# Integers on the Coordinate Plane

Parts of a coordinate plane:

x-axis: a horizontal number line y-axis: a vertical number line

origin: the place where the two number lines meet quadrants: the four sections created by the two number lines

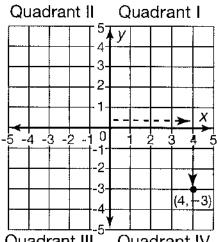
A point in a coordinate plane is represented by

an ordered pair.

T T x-coordinate y-coordinate

To locate point (4, -3), start at the origin.

Move to 4 on the x-axis. Then move to -3 on the y-axis. Quadrant III



Quadrant IV

Graph and label these points on the coordinate plane.

**1.** (4, 1)

**2.** (-3, 3)

**3.** (2, 0)

**4.** (4, -2)

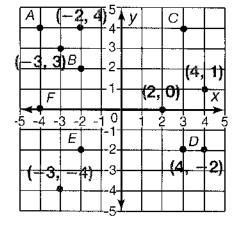
5. (-2, 4)

**6.** (-3, -4)

Write the ordered pair for each point.

- 7. A (-4, 4) 8. B (-2, 2)

- 9. D (3, -2) 10. E (-2, -2)



11. Writing to Explain How would you plot the point (-8, 10) on the coordinate plane?

Sample answer: Start at the origin. Move to the left 8 spaces. Then move up 10 spaces and place a point.

12. Reasoning In what quadrant will a point with a negative x-coordinate and a positive y-coordinate (negative number, positive number) be located?

#### Quadrant II

# Integers on the Coordinate Plane

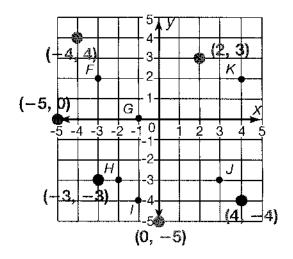
Write the ordered pair for each point.



3. 
$$H(-2, -3)$$
 4.  $I(-1, -4)$ 

Plot and label each ordered pair on the coordinate grid.





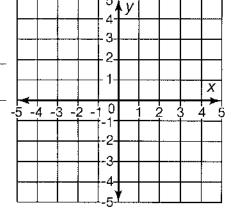
13. Writing to Explain A point is located in Quadrant IV. What do you know about the signs of the coordinates for the point? Explain.

Quadrant IV is the lower right quadrant. If a point is in Quadrant IV, the x-coordinate is positive and the y-coordinate is negative (x, -y).

**14.** Critical Thinking Draw three lines that are parallel to the *x*-axis. Read the ordered pairs for points on each line. What

generalization can you make about the ordered pairs for lines parallel to the x-axis?

The v-coordinate is the same for all points on a line parallel to the x-axis.



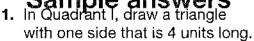
- 15. Geometry Which ordered pair is located in Quadrant III?
  - (A) (-1, -1)
    - B (-4, 0)
  - $\mathbf{C}$  (-2, 2)
  - **D** (0, 5)

# **Polygon Orders**

For each exercise, draw the figure required and write the ordered pair for each vertex. Draw the figures on the coordinate plane below.

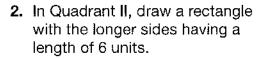
Sample answers

1. In Quadrant I, draw a triangle **Visual Thinking** 



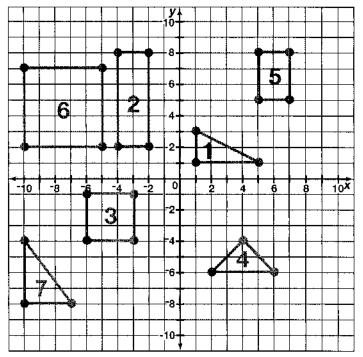
## for 1-7 and graph:

(1, 1), (1, 3), (5, 1)



$$(-2, 2), (-4, 2)$$

$$(-4, 8), (-2, 8)$$



3. In Quadrant III, draw a square with sides that are 3 units long.

$$(-3, -1), (-6, -1), (-6, -4), (-3, -4)$$

4. In Quadrant IV, draw an isosceles triangle with a base of 4 units.

$$(4, -4), (2, -6), (6, -6)$$

5. In Quadrant I, draw a rectangle with two sides that are 2 units long.

6. In Quadrant II, draw a square with sides that are 5 units long.

$$(-5, 2), (-10, 2), (-10, 7), (-5, 7)$$

In Quadrant III, draw a right triangle with a base of 3 units and a height of 4 units.

$$(-10, -4), (-7, -8), (-10, -8)$$

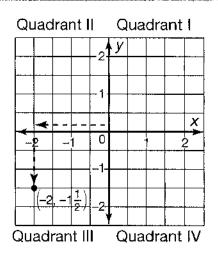
#### 8-2

# Rational Numbers on the Coordinate Plane

The coordinate grid has an *x*-axis, a *y*-axis, an origin (0, 0), and four quadrants.

