Abbott Lawrence Academy 2019-2020 Curriculum Map: Year at a Glance Subject: Advanced Honors Precalculus Grade: 11th

Unit Title	Time Allocation (# weeks based on 38 weeks in school year)	Essential Questions (for unit)	Core Text/Supp lemental Learnings (include major references)	Performance Tasks (How will you know that students have mastered the taught concepts)
1. Analyzing Trigonometric Functions	5 weeks	 Where are the turning points of the cosine and sine functions? What is a radian? How can you use a graph of y = sin x to estimate solutions to the equation sin x = -0.6? How are the six trigonometric functions defined? Why does the sin⁻¹function on a calculator only return results between - ⁿ/₂ and ⁿ/₂? How many solutions are there to the equation such as cos x = 0.8? Given the maximum and minimum values of a cosine or sine function, how do you find the amplitude and vertical displacement? How can you make a sinusoidal function that has a specific period? How can use a sinusoidal function to model periodic phenomena? 	CME Project: Precalculus Common Core https://www.p earsonsuccessn et.com/ http://cmeproj ect.edc.org/ Edmodo: Virtual Classroom SMART Labs Khan Academy	 SWBAT answer the following types of questions: How can you use a graph of y = sin x to estimate solutions to the equation sin x = -0.6? Why does the sin⁻¹function on a calculator only return results between - ⁿ/₂ and ⁿ/₂? How many solutions are there to the equation such as cos x = 0.8? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how: The relationship between degree and radian measure as the length of an arc on the unit circle subtended by a central angle Relate the motion of an object around a circle to the graphs of the cosine, sine, and tangent functions Solve equations that involve cosine and sine The several relationships between the tangent function and the unit circle Sketch and describe the graph of the tangent function Define an inverse of a cosine, sine, and tangent Recognize three other trigonometric functions: secant, cosecant, and cotangent Make sense of sinusoidal functions in the context of real-world application Understand the geometry of sinusoidal functions Students are responsible for a unit project that relies on using the learned skills to express the relationship of "Trigonometry " of the unit square by exploring how one might define trigonometry on the unit square as opposed to the unit circle. They will build a construction of the square trigonometry to explain what happens and justify answers.

