

1) Find the following limits. If the limit *Does Not Exist* state D.N.E. and why ($+\infty, -\infty$, left $\neq$ right).

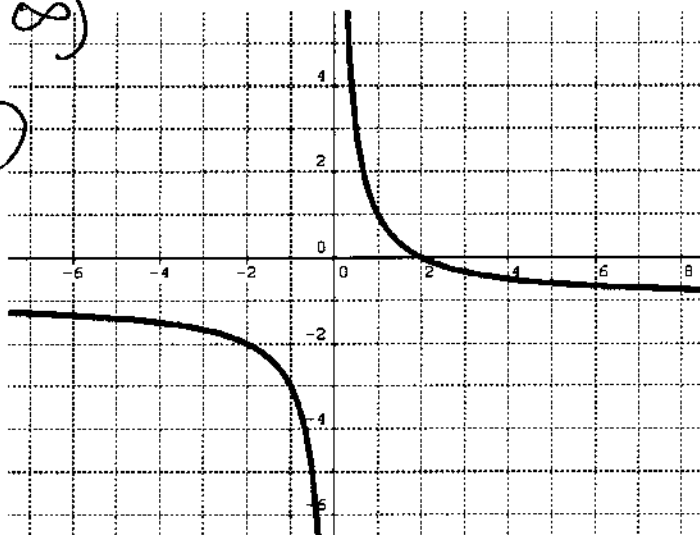
a) $\lim_{x \rightarrow 0^-} f(x) = \text{DNE } (-\infty)$

b) $\lim_{x \rightarrow 0^+} f(x) = \text{DNE } (\infty)$

c) $\lim_{x \rightarrow \infty} f(x) = -1$

d) $\lim_{x \rightarrow -\infty} f(x) = -1$

e) $\lim_{x \rightarrow 2} f(x) = 0$



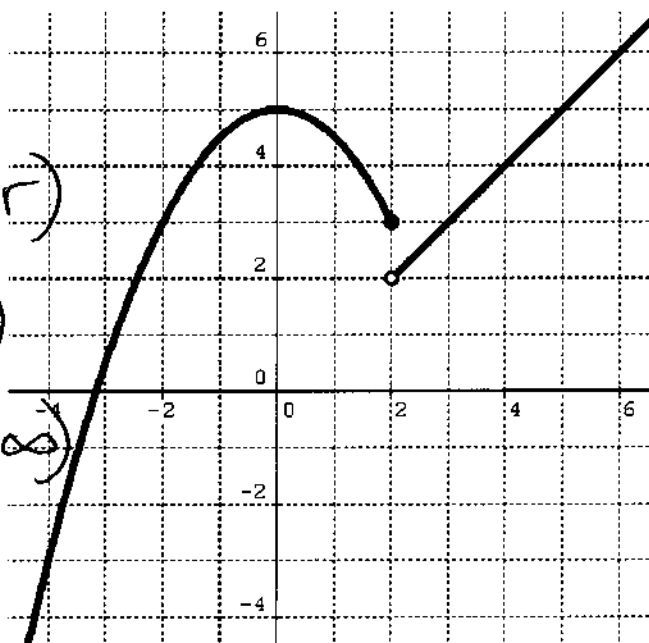
e) $\lim_{x \rightarrow 2^+} f(x) = 2$

f) $\lim_{x \rightarrow 2} f(x) = \text{DNE } (l \neq r)$

h) $\lim_{x \rightarrow \infty} f(x) = \text{DNE } (\infty)$

i) $\lim_{x \rightarrow -\infty} f(x) = \text{DNE } (-\infty)$

j) $\lim_{x \rightarrow 0} f(x) = 5$



2) Describe in words what it means to find the limit of a function as we approach a given x value.

The limit of a function is the y value that you get infinitely close to as you get infinitely close to a given x -value.

Find the following limits. Circle the correct answer **AND** show work whenever possible.

3) $\lim_{x \rightarrow -3^-} \frac{x-3}{x+3} = \frac{-6}{0}$ (a) -1 (b) 0 (c) $DNE(\infty)$ (d) $DNE(-\infty)$

$\frac{-3.5-3}{-3.5+3} = +$ $\frac{-3.9-3}{-3.9+3} = \text{more } +$ so heading up towards ∞

4) $\lim_{x \rightarrow -\infty} \frac{x^3 + 8x^2 + 1}{-9x^2 + x - 2}$ (a) $-\frac{1}{9}$ (b) $\frac{3}{4}$ (c) $DNE(\infty)$ (d) $DNE(-\infty)$

end behavior $\frac{-\text{huge}}{-\text{smaller}}$

5) $\lim_{x \rightarrow -6^+} \frac{x+6}{2x^2 + 13x + 6} = \frac{0}{0}$ (a) -11 (b) 0 (c) $-\frac{1}{11}$ (d) $\frac{1}{13}$

$\frac{x+6}{(x+6)(2x+1)} \Rightarrow \frac{1}{2x+1} \Rightarrow \frac{1}{2(-6)+1} = -\frac{1}{11}$

6) $\lim_{x \rightarrow -2^+} \frac{x^3 + 2x^2 + 2x + 4}{x+2} = \frac{0}{0}$ (a) -2 (b) 6 (c) $DNE(\infty)$ (d) $DNE(-\infty)$

$\frac{x^2(x+2) + 2(x+2)}{x+2} \Rightarrow \frac{(x+2)(x^2+2)}{x+2} \Rightarrow (-2)^2 + 2 = 6$

7) $\lim_{x \rightarrow -4^-} \frac{x+4}{x^2 - 8x - 16} = \frac{0}{32}$ (a) $-\frac{1}{8}$ (b) 0 (c) $DNE(\infty)$ (d) $DNE(-\infty)$

$= 0$

8) $\lim_{x \rightarrow \infty} \frac{-x^2 + 5x - 6}{5x^2 + 1}$ (a) $-\frac{1}{5}$ (b) 0 (c) $DNE(\infty)$ (d) $DNE(-\infty)$

end behavior

9) $\lim_{x \rightarrow 0^-} \frac{x+7}{x^2 + 7x} = \frac{7}{0}$ (a) 0 (b) 7 (c) $DNE(\infty)$ (d) $DNE(-\infty)$

$\frac{-1+7}{(-1)^2 + 7(-1)} = \frac{+}{-} = \text{neg.}$

$\frac{-0.1+7}{(-0.1)^2 + 7(-0.1)} = \frac{+}{-} = \text{more neg.}$