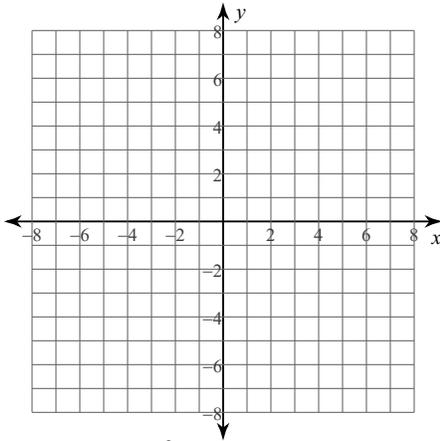


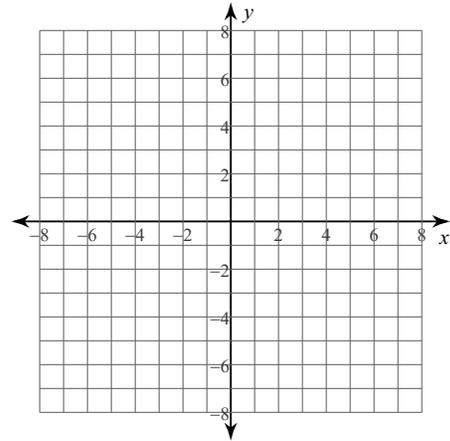
Chapter 3 Retest packet

Identify the holes, vertical asymptotes, and horizontal asymptote of each. Then sketch the graph.  
(No Calculator portion of the test)

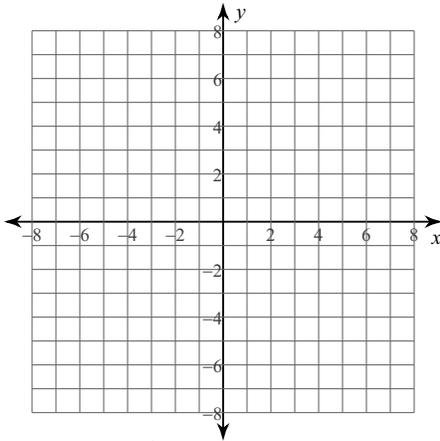
1)  $f(x) = \frac{-x - 3}{x + 1}$



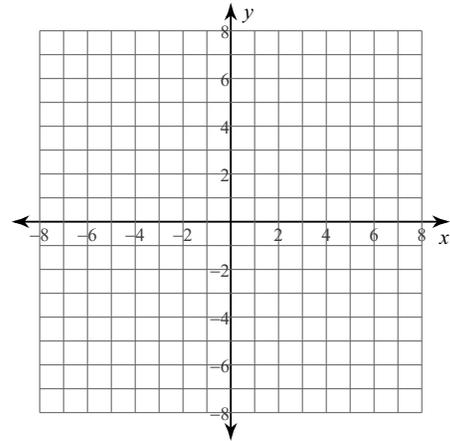
2)  $f(x) = \frac{x + 3}{x^2 + 3x}$



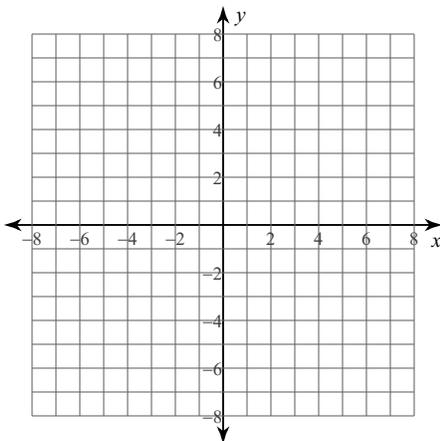
3)  $f(x) = \frac{x^2 + 3x - 4}{4x^2 - 12x + 8}$