2. Complex Numbers and Trigonometry	4 weeks	 How can you write a complex number using trigonometry? What are the magnitude and argument of a complex number, and how do you find them? How do you use geometry to calculate something like (1 - i√3)(-3√3 + 3i)? How can you test to see if an equation might be an identity? How can you use complex numbers to find formulas for cos 2x and sin 2x ? How can you use identities to prove other identities? How do you use De Moivre's Theorem to write a rule for an equation like cos 3x ? How can you connect roots of unity to regular polygons? For what values of cos x does cos 3x = 0? 	CME Project: Precalculus Common Core <u>https://www.p</u> <u>earsonsuccessn</u> <u>et.com/</u> <u>http://cmeproj</u> <u>ect.edc.org/</u> Edmodo: Virtual Classroom SMART Labs Khan Academy Research:	 SWBAT answer the following types of questions: How do you use geometry to calculate complex numbers? How can you use complex numbers to find formulas for cos 2x and sin 2x? For what value of cos x does cos 3x = 0? How do you use De Moivre's Theorem to write a rule for a trigonometric function? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to: Graph complex numbers in the complex plan to use geometry to explain arithmetic fact of complex numbers using both rectangular coordinates and polar coordinates Test trigonometric functions to predict identities and show the Multiplication Law for complex numbers Use Pythagorean identities and algebra to prove the trigonometric equations is an identity Calculate powers of complex numbers using De Moivre's Theorem The geometry of roots of unity and the connections to roots of equations in a certain form. Find exact algebraic expression for certain trigonometric values Students are responsible for a unit project that relies on using the learned skills to read through a mathematical proof and make it their own to understand the reasons behind the steps. Students will use develop a formula for determining roots of a general cubic. Students will be able to understand how complex numbers crop in their development
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3. Analysis of Functions	5 weeks	 given its factored form? How can you determine a polynomial's behavior at very large or very small inputs? How can you use long division to find equations of secant or tangent lines to the graphs of a polynomial function? What happens to equation like if f(x) = 3x²+2x-1/5x²-3x+10 as x gets larger and larger? Why do graphs of functions like g(x) = x²-15/x-4 and h(x) = x²-16/x-4 look so different from each other? How can you find tangent lines to rational functions? What happens when interest is compounded 	CME Project: Precalculus Common Core https://www.p earsonsuccessn et.com/ http://cmeproj ect.edc.org/ Edmodo: Virtual Classroom SMART Labs Khan Academy	 Students will work in a variety of way to demonstrate mastery of the content. This unit focuses on analysis of functions which students will do by thinking about continuity and the slope of a line tangent to a graph at a point, students will part take in the following: In-class discussions: generalize the process and find an equation for the slope of the tangent to the graph of an exponential or logarithm function by finding equations for the tangent to the graph of various polynomial functions and rational functions. Mathematical reflections: Students will be assigned mathematical reflections as a study guide to make sure that students comprehend key concepts like: average rate of change continuous continuously compounded interest determinant e hole infinite discontinuity instantaneous speed linear fractional transformation, R_A power function removable discontinuity secant line Pictorial representations: students will be to visualize a line through those two points—a secant line by relating the graph of a function to the slope of its tangent at any point and use that information to analyze the graph. Project: Partial Fractions: students will be not usual the slope of its tangent at any point and use that information to evaluate sums and to graph rational function. Students will be able to explain how to produce a partial fraction decomposition for certain rational functions.
4. Combinatorics	4 weeks	 using only the digits 1 and 2? In a kindergarten class, each student has four pictures: a square, a triangle, a circle, and a star. Each of the kids will make a design by gluing these four pictures in a line. There are 20 kids in the class. Can each child make a different design or will there have to be repeats? What does it mean for two problems to be isomorphic? In how many ways can you pick three objects, in order, from a set of six distinct objects? How many three-digit numbers are there that have repeated digits? How many five-student committees are possible in a class of 26 students? 	Precalculus Common Core	 Students will work in a variety of way to demonstrate mastery of the content. This unit focuses on making sense of the linear algebra focusing on topics like solving systems of equations in matrix format. Students will learn use Gaussian Elimination. students will part take in the following: In-class discussions defining how to use various methods that can be used to count the number of elements in a set without enumerating them. Mathematical reflections: Students will be assigned mathematical reflections as a study guide to make sure that students comprehend key concepts like: anagram combination isomorphic permutation a^D_k, number of permutations of n objects. Taken at k at a time Pictorial representations: students will create various graphing techniques and tables to use the number of counting strategies to develop the habit of looking at the mathematical structure to determine what strategies make sense.

		 What is the connection between the Pascal's Paths problem and the entries in Pascal's Triangle? What is the sum of the entries in row n of Pascal's Triangle 2ⁿ? 	 Project: The Simple Locks: students will be presented with certain rules to find the "combination" to the simplex lock by using the correct permutation from all of the possible codes.9 Other common forms of assessments include: test/quizzes/homework/classwork(calculations)
5. Functions and Tables	5 weeks	 What are the differences between a closed-form definition and a recursive definition for a function? How can you prove that a closed-form and a recursive function definition agree at each of infinitely many inputs? What happens to the ratio of consecutive Fibonacci numbers? If the third differences in the table of a polynomial function are all 24, what can you say about that function? What are Mahler polynomials? How can you use differences to find a polynomial function that fits a table? How can you find a closed-form function definition that satisfies a two-term recurrence? What is the monthly payment for a three-year car loan for \$15,000, taken out at 5% APR? 	ius focuses connections to the properties of Pascal's Triangle with properties of difference tables. Students will part take in the following: www.p In-class discussions: students will talk how to connect the properties of Pascal's Triangle with properties of difference table and use the connections to construct and verify functions that fit tables. meproi Mathematical reflections: Students will be assigned mathematical reflections as a study guide to make sure that students comprehend key concepts like: o base case o closed-form definition memory Fibonacci sequence o foructional equation abs hockey-stick property Mahler polynomials Mahler polynomials
6. Analytic Geometry	5 weeks	 What is the set of points equidistant from the x-axis and the point (0,4)? How can you use coordinates to show that the diagonals of a parallelogram bisect each other? How can you find the center and radius of a circle with an equation written in normal form? How do you slice an infinite double cone with a plane to get a parabola? What is the locus definition of a hyperbola? What kind of conic section do you get when you graph x² + 16y² - 8x + 64y + 64 = 0? Virtual How can you interpret the matrix operations of sum and scalar product geometrically? 	ius focuses on learning that by choosing the "generic" coordinates students can simplify their algebraic calculations and see more meaning in them. Students will part take in the following: www.p In-class discussions defining how a slicing plane intersects a double cone at different angles, cutting off different conic sections. meproj Mathematical reflections: Students will be assigned mathematical reflections as a study guide to make sure that students comprehend key concepts like: o affine combination o conic sections memory convex combination o convex combination