Ordered pairs of rational numbers can be plotted just like ordered pairs of integers. Plot  $(-2, -1\frac{1}{2})$  on the grid.

To locate point  $(-2, -1\frac{1}{2})$ , start at the origin. Move 2 units to the left on the *x*-axis. Then move down  $1\frac{1}{2}$  units on the *y*-axis.

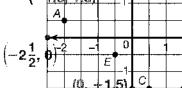


Graph and label these points on the coordinate plane.

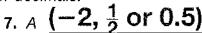
3. 
$$(1\frac{1}{2}, -1\frac{1}{2})$$

**4.** 
$$(-2\frac{1}{2}, 0)$$

**6.** 
$$(-1\frac{1}{2}, -2\frac{1}{2})$$



Write the ordered pair for each point, using fractions or decimals.



8. B 
$$(-0.5 \text{ or } -\frac{1}{2}, 1.5 \text{ or } 1\frac{1}{2})$$

9. C 
$$(\frac{1}{2} \text{ or } 0.5, -1\frac{1}{2} \text{ or } -1.5)$$

<sub>10. D</sub> (2, 0.5 or 
$$\frac{1}{2}$$
)

<sub>11. E</sub> 
$$(-0.5 \text{ or } -\frac{1}{2}, -0.5 \text{ or } -\frac{1}{2})$$

<sub>12. F</sub> 
$$(1.5 \text{ or } 1\frac{1}{2}, -2.5 \text{ or } -2\frac{1}{2})$$

**13. Reasoning** In which quadrant will both the *x*-coordinate and *y*-coordinate of a point be negative?

#### Quadrant III

# **Rational Numbers on the** Coordinate Plane

Write the ordered pair for each point.

1. 
$$A\left(-\frac{1}{4}, 0\right)$$

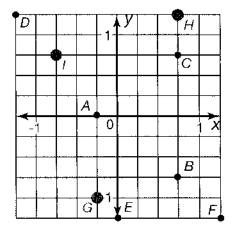
1. 
$$A\left(-\frac{1}{4}, 0\right)$$
 2.  $B\left(\frac{3}{4}, -\frac{3}{4}\right)$ 

5. 
$$E\left(0, -1\frac{1}{4}\right)$$

5. 
$$E\left(0, -\frac{1}{4}\right)$$
 6.  $F\left(\frac{1}{4}, -\frac{1}{4}\right)$ 

For 7 through 9, plot the ordered pairs.

**8.** 
$$H(\frac{3}{4}, 1\frac{1}{4})$$

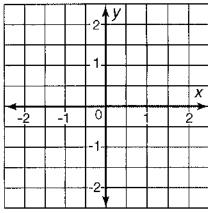


10. Writing to Explain A point is located in Quadrant II. What do you know about the signs of the coordinates for the point? Explain.

Quadrant II is the upper left quadrant. If a point is in Quadrant II, the x-coordinate is negative and the y-coordinate is positive (-x, +y).

11. Critical Thinking Draw three lines that are parallel to the y-axis. Read the ordered pairs for points on each line. What generalization can you make about the ordered pairs for lines parallel to the y-axis?

The x-coordinate is the same for all points on a line parallel to the y-axis.



12. Reason In which quadrants do the x-coordinate and the y-coordinate of a point have the same sign? Explain.

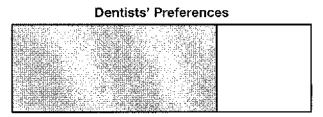
Quadrants I and III; Sample explanation: In Quadrant I they are both positive, in Quadrant III they are both negative.

#### **Benchmark Ads**

Benchmark fractions are used in many situations where an exact amount is not needed. Use benchmark fractions to help create advertising slogans using the data in the graphs.

