

Name \_\_\_\_\_

1) For each function  **$f(x)$**  below, determine the number of...

FIND HOW MANY

3 Critical Points

1 Relative Maximums

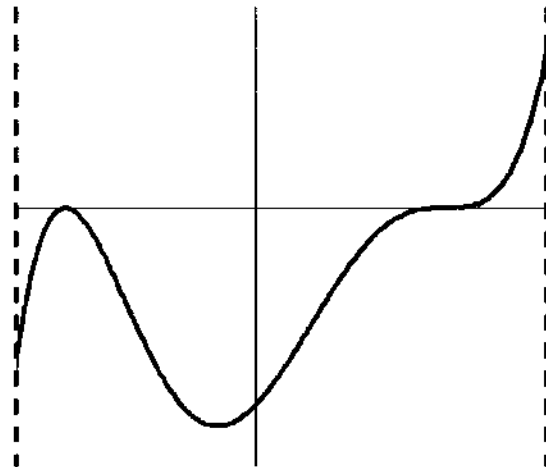
1 Relative Minimums

1 Absolute Maximums

1 Absolute Minimums

3 Inflection Points

Domain is all  $x$  values between dashed lines.



3 Critical Points

1 Relative Maximums

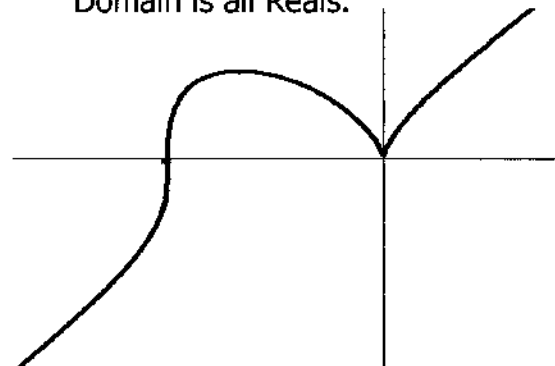
1 Relative Minimums

0 Absolute Maximums

0 Absolute Minimums

1 Inflection Points

Domain is all Reals.



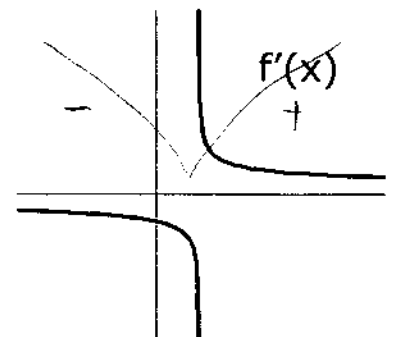
2) The graph of  **$f'(x)$**  is shown below. Given that the original function,  $f(x)$ , is defined for all real numbers, which must be true about the original function?

(1)  $f(x)$  has 1 critical point which is a local (relative) maximum.

☒ (2)  $f(x)$  has 1 critical point which is a local (relative) minimum.

(3)  $f(x)$  has 1 critical point which not a maximum or minimum.

(4)  $f(x)$  has no critical points.

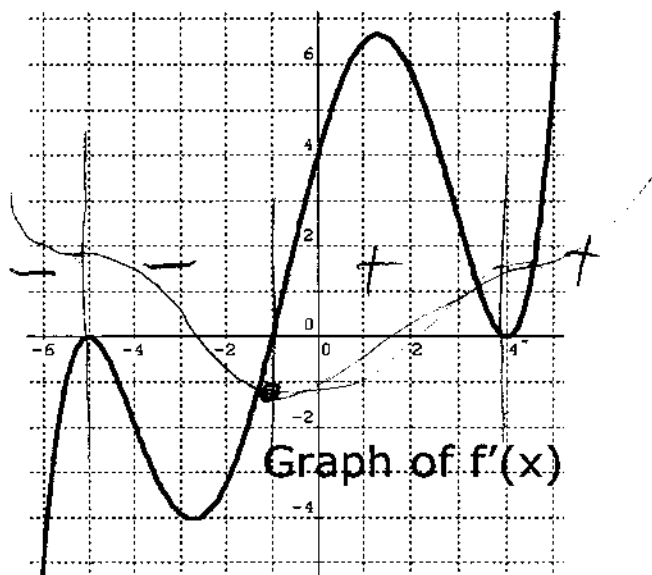


3) Use the graph of  $f'(x)$  shown to determine at which x-values the original function  $f(x)$  has...

Critical point(s) at  $x = \underline{-5, -1, 4}$

Relative maximum(s) at  $x = \underline{\text{NONE}}$

Relative minimum(s) at  $x = \underline{-1}$



4) Use the **first derivative** and **second derivative** to determine the x-values of the critical points, maximums and minimums, concavity, and inflection points. Then sketch a curve that approximates the function.