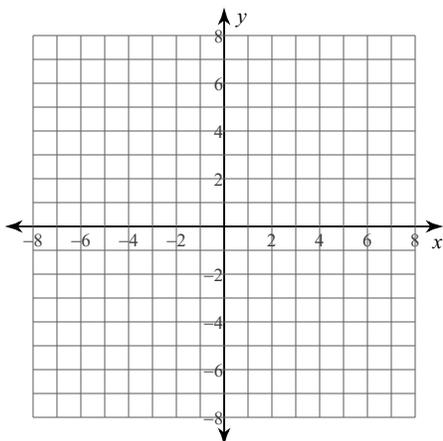
4)  $f(x) = \frac{2x + 8}{x + 1}$



5)  $f(x) = \frac{x^2 + x - 2}{4x + 16}$



$$6) f(x) = \frac{x^2 - 5x + 4}{-4x^2 + 4x + 24}$$



**Find the slant asymptote for each function. (No calculator portion)**

$$7) f(x) = \frac{x^2 + 3x + 4}{x + 2}$$

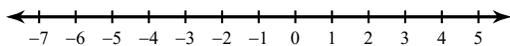
$$8) f(x) = \frac{6x^2 - 17x + 12}{3x - 4}$$

$$9) f(x) = \frac{x^3 + 1}{x^2}$$

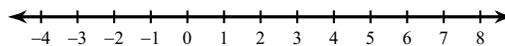
$$10) f(x) = \frac{3x^3 - 2x + x - 4}{x^2 + 1}$$