Estimation

Example:

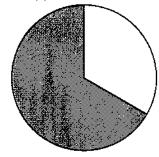


Sample answers are given

- Dentists who recommend True Clean toothpaste
- Dentists who recommend other toothpastes

More than  $\frac{2}{3}$  of dentists recommend True Clean toothpaste!

1. Shoppers' Preferences



- Customers who shop at Big Bargain Land
- Customers who shop at other stores

About  $\frac{2}{3}$  of

customers

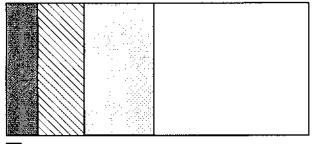
shop at

Big Bargain

Land!

2.

Cereal Preferences



- People who prefer Toasty Squares cereal
- People who prefer Fun O's cereal
- People who prefer Tasty Flakes cereal
- People who prefer Wheat Nuggets cereal

Wheat

**Nuggets** are

the choice

of  $\frac{1}{2}$  of

people tested

# Distance on the Coordinate Plane

Find the distance between (-3, 5) and (4, 5).

Use absolute value. Look at the *x*-coordinates. Since the points are in different quadrants, add the absolute values.

$$|-3| + |4| = 3 + 4 = 7.$$

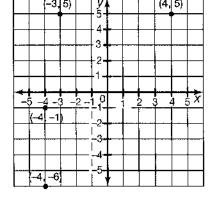
The points are 7 units apart.

Find the distance between (-4, -1) and (-4, -6).

Use absolute value. Look at the *y*-coordinates. Since the points are in the same quadrant, subtract the absolute values.

$$|-6| + |-1| = 6 - 1 = 5$$
.

The points are 5 units apart.



Use the coordinate plane for 1 through 3.

- 1. What is the distance between (1, 4) and (5, 4)?
  - A 1 unit
  - **B** 3 units
  - (C) 4 units
  - **D** 6 units
- **2.** Find the distance between (2, 2) and (2, -4).

#### 6 units

- 5 (1 4) (5, 4) 4 (2, 2) 2 (2, 2) -5 -4 -3 -2 -1 1 (1, -2) (-5, -2) -2 (1, -2) -3 (2, -4)
- 3. Writing to Explain How can you find the distance between (-5, -2) and (1, -2)?

Sample answer: First look at the x-coordinates. The points are in different quadrants, so add

the absolute values. |-5| + |1| = 5 + 1 = 6.

The points are 6 units apart.

#### 8-3

# Distance on the Coordinate Plane

For 1 through 12, find the distance between the ordered pairs. You can use a coordinate plane to help.

- **1.** (-1, 7), (5, 7) **2.** (-3, -9), (-3, -1) **3.** (-2, -6), (-2, 0) **4.** (12, -2), (12, 12)

- 6 units

- 8 units 6 units 14 units

- **5.** (2, -9), (-3, -9) **6.** (-1, 5), (5, 5) **7.** (0, -1), (0, 16) **8.** (15, -9), (15, -6)
- 5 units 6 units 17 units
- 3 units

- **9.** (-8, -4), (3, -4) **10.** (-7, -9), (-7, 8) **11.** (13, -3), (-3, -3) **12.** (-16, -9), (-16, -11)

- 11 units
- 17 units
- 16 units
- 2 units
- **13.** On a map, a museum is located at (15, 17). A library is located at (15, -2). How many units away is the museum from the library?
  - A 2 units
- C 17 units
- **B** 13 units
- **( D)** 19 units

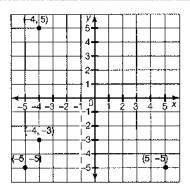
Use the coordinate plane for 14 and 15.

**14.** What is the distance from (5, -5) to (-5, -5)?

10 units

**15.** Kendra walks from a park located at (-4, -3) to her house at (-4, 5), How far did she walk?





**16. Reason** On a map, Jorge is standing at (11, −11). His friend Leslie is standing at (1, -11). If Jorge walks 10 units to the right, will he be standing with Leslie? Explain.

No; sample explanation: If Jorge walks 10 units to the right, he will be at (21, -11), not (1, -11).

### **Box Mixes**

3 \_\_\_\_

3.

Fill in the boxes with missing fractions to make each subtraction sentence true, both going across and down. Then write the final difference for each exercise in the circle in the lower right-hand corner. Write all fractions in simplest form.

