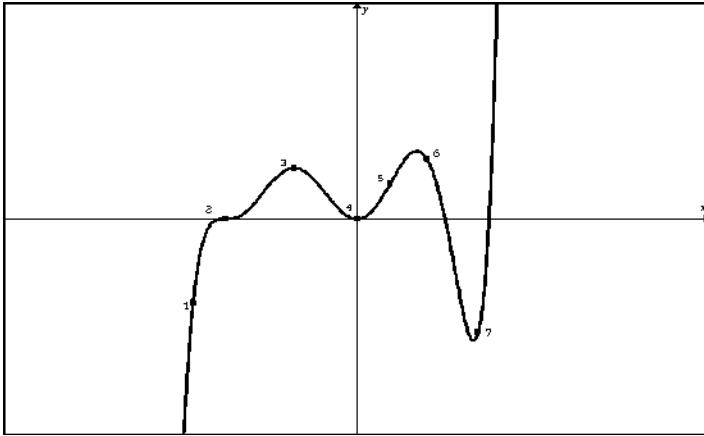


Quiz Meaning of Derivatives 2019 A.doc

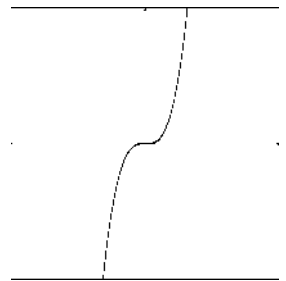
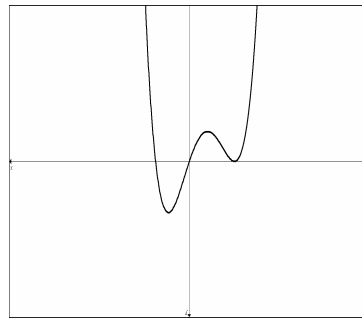
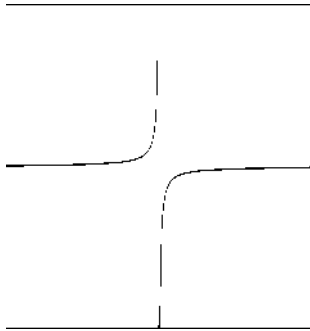
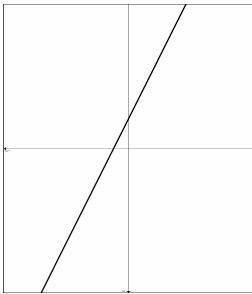
Name:

Introduction to Calculus

1. Given the function $f(x)$ below, indicate if $f(x)$, $f'(x)$, and $f''(x)$ are positive, negative, or zero at each point.



2. Sketch the first derivative of each of the following functions.



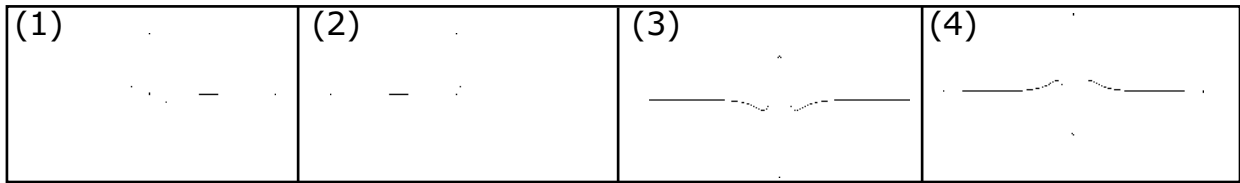
- 3) Find the derivative of $f(x)$ below using the limit definition of the derivative,

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

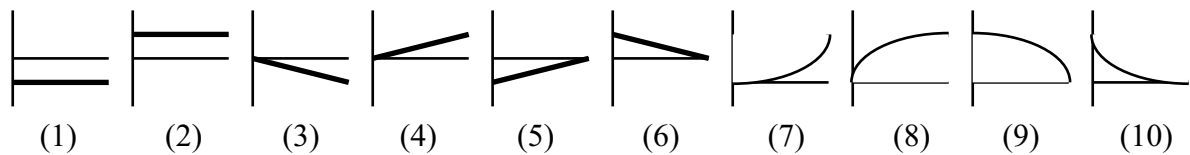
$$f(x) = x^2 - 3x + 7$$

4) Which of the functions below are the first and second derivatives of function $f(x)$ below?

$f(x) \rightarrow$  $f'(x) = \underline{\hspace{2cm}}$ $f''(x) = \underline{\hspace{2cm}}$



Questions 5 & 6 refer to the graphs below.



5) In an experiment, the temperature, $f(t)$, of a liquid is measured every minute for 10 minutes. Assume temperature is a function of time, t . Each minute during the experiment the temperature is decreasing by less than it did the previous minute.

_____ a) Which graph above best represents $f(t)$?

_____ b) Which graph above best represents $f'(t)$?

_____ c) Which graph above best represents $f''(t)$?

_____ d) What are the units of f' ?

(1) minutes per degree

(3) degrees

(2) degrees per minute

(4) degrees per minute per minute

6) Sharks continue to grow larger throughout their entire lives; however, their rate of growth slows as they get older. Length, $f(x)$, is a function of age, x .

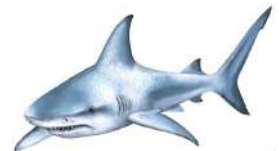
_____ a) Which graph above best represents $f(x)$?

_____ b) Which is true about $f''(x)$?

(1) $f''(x) > 0$

(2) $f''(x) < 0$

(3) $f''(x) = 0$



c) Use function notation to write the following:

_____ A 16 foot shark is 12 years old.

_____ An "**a**" year old shark's growth is slowing at a rate of "**b**".