**Solve each inequality and graph its solution. (No calculator portion)**

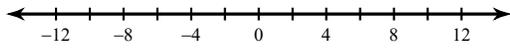
$$11) |3 - 5x| > 2$$



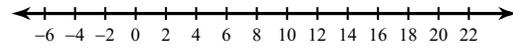
$$12) |6 + 9p| < 21$$



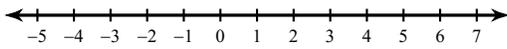
$$13) \quad |-3 - 8x| > 69$$



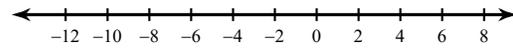
$$14) \quad |8 - a| \geq 11$$



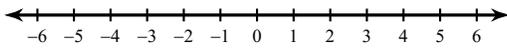
$$15) \quad |7x - 4| + 2 < 19$$



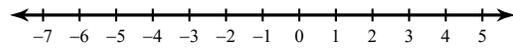
$$16) \quad |10 + 6n| - 2 \geq 36$$



$$17) \quad |n + 1| - 1 < -12$$

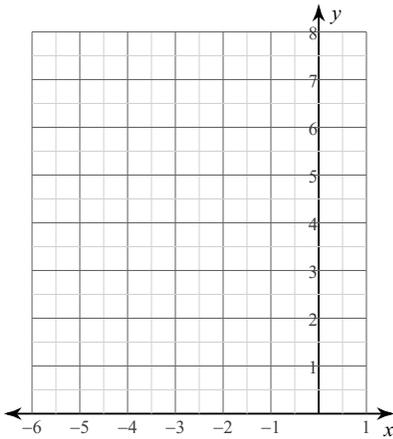


$$18) \quad 5 + 3|-10m - 10| \leq 95$$

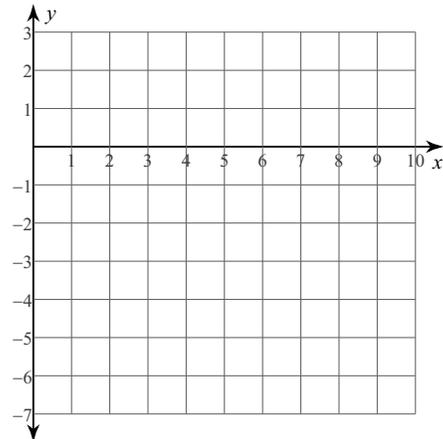


**Sketch the graph of each function. (No calculator portion)**

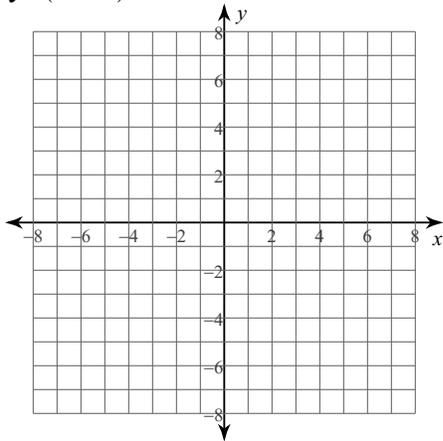
19)  $y \leq (x + 4)^2 + 3$



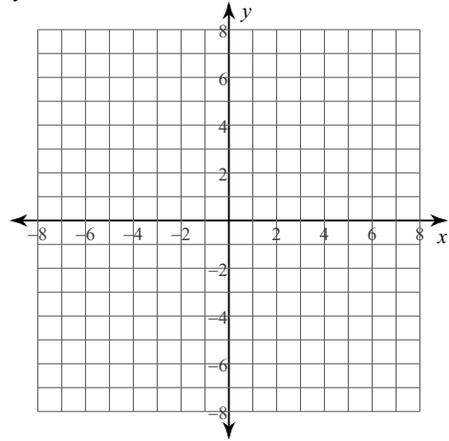
20)  $y \leq -2(x - 2)^2 + 2$



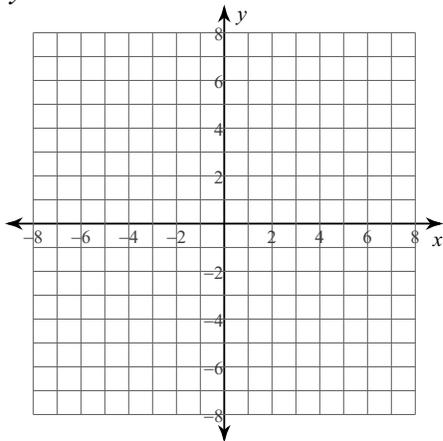
21)  $y > (x - 1)^3 + 2$



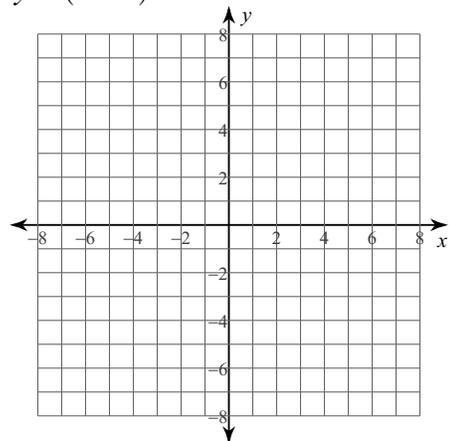
22)  $y \leq \sqrt{x - 3} - 3$



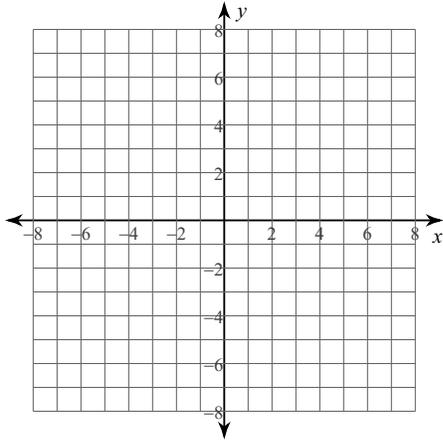
23)  $y \geq \sqrt[3]{x + 1} + 1$



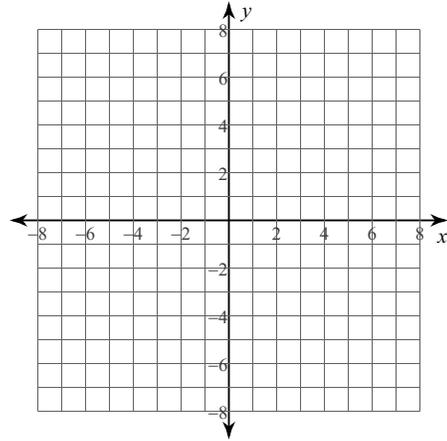
24)  $y > (x - 4)^3$



25) Sketch a function that is even.



26) Sketch a function that is odd.