**Number Sense** 

1.

$$-\boxed{2\frac{3}{4}} = \boxed{\frac{1}{3}}$$

$$\boxed{4\frac{1}{6}} - \boxed{2\frac{3}{4}} = \boxed{1\frac{5}{12}}$$

$$2\frac{3}{4} = 1\frac{5}{12}$$

$$2\frac{1}{6}$$
 =  $4\frac{1}{6}$ 

$$\begin{bmatrix} 3\frac{5}{9} \\ \end{bmatrix} - \begin{bmatrix} 2\frac{1}{9} \\ \end{bmatrix} = \begin{bmatrix} 1\frac{4}{9} \\ \end{bmatrix}$$

$$\boxed{2\frac{7}{9} - \boxed{\frac{1}{18}}} = 2\frac{13}{18}$$

$$\begin{bmatrix} 12\frac{5}{8} \\ \end{bmatrix} - \begin{bmatrix} 7\frac{3}{8} \\ \end{bmatrix} = \begin{bmatrix} 5\frac{1}{4} \\ \end{bmatrix}$$

$$4\frac{5}{12}$$
  $1\frac{47}{48}$   $=$   $2\frac{7}{16}$ 

$$\begin{bmatrix} 8\frac{5}{24} \end{bmatrix} - \begin{bmatrix} 5\frac{19}{48} \end{bmatrix} = \underbrace{2\frac{13}{16}}$$

$$5\frac{3}{5}$$
  $4\frac{1}{10}$   $=$   $1\frac{1}{2}$ 

$$2\frac{1}{3}$$
  $2\frac{2}{15}$   $=$   $\frac{1}{5}$ 

$$\boxed{3\frac{4}{15}} - \boxed{1\frac{29}{30}} = \boxed{1\frac{3}{10}}$$

4.

# Polygons on the

**Coordinate Plane** 

How can you find the perimeter of a polygon on the coordinate plane?

Remember, perimeter is the distance around a figure. So, find the distance between each pair of points by counting or using absolute value.

Top side: (-3, 4) to (2, 4): 5 units

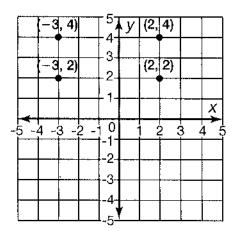
Right side: (2, 4) to (2, 2): 2 units

Bottom side: (2, 2) to (-3, 2): 5 units

Left side: (-3, 2) to (-3, 4): 2 units

$$5+2+5+2=14$$
.

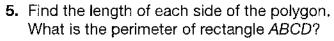
So, the perimeter is 14 units.



C

In 1 through 4, list the coordinates of each point.

- 1. A (-5, 2) 2. B (-2, 2)
- 3. C(-2, -4) 4. D(-5, -4)





In 6 through 10, list the coordinates of each point.

- 6. E (1, 2) 7. F (4, 2)
- 8. G(4,-1) 9. H(1,-1)
- **10.** Find the length of each side. What is the perimeter of polygon *EFGH*?

12 units

**11. Geometry** What type of quadrilateral is polygon *EFGH*? Be as specific as possible.

Square

# Polygons on the **Coordinate Plane**

For 1 through 3, graph the ordered pairs. Connect the points in order and identify the polygon you drew.

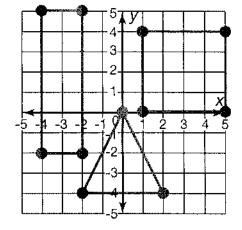
**1.** (1,0), (5,0), (5, 4), (1,4)

### Square

**2.** (0, 0), (2, -4), (-2, -4)

#### Isosceles triangle

**3.** (-4, -2), (-2, -2), (-2, 5), (-4, 5)



#### Rectangle

4. What is the perimeter of the polygon you drew in 1 above?

#### 16 units

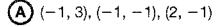
5. What is the perimeter of the polygon you drew in 3 above?

#### 18 units

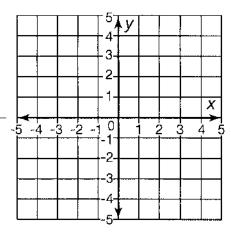
6. Reasoning The two opposite vertices of a square are (-2, 2) and (1, -1). What are the other two vertices of the square? Use the coordinate grid to help you.



