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Name Answers

Find the derivative of each function. Simplify each answer.

1) $y = 2x^5 + \frac{3x^{2/3}}{4} + 2\cos(x) - (6)^x + 8$

$y' = 10x^4 + \frac{1}{2}x^{-1/3} - 2\sin x - (\ln 6)6^x$

4 pts
each

-1
if no
y'

2) $g(x) = x^3 \cdot \sin(x)$ Product (+2)

$g'(x) = 3x^2 \sin x + x^3 \cos x$ or $x^2(3\sin x + x \cos x)$

3) $f(x) = 2(10)^{3x^2}$

$f'(x) = 2 \ln 10 \cdot 10^{3x^2} \cdot 6x$
 $= 12 \ln 10 \cdot x \cdot 10^{3x^2}$

4) $f(x) = \frac{6x+1}{5x-2}$

$f'(x) = \frac{6(5x-2) - (6x+1)5}{(5x-2)^2}$ (+3)

$= \frac{30x - 12 - 30x - 5}{(5x-2)^2}$ (+1 to simplify)

$= \frac{-17}{(5x-2)^2}$

$$5) y = \sin^5(x^4 - 2x) = (\sin(x^4 - 2x))^5$$

$$y' = 5 (\sin(x^4 - 2x))^4 \cdot \cos(x^4 - 2x) (4x^3 - 2) \quad (+4)$$

$$6) h(x) = \frac{8x}{e^{2x+1}}$$

$$h'(x) = \frac{8e^{2x+1} - 8x \cdot e^{2x+1} \cdot 2}{(e^{2x+1})^2} = \frac{8 - 16x}{e^{2x+1}}$$

Find the derivative of each function. Do NOT simplify answers.

$$7) f(x) = e^{\sin x} \sqrt{(2x^3 - 4x)}$$

No product (-2)

$$f'(x) = e^{\sin x} \cos x (2x^3 - 4x)^{\frac{1}{2}} + e^{\sin x} \cdot \frac{1}{2} (2x^3 - 4x)^{-\frac{1}{2}} (6x^2 - 4)$$

$$8) f(x) = \left(\frac{2x-3}{3x^2+5x-1} \right)^9 \quad \text{or} \quad \frac{(2x-3)^9}{(3x^2+5x-1)^9}$$

$$f'(x) = 9 \left(\frac{2x-3}{3x^2+5x-1} \right)^8 \left(\frac{2(3x^2+5x-1) - (2x-3)(6x+5)}{(3x^2+5x-1)^2} \right)$$

or

$$f'(x) = \frac{9(2x-3)^8 \cdot 2 \cdot (3x^2+5x-1)^9 - (2x-3)^9 \cdot 9(3x^2+5x-1)^8 (6x+5)}{((3x^2+5x-1)^9)^2}$$