## Advanced Algebra

Spring Semester Review: Part III

Evaluate each of the following logarithms.

1) 
$$\log_2 32 =$$

$$2) \log_4\left(\frac{1}{64}\right) =$$

3) 
$$\log_3 0 =$$

4) 
$$\log_5 5^3 =$$

5) 
$$\ln e^4 =$$

Write each of the following in logarithmic form.

1) 
$$5^2 = 25$$

2) 
$$10^{-3} = .001$$

3) 
$$3^{-2} = \frac{1}{9}$$

4) 
$$4^{-3} = \frac{1}{64}$$

Write each of the following as a single logarithm.

1) 
$$\log_2 8 + 3\log_2 x + 5\log_2 y$$

2) 
$$(4\log_3 x + 2\log_3 y) - (\log_3 9 + 2\log_3 z)$$

3) 
$$\ln x + \ln y - \ln z$$

4) 
$$\log_2 8 + \log_4 16 - \log_3 9$$

Expand each of the following logarithms.

1) 
$$\log_3 x^3 y^2 z^5$$

2) 
$$\log \frac{2x^2y^6}{a^2b^5}$$

3) 
$$\log_2(x+4)^2 y^5$$

4) 
$$\log_5\left(\frac{x^2}{y^4}\right)^3$$

Solve each of the following equations.

1) 
$$25^{2x} = 125$$

2) 
$$\log_2 4x = 5$$

3) 
$$\log(7x+1) = \log(x-2)+1$$

4) 
$$\log(3x+1) = 2$$

5) 
$$\log 5 - \log 2x = 1$$

6) 
$$\ln x + \ln(x+1) = 2$$