7. Geometry Which set of ordered pairs can be connected in order to form a right triangle?



**D** 
$$(0, 5), (-3, 3), (3, -3)$$



# **Using Circles as Graphs**

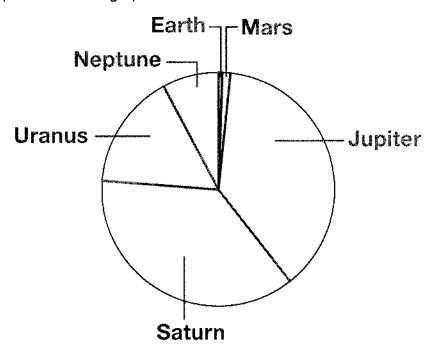
Circles can be used to graph and organize information. Using the number of degrees in a circle, you can divide the circle to represent the data given.

Data

1. There are 169 known moons that orbit the planets in our solar system. Mercury and Venus do not have moons, but each of the other six planets has at least 1 moon. Complete the table below. First find the percentage of total moons for each planet. Round each percentage to the nearest hundredth. Then multiply the percentage by 360° to find the measure to the nearest degree of each central angle.

Planet	Number of Moons	Percentage of 169 Moons (to nearest hundredth)	Measure of Central Angle (to nearest degree)
Earth	1	0.59%	2°
Mars	2	1.18%	40
Jupiter	64	37.87%	136°
Saturn	62	36.69%	132°
Uranus	27	15.98%	58°
Neptune	13	7.69%	28°

2. Complete the circle graph to show the moon data from the table.



# **Graphing Equations**

#### How to graph equations:

Graph the equation y = x - 3.

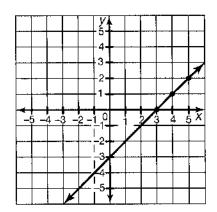
First make a T-table like the one at the right.

Use at least 3 values for x.

X	У
3	0
4	1
5	2

Graph each ordered pair onto the coordinate plane, then draw a line connecting the points. Every point on this line meets the condition that y = x - 3.

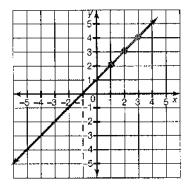
Because the graph of this equation is a straight line, it is called a linear equation.



Complete each T-table. Then graph each equation.

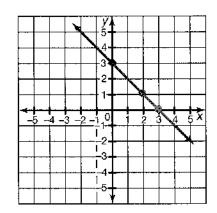
1. 
$$y = x + 1$$

х	У
1	2
2	3
3	4



2. 
$$y = 3 - x$$

х	У
0	3
2	1
3	0



# **Graphing Equations**

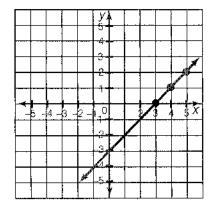
For 1 and 2, make a T-table. Then graph each equation.

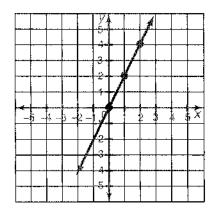
**1.** 
$$y = x - 3$$

X	У
3	0
4	1
5	2

**2.** 
$$y = 2x$$

X	У
0	0
1	2
2	4





**3. Reasoning** Is the point (5, 6) on the graph for the equation y = 2x + 5?

#### No

- **4.** Which point is on the graph for the equation y = x + 14?
  - **A** (2, 17)
  - **B** (5, 20)
  - **(10, 24)**
  - **D** (7, 23)
- 5. Writing to Explain Explain how making a T-table helps you graph an equation.

Sample answer: Using a T-table provides the coordinates needed to graph the equation.

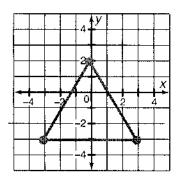
# **Ordered Pair Challenge**

Circle the letter for the set of ordered pairs that would form each figure when connected. Then plot the points and draw the shape on the coordinate plane.

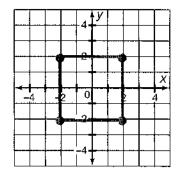
**Visual Thinking** 

1. Triangle

**C** 
$$(-3, 2), (-5, 2), (-4, 2)$$

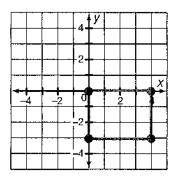


2. Square



3. Rectangle

$$(0, 0), (4, 0), (4, -3), (0, -3)$$



**4.** Without graphing, name four ordered pairs that, if connected, would form a square.

Sample anwer: (5, 5), (5, -5), (-5, -5), (-5, 5)

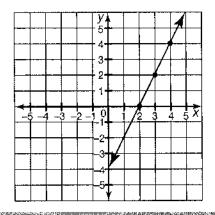
# **More Graphing Equations**

Use the same steps to graph an equation with more than one operation as you used to graph an equation with only one operation. Graph y = 2x - 4.