27) Describe the transformation of the parent graph.

$$y = 2\sqrt{x-4} + 3$$

28) Describe the transformation of the parent graph.

$$y = -\frac{1}{2}\sqrt{x+7} - 1$$

29) Describe the transformation of the parent graph.

$$y = \left(\frac{1}{2}x - 2\right)^2 + 7$$

30) Describe the transformation of the parent graph.

$$y = -|5x + 3| - 5$$

**Determine whether each function is symmetric with respect to the x-axis, y-axis,  $y=x$ ,  $y=-x$  and/or the origin. Verify your work. (Calculators allowed)**

31)  $x + y^2 = 1$

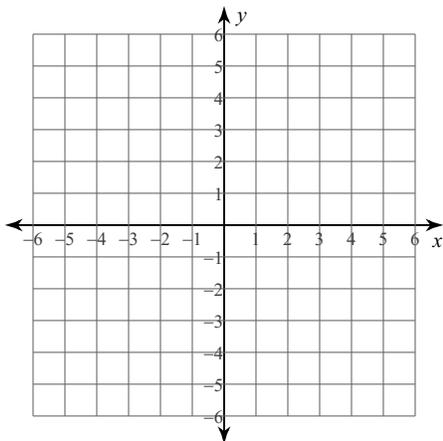
32)  $y = -5x$

33)  $y = x^3 - x$

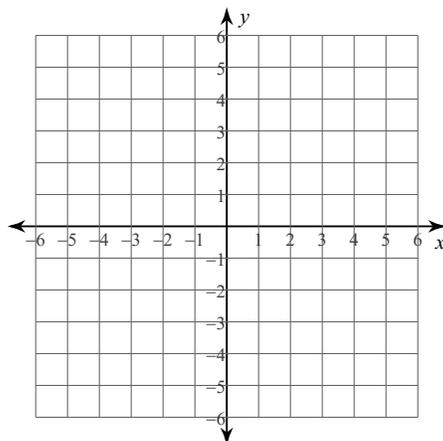
34)  $4x^2 + 9y^2 = 108$

Find the inverse of each function. Then graph the function and its inverse.

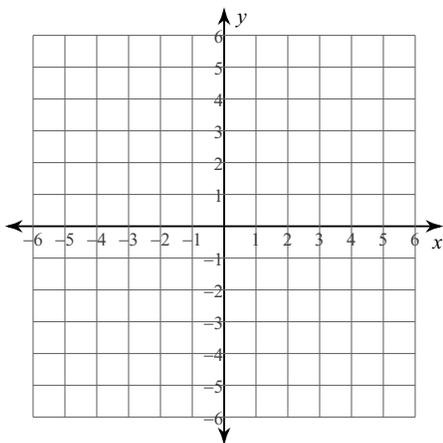
35)  $g(n) = -1 + (n - 2)^3$



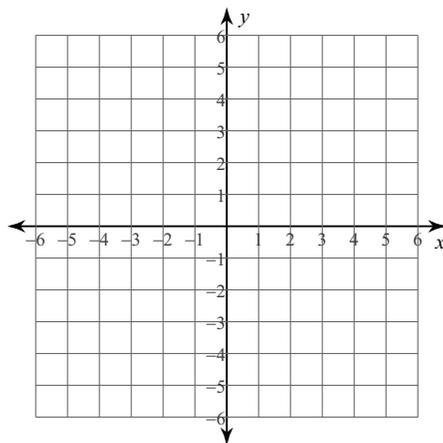
36)  $g(x) = \frac{1}{x + 1} + 1$



37)  $g(x) = \sqrt[3]{x + 2} - 2$

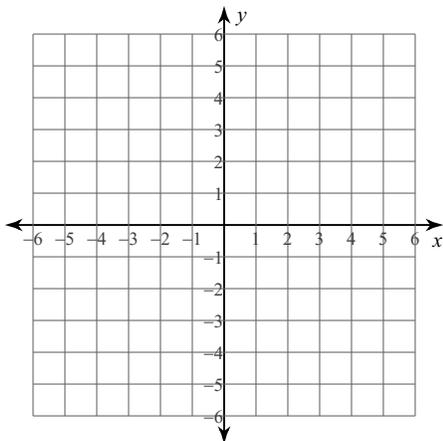


38)  $h(n) = \sqrt[5]{n + 2}$

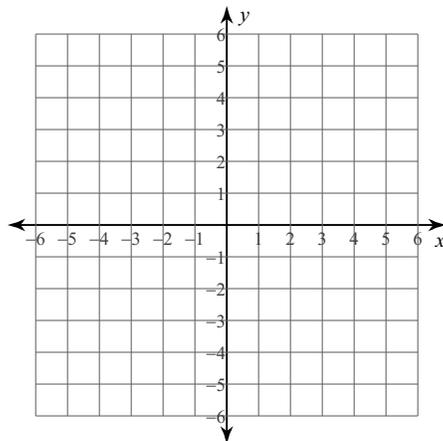


Graph each equation.