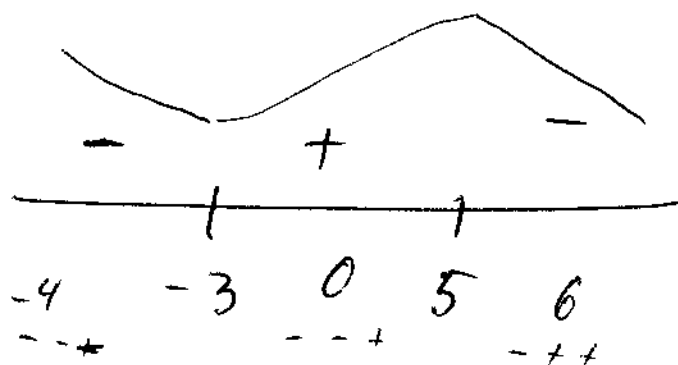
$$f(x) = -\frac{1}{3}x^3 + x^2 + 15x$$

$$f'(x) = -x^2 + 2x + 15$$

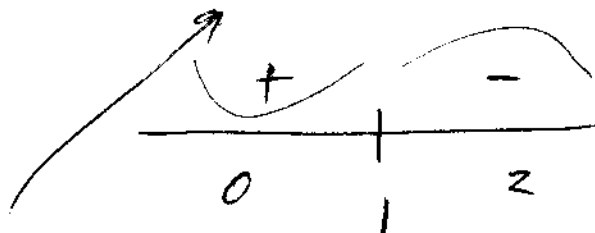
$$0 = -1(x^2 - 2x - 15)$$

$$0 = -1(x - 5)(x + 3)$$

$$x = 5 \quad x = -3$$



$$f''(x) = -2x + 2$$



Critical Point(s):  $x = 5, x = -3$

Local Maximum(s):  $x = 5$

Local Minimum(s):  $x = -3$

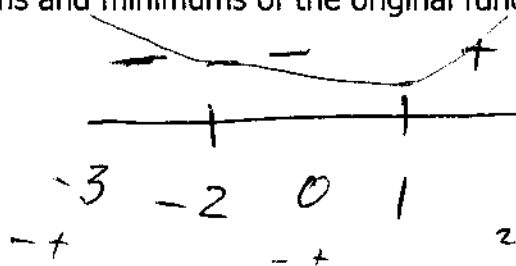
Inflection Point(s):  $x = 1$

$$-2x + 2 = 0$$

$$-2x = -2$$

$$x = 1$$

5) Given the **first** derivative of a function  $f'(x) = 6(x-1)(x+2)^2$  determine the x-values of the critical points, maximums and minimums of the original function.



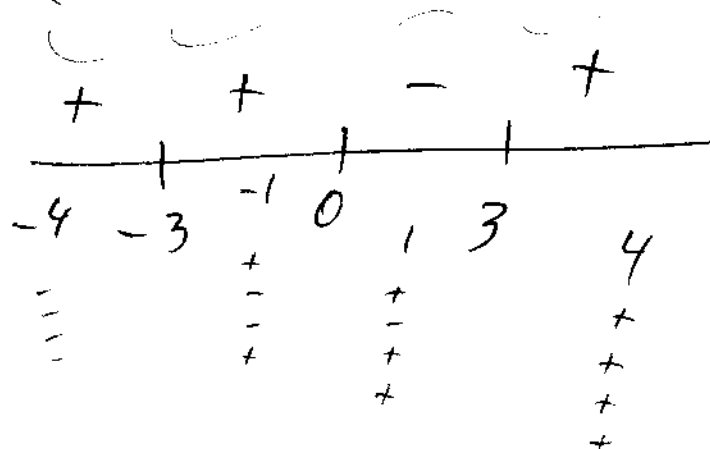
Critical Point(s):  $x = -2, x = 1$

Maximum(s): ~~1~~ NONE

Minimum(s):  $x = 1$

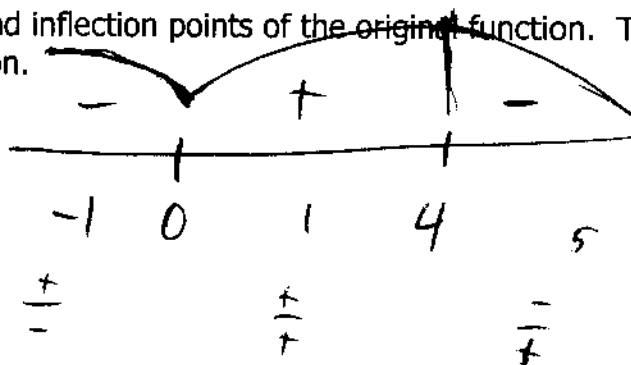
6) Given the **second** derivative of a function  $f''(x) = (x^2 - 9)(x^2 + 3x)$  determine the x-values of the inflection points of the original function.

$$0 = (x+3)(x-3)(x)(x+3)$$



Inflection Point(s):  $x = 0, x = 3$

7) Given the **first** derivative of a function  $f'(x) = \frac{4-x}{x}$  determine the x-values of the critical points, maximums, minimums, and inflection points of the original function. Then sketch a curve that approximates the function.



Critical Point(s) at  $x = 0, 4$

Maximum(s) at  $x = 4$

Minimum(s) at  $x = 0$

Inflection Point(s) at  $x = \text{None}$

Sketch of  $f(x)$ :

$$f''(x) = \frac{-1(x) - (4-x)}{x^2}$$

$$f''(x) = -\frac{x-4+x}{x^2}$$

$$f''(x) = -\frac{4}{x^2}$$

always negative  
concave down

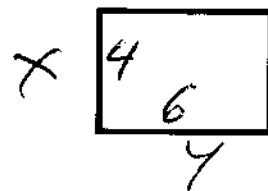
**Bonus:** The length of a rectangle is decreasing at a rate of 2 cm/sec while the width is increasing at a rate 3 cm/sec. When the length is 6 cm and the width is 4 cm find the rate of change of the area.

$$A = xy$$

$$\frac{dA}{dt} = \frac{dx}{dt}y + x\frac{dy}{dt}$$

$$\frac{dy}{dt} = -2$$

$$\frac{dx}{dt} = 3$$



$$\frac{dA}{dt} = (4)(3)(6) + (4)(-2)$$

$$\frac{dA}{dt} = 10$$