**Step 1:** Make a T-table. Use at least three number pairs in the table.

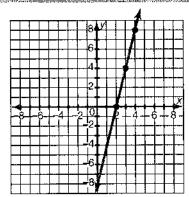
	х	у	Ordered Pairs
	2	0	$\rightarrow$ (2, 0)
	3	2	→ (3, 2)
ļ	4	4	→ (4, 4)

Step 2: Graph each ordered pair on a coordinate plane. Connect the points.



**1.** Complete the T-table and graph the equation. y = 4x - 8

X	У	Ordered Pairs
2	0	(2, 0)
3	4	(3, 4)
4	8	(4, 8)



Graph y = 6 - 2x at the right. Use it to answer **2** through **4**.

2. At what point does the equation y = 6 - 2x cross the y-axis?

(0, 6)

3. If x = 2, what is the value of y? 2

**4. Writing to Explain** Plot point (0, 4) on the grid. Is (0, 4) a solution to y = 6 - 2x? Explain.

No, the point is not on the graph.

# **More Graphing Equations**

For 1 and 2, make a T-table and graph each equation.

**1.** 
$$y = 3x - 5$$

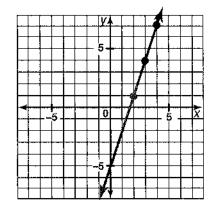
Х	У
2	1
3	4
4	7

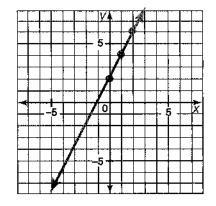
Sample answers in table.

**2.** 
$$y = 2x + 2$$

	T
X	У
0	2
1	4
2	6

Sample answers in table.



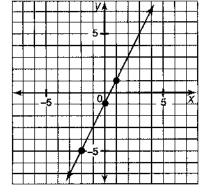


3. Which equation is shown by the graph?

**B** 
$$y = x - 1$$

**C** 
$$y = 2x + 1$$

**D** 
$$y = x + 1$$



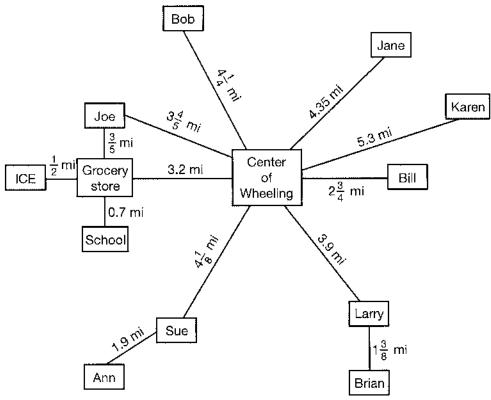
**4. Writing to Explain** Carrie says that one solution to y = 3x - 5 is (4, 7). Describe two ways to check if her statement is true. Use at least one way to check her answer.

Sample answer: Solve the equation or graph the equation and check that the ordered pair is on the graph:  $3 \times 4 - 5 = 12 - 5 = 7$ . The point is also on the graph in Exercise 1. So it checks.

#### **Rational Orders**

The members of a group of friends live in various locations around the town of Wheeling. They have been discussing who lives closer and who lives farther from school and from other places.

**Number Sense** 



1. Who lives closer to the center of Wheeling, Joe or Larry?

Joe

2. Joe went to the grocery store and then to the school. Which part of his trip was longer?

#### Trip from the grocery to the school

3. Who lives farther from the center of Wheeling, Jane or Sue?

#### Jane

**4.** Which is greater, the distance from Ann's house to Sue's or the distance from Brian's house to Larry's?

#### The distance from Ann's house to Sue's

5. Order the distances from the center of town to the homes of Bob, Sue, Karen, and Bill from greatest to least.

#### Karen, Bob, Sue, and Bill

# **Problem Solving: Multiple-Step Problems**

Some word problems have hidden questions that must be answered before you can solve the problem.

A paved trail is 8 miles long. Rita runs  $\frac{3}{8}$  of the length of the trail and walks the rest of the way. How many miles of the trail does Rita walk?

What do you know?

What are you asked to find?

How can you find the distance that Rita walks?