39)  $y = -2|3x - 4| + 1$



40)  $y = -2|-3x + 4| + 3$



**Describe the end behavior of each function.**

41)  $f(x) = -x^2 - 6x - 5$

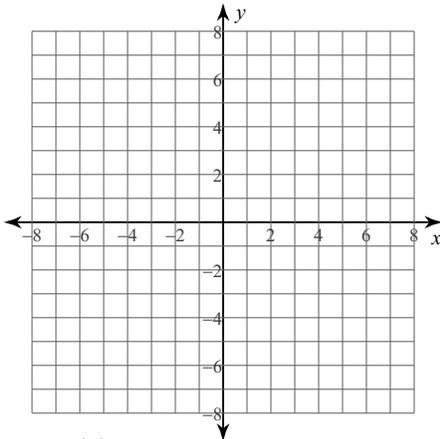
42)  $f(x) = x^5 - 4x^3 + 4x - 4$

43)  $f(x) = -x^4 + 4x^2 + x - 1$

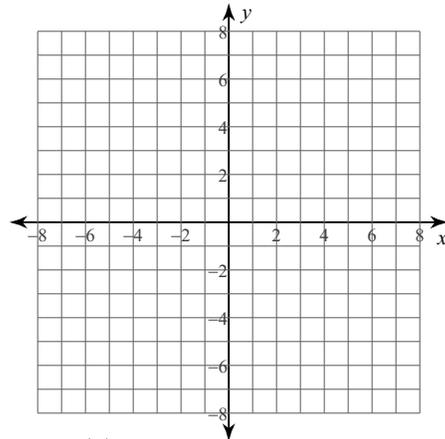
44)  $f(x) = -x^4 + x^3 + 3x^2 - 5$

**Sketch the graph of each function. Approximate the relative minima and relative maxima to the nearest tenth.**

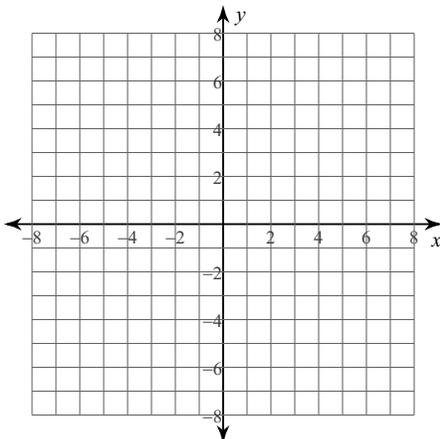
45)  $f(x) = -x^4 + x^3 + 4x^2 - 4$



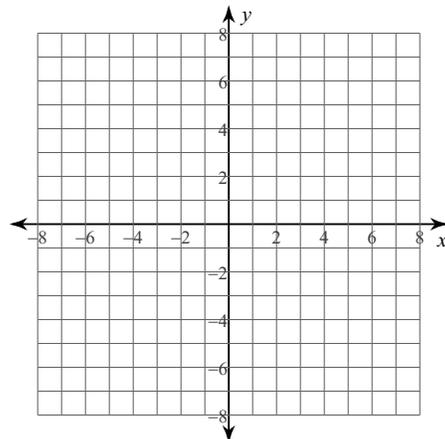
46)  $f(x) = x^3 - x^2 - 2$



47)  $f(x) = x^4 - 4x^2$



48)  $f(x) = -x^5 + 3x^3 - 2$



**Determine if the function is continuous at the given value. If discontinuous, state the type of discontinuity: point (hole), infinite (asymptote), jump.**

49)  $f(x) = x^2 + 2x - 1$  at  $x = 4$ .

