

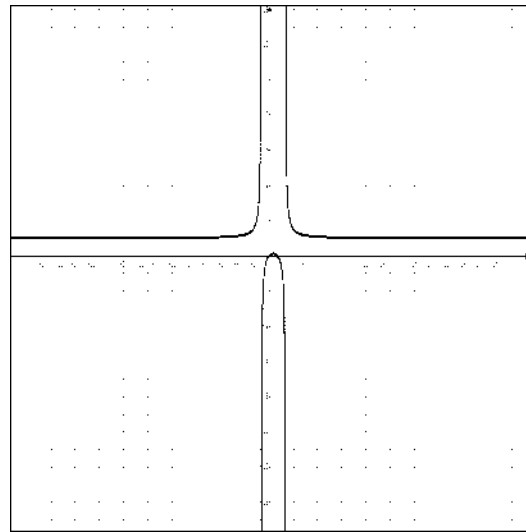
1) Find the following limits. If the limit *Does Not Exist* state D.N.E. and why ( $+\infty$ ,  $-\infty$ , *left*  $\neq$  *right*).

a)  $\lim_{x \rightarrow -1^-} f(x) =$

b)  $\lim_{x \rightarrow -1^+} f(x) =$

c)  $\lim_{x \rightarrow 0} f(x) =$

d)  $\lim_{x \rightarrow -\infty} f(x) =$



e)  $\lim_{x \rightarrow -5} f(x) =$

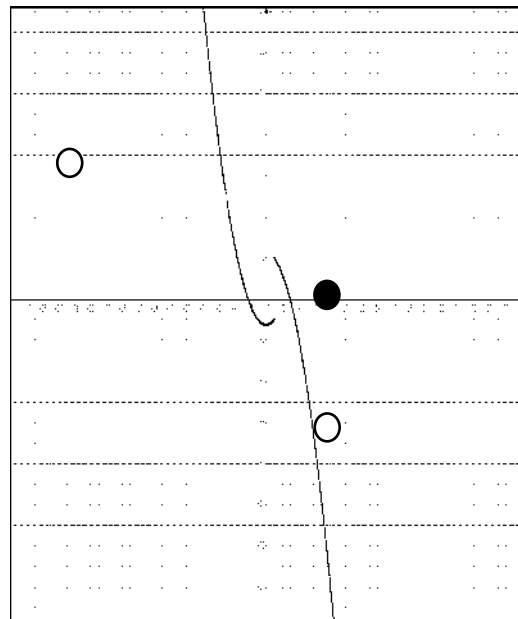
f)  $\lim_{x \rightarrow 1^+} f(x) =$

g)  $\lim_{x \rightarrow 1^-} f(x) =$

h)  $\lim_{x \rightarrow 1} f(x) =$

i)  $\lim_{x \rightarrow -3} f(x) =$

j)  $\lim_{x \rightarrow \infty} f(x) =$



2) Find the following limits.

a)  $\lim_{x \rightarrow -\infty} \frac{-8x^2 + 3x + 9}{x^3 + x - 7}$

b)  $\lim_{x \rightarrow \infty} \frac{4x^2 - 2x}{4 - x}$



3) Find the following limits algebraically. (SHOW YOUR WORK.)

a)  $\lim_{x \rightarrow 0} \frac{x-1}{x^3 + 5x^2}$

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b)  $\lim_{x \rightarrow -6} \frac{x+6}{x^2 + 4x - 12}$

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c)  $\lim_{x \rightarrow -2} \frac{x^3 - 1}{x^2 - 2x + 1}$

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**Bonus Question:** Fill in the blanks with the correct number of discontinuities.

The piecewise function shown has:

\_\_\_\_\_ jump

\_\_\_\_\_ removable (point)

\_\_\_\_\_ infinite (asymptotic) discontinuities.

$$f(x) = \begin{cases} \frac{x^2}{x^2 + 1} & (x < 0) \\ \frac{x^2}{x^2 - 1} & (x \geq 0) \end{cases}$$