What is the hidden question? The hidden question will help you find data you need to solve the problem.

Rita runs \( \frac{3}{8} \) of an 8-mile trail.

How many miles of the trail that Rita

walks.

Subtract the distance Rita ran from the

length of the trail.

How many miles did Rita run?

To answer, find  $\frac{3}{8} \times 8 = 3$ .

Use the data to solve: 8 - 3 = 5, so Rita walked 5 of the 8 miles.

Write and answer the hidden question(s) in each problem. Then solve the problem.

April surfed for  $\frac{1}{3}$  of the 6 hours she was at the beach. She spent the rest of the time building a sand castle. How many hours did she spend building the castle?

Hidden question: How many hours did April surf?  $\frac{1}{3} \times 6 = 2$ 

6 - 2 = 4; 4 hours

2. Bill put gasoline in 2 of his 5-gallon cans and 4 of his 2-gallon cans. He filled all the cans to the exact capacity. How many gallons of gasoline did he buy?

How many gallons are in two 5-gallon cans?

Hidden question 12 × 5 = 10

How many gallons are in four 2-gallon cans?

Hidden question  $24 \times 2 = 8$ 

10 + 8 = 18; 18 gallons of gas Solution:

It costs Le Stor \$20 to buy a shirt. The store sells the shirt for  $2\frac{1}{2}$  times its cost. What 3. is the profit for 100 of these shirts? Hint: Profit equals sales minus cost.

What is the selling price of the shirt?

Hidden question  $12\frac{1}{2} \times \$20 = \$50$ 

Hidden question 2: What is the profit for one shirt?

\$50 - \$20 = \$30

# Problem Solving: **Multiple-Step Problems**

Write and answer the hidden question(s) in each problem. Then solve the problem.

Tiwa spent 1½ hours setting up her computer. It took her 3 times as long to install the software. How long did it take Tiwa to set up the computer and install software?

How many hours did it take to install software? 1.

Hidden question(s):  $3 \times 1 = 4$ 

 $1\frac{1}{2} + 4\frac{1}{2} = 6$ ; 6 hours

Solution:

Lon bought 40 ounces of sliced ham. He used  $\frac{3}{4}$  of the ham to make sandwiches for 2. his friends and  $\frac{1}{5}$  of the ham in an omelet. How many ounces of ham were left? How many ounces of ham were used to make Hidden question(s): sandwiches? 3/4 × 40 = 30; How many ounces

of ham were used in the omelet?  $40 \times \frac{1}{5} = 8$  40 - 30 - 8 = 2; 2 ounces Solution:

Lionel cut off  $\frac{1}{6}$  of a 48-inch piece of rope. Marsha cut off  $\frac{1}{4}$  of a 36-inch piece of 3. rope. They compared their cut pieces. Whose piece is longer? How much longer?

Hidden question(s): How long is Lionel's cut piece?  $\frac{1}{6} \times 48 = 8$ ; How long is Marsha's cut piece?  $\frac{1}{4} \times 36 = 9$ 

Solution: Marsha's rope is 1 inch longer: 9 8 = 1.

Melanie bought 3 CDs. The country music CD cost \$15. The rock music CD cost  $\frac{2}{3}$ 4. as much as the country music CD. The platinum edition CD cost twice as much as the rock CD. What was the cost of the three CDs?

was the cost of the three CDs? How much did the rock CD cost?  $\frac{2}{3} \times $15 = $10$ ;

Hidden question(s): How much did the platinum CD cost?

 $2 \times \$10 = \$20$ 

\$15 + \$10 + \$20 = \$45

Writing to Explain Choose one of the problems above. Explain how you determined the hidden question and why it was necessary to answer that question in order to solve the problem.

Sample answer: In Problem 1, the question asks for the time spent on two tasks, so I needed to add the two times to answer the question. Only the time for one task was given in the problem, so the hidden question had to be to find the other time.

**Patterns** 

# **Fraction Figures**

Divide the square into fourths.

1. How many fourths do you see?

4

Divide one of the fourths into fourths.

2. How many total sections are there?

7

**3.** Continue the pattern three more times. Each time you divide a new section into fourths, tell how many total sections you have.

10, 13, 16

**4.** What pattern do you see in the number of sections?

### Add 3

**5.** Divide the rectangle into thirds. Divide one of the thirds into thirds. Continue the pattern three more times.

6. What pattern do you see in the number of sections?

Add 2