		 Why might it be useful to write an equation of a line in vector form? how can you use vectors to prove that the medians of a triangle are concurrent? 	Khan Academy	 eccentricity ellipse focus, foci head and tail of a vector hyperbola locus major axis minor axis parabola point-tester power of a point, ∏. (P) signed power of a point, ∏s (P) vector, AB Pictorial representations: students will create visually create vectors on a coordinate plane and they will model conic sections as wheel as coordinate geometry. Project: The General Quadratic: students will analyze the graph of the general quadratic. Other common forms of assessments include: test/quizzes/homework/classwork(calculations)
7. Probability and Statistics	6 weeks	 If you are to roll four number cubes, what is the probability they sum to 12? What is expected value? How can you use polynomials to solve probability problems? How can you calculate the standard deviation for a large set of data? What happens to the mean, variance, and standard deviation if an experiment is repeated a second time? What is the mean and standard deviation for the number of heads on 400-coin flips? What is the Central Limit Theorem? Why is the normal distribution so common? What is the probability of rolling 10% or fewer sizes if you roll 1000 number cubes? 	CME Project: Precalculus Common Core https://www.p earsonsuccessn et.com/ http://cmeproj ect.edc.org/ Edmodo: Virtual Classroom SMART Labs Khan Academy	Students will work in a variety of way to demonstrate mastery of the content. This unit focuses on probability and statistical analysis by using patterns in the form of calculation to draw out conclusions with having to do complex calculations. Students will part take in the following: In-class discussions will revolve around having students explain how they have connected the result of the calculations in context with the problem to draw conclusions about probability situations. Mathematical reflections: Students will be assigned mathematical reflections as a study guide to make sure that students comprehend key concepts like: Bernoulli trial conditional probability control group cumulative density function expected value, E(x) experiment experimental probability frequency, A independent mean absolute deviation, or variance, σ^2 mutually exclusive normal distribution, $N(\mu, \sigma)$ observational study population parameter probability density function probability density function

		 root mean squared deviation, or standard deviation, σ sample proportion sample space sample statistic sample survey theoretical probability treatment group z-score Pictorial representations: students will create probability distributions for a series of repeated independent trials of a probability experiment in several different contexts to similarities between the graphs to understand the Central Limit Theorem. Project: Faking the Flips: students will be asked to make "truly" random data, and try to make a believable fake. Other common forms of assessments include: test/quizzes/homework/classwork(calculations)
8. 4 w Ideas of Calculus	 How can you find the area of an shaped figure? How can you estimate the area What is the area of the region u of y = x² from x = 0 to x = 1? What is a closed-form expression function defined by F(b) = s(where b > 1? What is a closed-form expression function defined by F(b) = s(where b > 1? What is Fermat's approach to fin under the graph of y = x^m betw and x = 1? What is the value of S[1,2](x⁻ What is the value of S[1,2](e^x 	Precalculus under a curve? nder the graphPrecalculus Common Corefocuses on the introduction of the ideas that underlie calculus and several different ways of

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 1 "Analyzing Trigonometric Functions" (5) Weeks

