilations**

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# A dilation is a transformation whose pre image and image are similar. Thus, a dilation is a similarity transformation. It is *not*, in general, a rigid motion.



Pupil



**Dilated Pupil** 

Every dilation has a center and a scale factor n, n > 0. The scale factor describes the size change from the original figure to the image.

# A dilation with center R and scale factor n, n > 0, is a transformation with the following properties:



- The image of R is itself (R' = R)
- For any other point B, B' is on  $\overrightarrow{RB}$

$$-RB' = n \bullet RB \text{ or } n = \frac{RB'}{RB}$$

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The symbol for scale factor is *n*.

A dilation is an enlargement if *n* > 1.

A dilation is a reduction if 0< *n* < 1.

What happens to a figure if *n* = 1?









The dashed line figure is a dilation image of the solid-line figure. *D* is the center of dilation. Tell whether the dilation is an enlargement or a reduction. Then find the scale factor of the dilation.



## <sup>48</sup> Is a dilation a rigid motion?

 $\bigcirc$  Yes

 $\bigcirc$  No



## 49 Is a dilation a rigid motion?

 $\bigcirc$  Yes

ONo





 $\bigcirc$  enlargement, n = 3

 $\bigcirc$  enlargement, n = 1/3

 $\bigcirc$  reduction, n = 3

$$\bigcirc$$
 reduction, n = 1/3











H

52 Is the dilation an enlargement or reduction? What is the scale factor of the dilation?





- $\bigcirc$  reduction, n = 2
- $\bigcirc$  reduction, n = 1/2





53 Is the dilation an enlargement or reduction? What is the scale factor of the dilation?

 $\bigcirc$  enlargement, n = 2

 $\bigcirc$  enlargement, n = 3

- $\bigcirc$  enlargement, n = 6
- $\bigcirc$  not a dilation





54 The solid-line figure is a dilation of the dashed-line figure. The labeled point is the center of dilation. Find the scale factor of dilation.



1/3

54 The solid-line figure is a dilation of the dashed-line figure. The labeled point is the center of dilation. Find the scale factor of dilation.



55 A dilation maps triangle LMN to triangle L'M'N'. MN = 14 in. and M'N' = 9.8 in. If LN = 13 in., what is L'N'?

Q 13 in.

○ 14 in.

○ 9.1 in.

○ 9.8 in.



#### **Drawing Dilation Images**

#### Draw the dilation image $\Delta B'C'D'$ .

 $D_{(2, X)}(\Delta BCD)$ 



#### **Steps**

1. Use a straightedge to construct ray  $\overline{XB}$ .

2. Use a compass to measure  $\overline{XB}$ .

3. Construct  $\overline{XB'}$  by constructing a congruent segment on ray  $\overline{XB}$  so that  $\overline{XB'}$  is twice the distance of  $\overline{XB}$ .

4. Repeat steps 1- 3 with points C and D.





### **Dilations in the Coordinate Plane**

Suppose a dilation is centered at the origin. You can find the dilation image of a point by multiplying its coordinates by the scale factor.



### **Graphing Dilation Images**

### To dilate a figure from the origin, find the dilation images of its vertices.

 $\triangle$ HJK has vertices H(2, 0), J(-1, 0.5), and K(1, -2). What are the coordinates of the vertices of the image of  $\triangle$ HJK for a dilation with center (0, 0) and a scale factor 3? Graph the image and the preimage.









In this example, the center of dilation is NOT the origin. The center of dilation D(-2, -2) is a vertex of the original figure. This is a reduction with scale factor 1/2.

Point *D* and its image are the same. It is important to look at the distance from the center of dilation *D*, to the other points of the figure.

If AD = 6, then A'D' = 6/2 = 3.

Also notice AB = 4 and A'B' = 2, etc.




- 56 What is the y-coordinate of the image (8, -6) under a dilation centered at the origin and having a scale factor of 1.5?
  - Q -3 ○ -8 ○ -9

O -12

56 What is the y-coordinate of the image (8, -6) under a dilation centered at the origin and having a scale factor of 1.5?



Answer

○ -9

**O** -12

С

57 What is the x-coordinate of the image (8, -6) under a dilation centered at the origin and having a scale factor of 1/2?

 $\mathbf{Q}$  4 **8** C ) -6 ) -3



58 What is the y-coordinate of the image (8, -6) under a dilation centered at the origin and having a scale factor of 1/2?

)				
6				
	6	6	6	6

-3



- 59 What is the x-coordinate of the image of (8, -6) under a dilation centered at the origin and having a scale factor of 3?
  - 8
    -2
    24
    -6



- 60 What is the x-coordinate of the image of (8, -6) under a dilation centered at the origin and having a scale factor of 1.5?
  - 3
    8
    9
    12



61 What is the y-coordinate of the image of (8, -6) under a dilation centered at the origin and having a scale factor of 3?

Q -8	
<b>O</b> -2	
○ -24	
◯ -18	



62 What is the x-coordinate of (4, -2) under a dilation centered at (1, 3) with a scale factor of 2?

Q 7

O -2

**O** -7

**8** C



63 What is the y-coordinate of (4, -2) under a dilation centered at (1, 3) with a scale factor of 2?

Q 7

**O** -2

**O** -7

**8** C



## Similarity Transformations

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### Warm Up

**1. Choose the correct choice to complete the sentence.** 

Rigid motions and dilations both preserve angle measure / distance.

2. Complete the sentence by filling in the blanks.

 dilations
 rigid motions

 preserve distance;
 do not preserve distance.

Answer

3. Define similar polygons on the lines below.



#### **Drawing Transformations**

Triangle *GHI* has vertices G(-4, 2), H(-3, -3) and N(-1, 1). Suppose the triangle is translated 4 units right and 2 units up and then dilated by a scale factor of 2 with the center of dilation at the origin. Sketch the resulting image of the composition of transformations.





# $\triangle$ *LMN* has vertices L(0, 2), M(2, 2), and N(0, 1). For each similarity transformation, draw the image.

**1.**  $D_2 \circ R_x$  -axis ( $\triangle LMN$ )



# $\triangle$ *LMN* has vertices L(0, 2), M(2, 2), and N(0, 1). For each similarity transformation, draw the image.

**2. D**<sub>2</sub> O **r**<sub>(270</sub> ∘, o) (△ *LMN* )



### **Describing Transformations**

What is a composition of transformations that maps trapezoid *ABCD* onto trapezoid *MNHP*?





## For each graph, describe the composition of transformations that maps $\triangle ABC$ onto $\triangle FGH$





## For each graph, describe the composition of transformations that maps $\triangle ABC$ onto $\triangle FGH$





### **Similar Figures**

Two figures are **similar** if and only if there is a similarity transformation that maps one figure onto the other.

Identify the similarity transformation that maps one figure onto the other and then write a similarity statement.



64 Which similarity transformation maps  $\triangle ABC$  to  $\triangle DEF$ ?

$$\bigcirc A \quad R_{x-axis} \circ D_{0.5}$$
$$\bigcirc B \quad R_{x-axis} \circ D_2$$
$$\bigcirc C \quad r_{(90^\circ,o)} \circ D_{0.5}$$
$$\bigcirc D \quad r_{(270^\circ,o)} \circ D_2$$





# 65 Which similarity transformation does not map $\Delta$ PQR to $\Delta$ STU?






- 66 Which of the following best describes a similarity transformation that maps  $\Delta$ JKP to  $\Delta$ LMP?
  - $\bigcirc$  a dilation only



- $\bigcirc$  a rotation followed by a dilation
- $\bigcirc$  a reflection followed by a dilation
- $\bigcirc$  a translation followed by a dilation