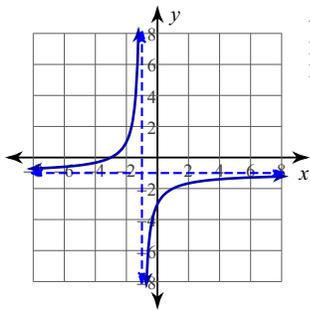
50)  $f(x) = \frac{x^2 - x - 2}{x^2 - 3x - 4}$  at  $x = 4$ .

51)  $f(x) = \frac{x^2 - x - 2}{x^2 - 3x - 4}$  at  $x = -1$ .

52)  $f(x) = \frac{x^2 - x - 2}{x^2 - 3x - 4}$  at  $x = 0$ .

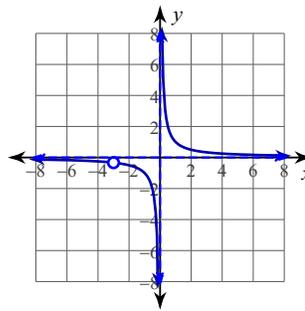
# Answers to Chapter 3 Retest packet

1)



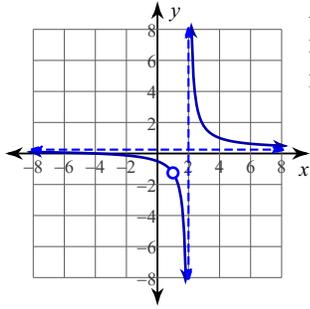
Vertical Asym.:  $x = -1$   
Holes: None  
Horz. Asym.:  $y = -1$

2)



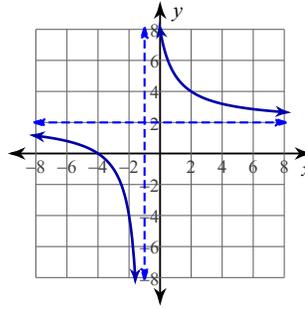
Vertical Asym.:  $x = 0$   
Holes:  $x = -3$   
Horz. Asym.:  $y = 0$

3)



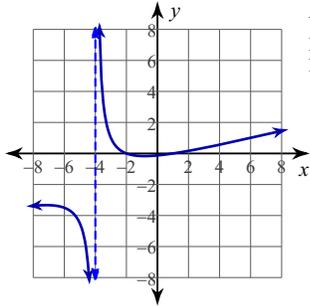
Vertical Asym.:  $x = 2$   
Holes:  $x = 1$   
Horz. Asym.:  $y = \frac{1}{4}$

4)



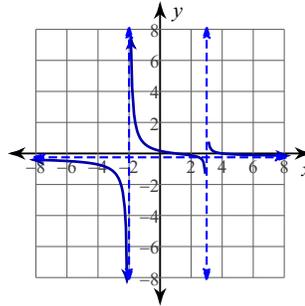
Vertical Asym.:  $x = -1$   
Holes: None  
Horz. Asym.:  $y = 2$

5)



Vertical Asym.:  $x = -4$   
Holes: None  
Horz. Asym.: None

6)



Vertical Asym.:  $x = 3, x = -2$   
Holes: None  
Horz. Asym.:  $y = -\frac{1}{4}$

7)  $y = x + 1$

8)  $y = 2x - 3$

9)  $y = x$

10)  $y = 3x - 2$

11)  $x < \frac{1}{5}$  or  $x > 1$ :

12)  $-3 < p < \frac{5}{3}$ :

13)  $x < -9$  or  $x > \frac{33}{4}$ :

14)  $a \leq -3$  or  $a \geq 19$ :

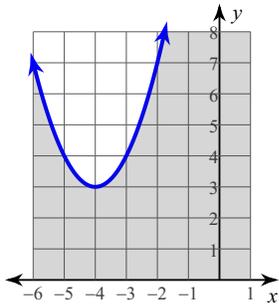
15)  $-\frac{13}{7} < x < 3$ :

16)  $n \geq \frac{14}{3}$  or  $n \leq -8$ :

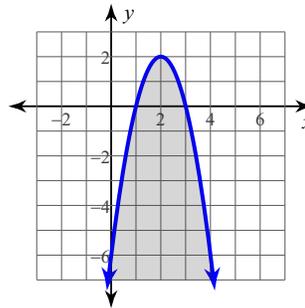
17) No solution.:

18)  $-4 \leq m \leq 2$ :

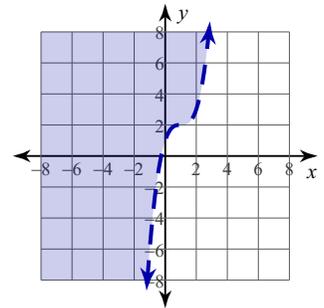
19)



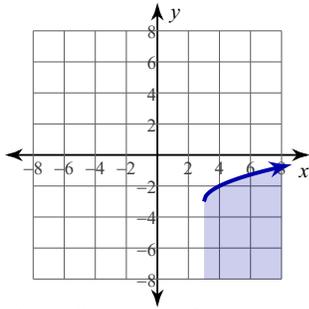
20)



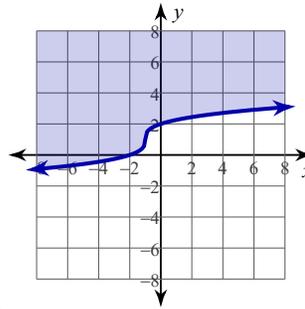
21)



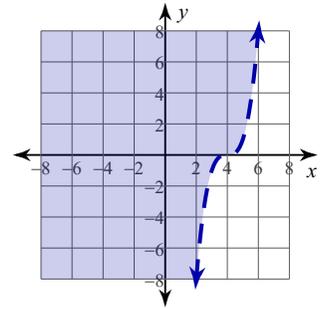
22)



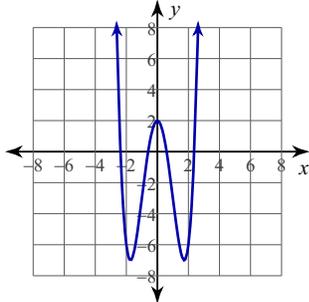
23)



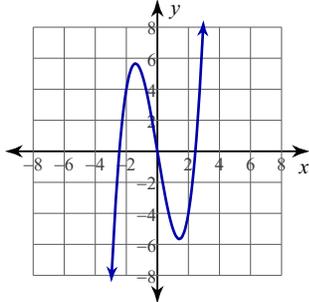
24)



25) Any function that is symmetrical to the y-axis is even.



26) Any function that is symmetrical to the origin is odd.



27) Right 4, Up 3, expands vertically

28) reflects over y-axis, Left 7, Down 1, compresses vertically

29) Right 2, Up 7, expands horizontally

30) reflects over y-axis, Left 3, Down 5, compresses horizontally

31) x-axis

32) origin

33) origin

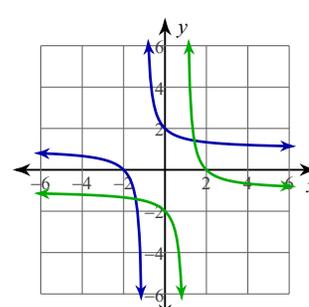
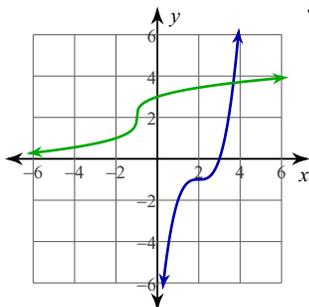
34) x-axis, y-axis

35)

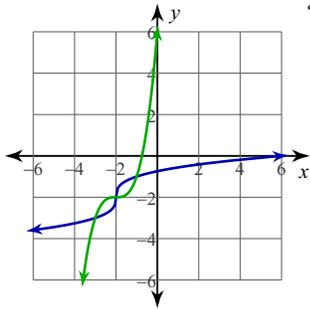
$$g^{-1}(n) = \sqrt[3]{n+1} + 2$$

36)

$$g^{-1}(x) = \frac{1}{x-1} - 1$$

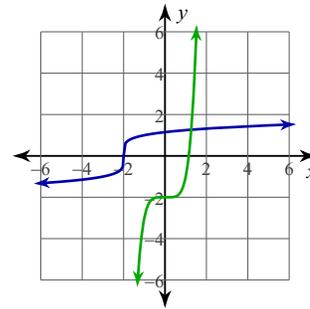


37)