Essential Questio		 What is a rad How are the s Given the ma How can you How can use 	 How are the six trigonometric functions defined? Given the maximum and minimum values of a cosine or sine function, how do you find the amplitude and vertical displacement? How can you make a sinusoidal function that has a specific period? How can use a sinusoidal function to model periodic phenomena? 				
		 (Experimenta by making co (Encapsulatio 	• (Experimentation) work with constructions to visualize trigonometric functions. They will learn to answer questions about what they observe by making conjectures and proving theorems that they might have made conjectures about.				
Performance task Summative	ks: Formative and	 How can you Why does the How many so Students will have The relations Relate the mu Solve equation The several ru Sketch and du Define an inv Recognize the Make sense of Understand to Model with s Students are responsed by exploring how of 	SWBAT answer the following types of questions:•How can you use a graph of $y = sin x$ to estimate solutions to the equation $sin x = -0.6$?•Why does the sin^{-1} function on a calculator only return results between $-\frac{n}{2}$ and $\frac{n}{2}$?•How many solutions are there to the equation such as $cos x = 0.8$?Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how:•The relationship between degree and radian measure as the length of an arc on the unit circle subtended by a central angle•Relate the motion of an object around a circle to the graphs of the cosine, sine, and tangent functions•Solve equations that involve cosine and sine•The several relationships between the tangent function and the unit circle•Sketch and describe the graph of the tangent function•Define an inverse of a cosine, sine, and tangent•Recognize three other trigonometric functions: secant, cosecant, and cotangent				
CC Standards/ Lawrence Standards	Language Objectives The reading, speaking, writing, and listening skills will you teach,	Academic Language The formal- language skills- vocabulary,	Content Objectives What students will know and be able to do at the end of the unit	Texts and Supplemental Learnings	Cross-Content Connections		

	re-teach, or review	grammar,			
	so students will be	punctuation,			
	able to explain and	syntax,			
	apply the content,	discipline-			
	skills, and/or procedures.	specific			
		terminology,			
		••••			
		or rhetorical			
		conventions—			
		that allow			
		students to			
		acquire			
		knowledge			
A.REI.1	Students will be able to:	amplitude	Learning Goals:	CME Project: Precalculus Common	All subjects:
Explain each step in solving	• convert degree measurements to	• arc	SWBAT-	Core-Chapter 1 (pages 2-81)	The students will consider the text/lecture and
a simple equation as	radian	 asymptote 	 discuss the relationship 	core enapter i (pages 2 oi)	collaborative work to engage/learn with their
following from the equality	• explain how the radian measure is	 central angle 	between degree and radian	https://www.pearsonsuccessnet.co	notes. They will create interactive notebooks
of numbers asserted at the	used as a distance measurement	 decreasing 	measure as the length of an arc	<u>m/</u>	based off of readings, lectures, collaborative
previous step, starting from	 graph sine and cosine functions 	 increasing 	on the unit circle subtended by	http://cmeproject.edc.org/	work, assignments, etc.
the assumption that the	and define a periodic function	 inverse function 	a central angle		
original equation has a	 solve equations that involve sine 	 maximum 	 relate the motion of an object 		Geometry:
solution. Construct a viable	and cosine	 minimum 	around a circle to the graphs of	Edmodo: Virtual Classroom	The students will learn to graph the unit circle
argument to justify a	 list the trigonometric functions by 	 period 	the cosine and sine functions		to work with trigonometric function to prove
solution method.	learning the tangent and the three	periodic	 solve equations that involve 	Khan Academy	the Pythagorean Identity.
A.REI.4	reciprocal functions: secant,	 phase shift Distribution 	cosine and sine (such as	https://www.khanacademy.org/ma	Dhusian
Solve quadratic equation in one variable.	 cosecant, and cotangent model graphs of the above 	 Pythagorean Identity 	3cos $x + 2 = 1$) • compare and contrast several	th/algebra2/trig- functions/constructing-sinusoids-	Physics: The students will learn to graph functions like
one variable.	functions and demonstrate each	Identity • radian	relationships between the	alg2/v/trig-function-equation	sine and cosine to define periodic functions and
A.SSE.1	function in the unit circle to work	 secant line 	tangent function and the unit	aig2/ v/ tig-function-equation	how a period is defined.
Interpret expression that	with the basic identities	 sinusoidal 	circle	https://www.khanacademy.org/ma	
represent a quantity in	 define one-to-one functions and 	function	 sketch and describe the graph of 	th/algebra2/trig-	SAT Prep:
terms of its context	inverse functions	 turning point 	the tangent function	functions/amplitude-and-midline-	The students will learn to think about
A.SSE.1.a	 how to restrict the domain of 	 vertical 	• define an inverse of cosine, sine,	of-sinusoids-from-formulas-	standardized test questions like arc length
Interpret parts of an	cosine, sine, and tangent in order to	displacement	and tangent	alg2/v/we-amplitude-and-period	relate it to the central angle for related
expression, such as terms,	define the inverses of these		 recognize and define three 		proportional rates problem.
factors, and coefficients.	functions		other trigonometric functions:	Other:	
A.SSE.1.b	• emphasize and validate the idea		secant, cosecant, and cotangent	http://tutorial.math.lamar.edu/pdf	Biology:
Interpret complicated	that trigonometric functions are		• explain how they made sense of	/Trig_Cheat_Sheet_Reduced.pdf	Students learn about the behaviors of a
expressions by viewing one	treated as "functions as usual" ● discuss the sinusoidal function		sinusoidal functions in the	http://www.epcc.edu/OfficeofStud	function in a manner that relates to biological
or more of their parts as a single entity.	transformations through amplitude		 context of previous experience model the geometry of 	entSuccess/tutorialservices/tutorial	functions like a period function.
A.SSE.3	and shift changes		sinusoidal functions	supportservices/futorialservices/futorial	Algebra II:
Choose and produce an			 model with sinusoidal functions 	rigonometry%20Handouts%20(PDF)	Student will continue to build on the parent
equivalent form of an				/Math%20Handout%20(Trigonomet	functions that were learned from Algebra to
expression to reveal and				ry)%20Trig%20Formulas%20Web%2	build on concepts relating to more complicated
explain properties of the			Habits and Skills:	0Page.pdf	analysis of the unit circle.
quantity represented by the			SWBAT-		
expression.			 calculate cosine and sine using 	Glencoe Common Core Algebra II	Trigonometry:
A.SSE.3.b			radians directly without	text	Students will build on the concepts of the unit
Complete the square in a			converting to degree	Glencoe Common Core Precalculus	circle and the trigonometric functions and how
quadratic expression to			 visualize periodic functions, and identify the size period 	text	they relate to concepts of Precalculus.
reveal the maximum and			identify their period		Chamistru
			1		Chemistry:

minimum value of the function it defines.

A.SSE.4

Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems

F.IF.3

Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers

F.IF.4

For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.

F.IF.5

Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

F.IF.6

Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph **F.IF.7**

Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. **F.IF.7.e** Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

F.BF.1.a

• demonstrate how to "undo"

- cosine or sine to solve equations
 compare the cosine and sine functions through their relation to the unit circle and through their graphs
- model the unit circle to generate the graph of y = tan x
- visualize geometrically the tangent and secant functions by graphing
- restrict the domain of a function to make it one-to-one
- solve equations and prove identities using trigonometric functions
- demonstrate and show the graph of y = Asin (ax + b) + B is simply a transformation of the basic graph of y = sin x

Students are starting to see behaviors of functions as a method of analyzing the transformation and shift changes similar to what students in labs. Students are learning to validate ideas and concepts to understand their hypothesis.

History:

Students are building concepts of relationship to better understand and interpret key behaviors similar to how they discuss and emphasize historical events with plausible causations and effects.

English/Speech:

Students are expected to relate concepts to build mathematical arguments to prove or disprove behaviors similar to how they would write persuasive essays or develop a thesis to prove or disprove their statements or those others.

Determine an explicit			
expression, a recursive			
process, or steps for			
calculations from a context			
F.BF.1.c			
(+) Compose functions.			
F.BF.2			
Write arithmetic and			
geometric sequences both			
recursively and with an			
explicit formula, use them			
to model situations, and			
translate between the two			
forms			
F.BF.3			
Identify the effect on the			
graph of replacing $f(x)$ = by			
f(x)+k, $k f(x)$, $f(kx)$, and $f(x)$			
+k) for specific values of k			
(both positive and negative			
values); find the value of k			
given the graphs.			
Experiment with the cases			
and illustrate an			
explanation of the effects			
on the graph using			
technology.			
F.BF.4			
Find inverse functions.			
F.BF.4.a			
Solve an equation of the			
form f(x)=c for a simple			
function f that has an			
inverse and write an			
expression for the inverse.			
F.BF.4.b			
(=) Verify by composition			
that one function is the			
inverse of another.			
F.BF.4.c			
(=) Read values of an			
inverse function from as			
graph or a table, given that			
the function has an inverse.			
F.BF.4.d			
(+) Produce an invertible function from a non			
invertible function by			
restricting the domain.			
F.TF.1			
Understand radian measure			
of an angle as the length of			
the arc on the unit circle			
subtended by the angle.			

