

SYMBOLIC DERIVATIVE AP STYLE QUESTION**Name:***AP Calculus*

Try this fun problem!

$g(x)$ and $f(x)$ are both thrice-differentiable functions where $g(x) = e^{ax} + f'(x)$ where a is a constant and

| | | | |
|--------------|---------------|--------------|----------------|
| $f(0) = 2$ | $f'(0) = -2$ | $f''(0) = 3$ | $f'''(0) = -4$ |
| $f'(-1) = 4$ | $f'(1) = e^2$ | $f''(1) = 2$ | $f'''(1) = -3$ |

- a) Calculate $g'(0)$ in terms of a
- b) Calculate $g''(1)$ in terms of e and a
- c) Write the equation of the line tangent to $g(x)$ at $x = 0$ in terms of a
- d) Knowing $g(x)$ has an inflection point at $x = 0$ find the positive value of a
- e) Using that value of a , compute the average rate of change of $g(x)$ on the interval $[0,1]$ in terms of e
- f) Using that value of a , and $h(x) = f(g(x))$ compute $h'(0)$