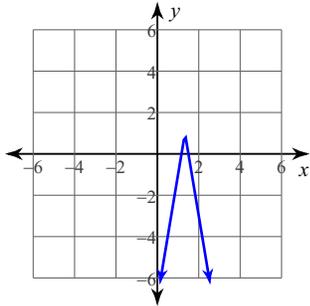
$$g^{-1}(x) = (x+2)^3 - 2$$

38)

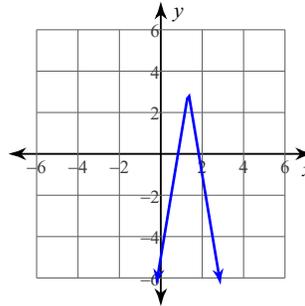


$$h^{-1}(n) = -2 + n^5$$

39)



40)



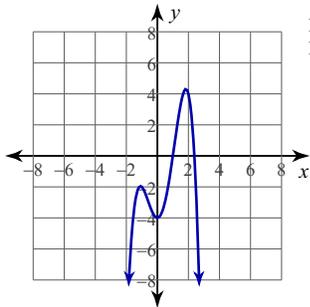
$$41) \begin{aligned} f(x) &\rightarrow -\infty \text{ as } x \rightarrow -\infty \\ f(x) &\rightarrow -\infty \text{ as } x \rightarrow +\infty \end{aligned}$$

$$42) \begin{aligned} f(x) &\rightarrow -\infty \text{ as } x \rightarrow -\infty \\ f(x) &\rightarrow +\infty \text{ as } x \rightarrow +\infty \end{aligned}$$

$$43) \begin{aligned} f(x) &\rightarrow -\infty \text{ as } x \rightarrow -\infty \\ f(x) &\rightarrow -\infty \text{ as } x \rightarrow +\infty \end{aligned}$$

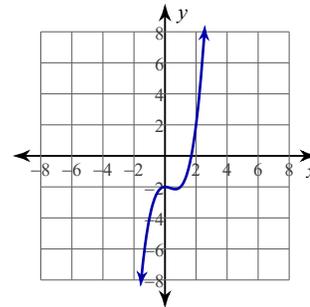
$$44) \begin{aligned} f(x) &\rightarrow -\infty \text{ as } x \rightarrow -\infty \\ f(x) &\rightarrow -\infty \text{ as } x \rightarrow +\infty \end{aligned}$$

45)



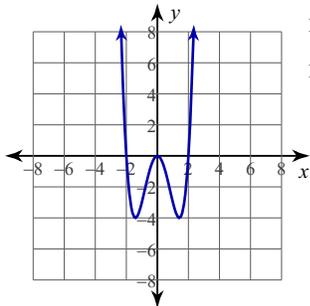
$$\begin{aligned} \text{Minima: } &(0, -4) \\ \text{Maxima: } &(-1.1, -2) \\ &(1.8, 4.3) \end{aligned}$$

46)



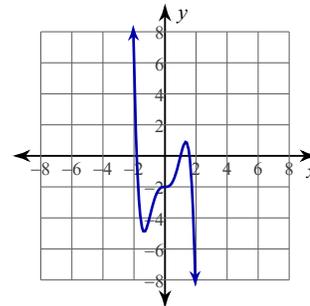
$$\begin{aligned} \text{Minima: } &(0.7, -2.1) \\ \text{Maxima: } &(0, -2) \end{aligned}$$

47)



$$\begin{aligned} \text{Minima: } &(-1.4, -4) \\ &(1.4, -4) \\ \text{Maxima: } &(0, 0) \end{aligned}$$

48)



$$\begin{aligned} \text{Minima: } &(-1.3, -4.9) \\ &(1.3, 0.9) \\ \text{Maxima: } &(0, 0) \end{aligned}$$

49) Continuous.  $f(4)$  exists and the function is approaching 23 from the left and right of  $x = 4$ .

50) Infinite discontinuity. There is a vertical asymptote at  $x = 4$ .

51) Point discontinuity. There is a hole at  $x = -1$ .

52) Continuous.  $f(0)$  exists and the function is approaching  $1/2$  from the left and right of  $x = 0$ .