F.TF.2			
Explain how the unit circle			
in the coordinate plane			
enables the extension of			
trigonometric function to all			
real numbers, interpreted			
as radian measures of			
angles traversed			
counterclockwise around			
the unit circle.			
F.TF.3			
(+) Use special triangles to			
determine geometrically the			
values of sine, cosine, and			
tangent for $\pi/3$, $\pi/4$ and			
$\pi/6$, and use the unit circle			
to express the values of			
sine, cosine, and tangent for			
x, π + x and 2π -x in terms of			
their values for x, where x is			
any real number.			
F.TF.4			
(+) Use the unit circle to			
explain symmetry (odd and			
even) and periodicity of			
trigonometric functions.			
F.TF.5			
Choose trigonometric			
functions to model periodic			
phenomena with specified			
amplitude, frequency, and			
midline.			
F.TF.6			
(+) Understand that			
restricting a trigonometric			
function to a domain on			
which it is always increasing			
or always decreasing allows			
it inverse to be constructed.			
F.TF.7			
(+) Use inverse functions to			
solve trigonometric			
equations that arise in			
modeling contexts; evaluate			
the solutions using			
technology, and interpret			
them in terms of the			
context.			
F.TF.8			
Prove the Pythagorean			
$sin^2\theta + cos^2 \theta = 1$			
identity and use it to			
calculate trigonometric			
ratios.			

G.SRT.7 Explain and use the relationship between the sine and cosine of complementary angles.			
S.ID.6 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related			

Abbott Lawrence Academy 2018-2019 Curriculum Map:Subject: Advanced Honors PrecalculusGrade: 11thUnit 2 "Complex Numbers and Trigonometry" (4) Weeks

Essential Questions	 How can you write a complex number using trigonometry? What are magnitude and argument of complex numbers and how do you find them? How can you test to see if an equation is an identity? How can you use identities to prove other identities? How do you calculate powers of complex numbers using De Moivre's Theorem? How do I calculate complex numbers? How can you connect roots of unit to regular polygons?
Learning Objectives for Unit	 Students will learn to (Visualization) use the complex plane to visualize the complex numbers and calculations with complex number geometrically. (Logical Reasoning) make connections to the complex number and calculations with trigonometric functions to generate and prove trigonometric identities. (Extension) work with the process of calculating roots of unity with polynomials.
Performance tasks: Formative and Summative	 SWBAT answer the following types of questions: How do you use geometry to calculate complex numbers? How can you use complex numbers to find formulas for cos 2x and sin 2x? For what value of cos x does cos 3x= 0? How do you use De Moivre's Theorem to write a rule for a trigonometric function? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to: Graph complex numbers in the complex plan to use geometry to explain arithmetic fact of complex numbers Represent complex numbers using both rectangular coordinates and polar coordinates Test trigonometric functions to predict identities and show the Multiplication Law for complex numbers Use Pythagorean identities and algebra to prove the trigonometric equations is an identity Calculate powers of complex numbers using De Moivre's Theorem The geometry of roots of unity and the connections to roots of equations in a certain form. Find exact algebraic expression for certain trigonometric values Students are responsible for a unit project that relies on using the learned skills to read through a mathematical proof and make it their own to understand the reasons behind the steps. Students will use develop a formula for determining roots of a general cubic. Students will be able to understand how complex numbers crop in their development

	Assessments: Tests, quizzes, homework, classwork, video project				
CC Standards/ Lawrence	Language Objectives	Academic	Content	Texts and	Cross-Content Connections
Standards		Language	Objectives	Supplemental	
				Learnings	
A.APR.4 Prove polynomial identities and use them to describe numerical relationship. A.REI.2 Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise. A.REI.4 Solve quadratic equations in one variable. A.REI.4.a Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(x-p)^2 = q$ that has the same solutions. Derived the quadratic formula from this form. A.REI.4.b Solve quadratic equations by inspection, taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as a+/- bi for real numbers a and b. A.SSE.1 Interpret expressions that represent a quantity in terms of its context. A.SSE.1.a Interpret complicated expressions, such as terms, factors, and coefficient. A.SSE.1.b Interpret complicated expressions by viewing one or more of their parts as a single entity. A.SSE.2 Use the structure of an expression to identify ways to rewrite it. F.TF.8 Prove the Pythagorean $sin^2\theta + cos^2 \theta = 1$ identity and use it to calculate trigonometric ratios. F.TF.9	Students will be able to: • explain how to determine the magnitude and argument of any complex numbers, orally and in writing • model complex numbers using both rectangular coordinates and polar coordinates and polar coordinates • choose and describe when its best to use either rectangular or polar coordinates to represent complex numbers • display the basic addition rules for cosine and sine using the Multiplication Law for complex numbers in writing • test and verify trigonometric equations to predict whether they are identities • model Pythagorean identities and algebra to prove that a trigonometric equation is an identity • explain how to calculate powers of complex numbers using De Moivre's Theorem, orally and in writing • compare and contrast the geometry of roots of unity • analyze the connection to roots of equations of the form x ⁿ -1=0 • calculate exact algebraic expression for certain trigonometric values • solve roots of unity	 argument, arg (x) polar coordinates complex numbers conjugate, <u>z</u> cyclotomy discriminant identically equal identity magnitude, z modulus norm, N(z) polar coordinates for complex numbers rectangular coordinates rectangular form for complex numbers roots of unity 	Learning Goals SWBAT: • Represent complex numbers using both rectangular coordinates and polar coordinates. • Determine the magnitude and argument of any complex number. • Decide when it is best to use wither rectangular or polar coordinates to represent complex numbers. • Test trigonometric equations to predict whether they are identities. • Show the basic addition rules for cosine and sine using the Multiplication Law for complex numbers. • Use Pythagorean identities and algebra to prove that trigonometric equations is and identity. • Calculate powers of complex numbers using De Moivre's Theorem. • Understand the geometry of roots of unity, and the connection to roots of equations of the form x ⁿ -1=0. • Find exact algebraic expressions for certain trigonometric values. Habits and Skills SWBAT: • Graph complex numbers in the complex plane.	CME Project: Precalculus Common Core- Chapter 2 (pages 82-163) https://www.pearsonsuc cessnet.com/ http://cmeproject.edc.or g/ Edmodo SMART Labs Khan Academy YouTube https://www.youtube.co m/watch?v=2lbABbfU6Zc Other: http://www.epcc.edu/Of ficeofStudentSuccess/tut orialservices/tutorialsupp ortservices/tutorialsupp ortservices/DP/Docume nts/Trigonometry%20Han douts%20(PDF)/Math%20 Handout%20(Trigonomet ry)%20Trig%20Formulas% 20Web%20Page.pdf	 All subjects: The students will consider the text/lecture an collaborative work to engage/learn with their notes. They will create interactive notebooks based off of readings, lectures, collaborative work, assignments, etc. Chemistry: Students will learn to better understand roots by comparing how important these roots are to the behavior of the function which will allow students to practice predicting and analyzing how things work with proof. Physics: Students will reinforce topics like waves in thi unit by thinking of the trigonometric function in terms of waves and polar coordinates looking a vector to analyze the argument and magnitudes. English: Students will learn to imprete expression by looking at the context similar to the skills learned English and Speech and Composition to analyze data in this particular case to see parts as a single entity by focusing on one aspect. History: Students will learn how prove identities to us the relationship to better analyze and review the information similar to the skills learned in PreAP and AP World History. Geometry: Students will start to represent trigonometric functions on the unit circle and to learn how these coordinates can be related on the Argand plane using complex numbers which are similar to the polar coordinates that students will learn about in this unit

(+) Prove the addition and subtraction	 • Use geometry to	
formulas for sine, cosine, and tangent and	explain arithmetic fact of	
use them to solve problems.	complex numbers	
C (DT 7	Multiply two complex	
G.SRT.7	numbers in the form	
Explain and use the relationship between	$r(\cos \Theta + i \sin \Theta)$.	
the sine and cosine of complementary	Manipulate	
angles.	trigonometric	
N.CN.1	expressions.	
Know there is a complex number I such	Determine useful test	
that $i^2 = -1$, and every complex number	cases and techniques to	
has the form a +bi with a and b real.	identify identities,	
N.CN.2	• Use basic rules to	
Use the relation show $i^2 = -1$ and the	generate more	
commutative, associative, and distributive	complicated rules.	
properties to add, subtract, and multiply	Calculate with complex	
complex numbers.	number.	
N.CN.3	Visualize complex	
(+) Find the conjugate of a complex	numbers and their	
number; use conjugates to find moduli	arithmetic.	
and quotients of complex numbers.		
N.CN.4		
(+) Represent complex number on the		
complex plane in rectangular and polar		
form, and explain why the rectangular		
and polar forms of a given complex		
number represent the same number.		
N.CN.5		
(+) Represent addition, subtraction,		
multiplication, and conjugation of		
complex numbers geometrically on the		
complex plane; use properties of this		
representation for computation.		
N.CN.7		
Solve quadratic equations with real		
coefficients that have complex solutions.		
N.CN.8		
(+) Extend polynomial identities to the		
complex numbers.		
N.CN.9		
(+) Know the Fundamental Theorem of		
Algebra; shoe that it is true for quadratic		
polynomials		

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 3 "Analysis of Functions" (5) Weeks

Essential Questions	 How can you graph a polynomial function given its factored form? How can you determine a polynomial's behavior at very large or very small inputs? How can you use long division to find equations of secant or tangent lines to the graph if a polynomial function? What are complex numbers? How can you use complex numbers to solve any quadratic equation? How do you represent a complex number graphically? What is the graphical effect of adding two complex numbers? How are the magnitude and argument of the product of two complex numbers related to the magnitude and argument of the original numbers?
Learning Objectives for Unit	 Students will learn to: (Reasoning by continuity) look at graphs of a function and chose two points on that graph to construct a secant line that will used to use the tangent and calculate slope. The slope of the constructed line is the limit of the slope of the secant line as the moving point approaches the fixed point. (Visualization) relate the graph of a function to the slope of its tangent at any point and use the information to analyze the graph. (Generalization) generalize the process and find an equation for the slope of the tangent to the graph of an exponential or logarithmic function without having a formal way to calculate the limit.
Performance tasks: Formative and Summative	 SWBAT answer the following types of questions: How can you graph a polynomial function given its factorial form? How can you determine a polynomial's behavior at a very large or very small inputs? How can you use long division to find equations of a secant or tangent lines to the graph of a polynomial function? What happens when interest is compounded more and more frequently? What are some reasons to introduce the number e? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to: Develop both formal and informal understanding of what continuity means by using key theorems to draw conclusions about the properties of the function given the degree Explore rational functions to find equations for the slope of the line tangent to a rational function graph at a point. Analyze the exponential and logarithmic functions to define the continuously compounded interest and limit definition. Find the slopes of the lines secant or tangent to the graph of a polynomial function Learn that these slope represent average and instantaneous rates of change of the function Graph functions that re quotients of polynomials Pay attention to the values of x for which the denominator polynomial has a value of 0 The constant e arises and different ways of computing it Find the natural log function and how to find the inverse of it Explain the effects of the discontinuities and the effects on graphs Graph rational functions using their horizontal and vertical asymptotes Students are responsible for a unit project that relies on using the learned skills to demonstrate the relationship how to use the partial fraction decomposition of a rational function to evaluate sum and to graph rational functions.
	Assessments: Tests, quizzes, homework, classwork, video project

CC Standards/ Lawrence	Language	Academic	Content Objectives	Texts and	Cross-Content
Standards	Objectives	Language		Supplemental	Connections
				Learnings	
A.APR.2	 state the Change of Sign 	 average rate of change 	Learning Goals	CME Project: Precalculus	All subjects:
Know and apply the Remainder	theorem and the	 continuous 	SWBAT:	Common Core-Chapter 3 (pages	The students will consider the
Theorem: For a polynomial p(x) and a	intermediate Value	 continuously compounded 	 state and use the limit definition 	164-273)	text/lecture and collaborative work
number a, the remainder on the division	Theorem for Polynomials	interest	of e and e ^x		to engage/learn with their notes.
by x-a is p(a), so p(a)=0 if and only if (x-	 analyze the graphs of 	 determinant 	 state and use the factorial 	https://www.pearsonsuccessn	They will create interactive
a) is a factor of p(x)	polynomial functions	• e	definition of e and e ^x	et.com/	notebooks based from readings,
A.APR.3	 find the equation of a line 	• hole	 use the inverse relationship 	http://cmeproject.edc.org/	lectures, collaborative work,
Identify zeros of polynomials when	secant to a polynomial	 infinite discontinuity 	between e ^x and ln x to solve		assignments, etc.
suitable factorization are available, and	functions and the average	 instantaneous speed 	problems	Edmodo	
use the zeros to construct a rough graph	rate of change of a function	 linear fractional 	 find an equation for the tangent 	SMART Labs	Physics:
of the function defined by the	between two points	transformation, R_A	to the graph of y=e ^x or y=ln x at a	Khan Academy	This particular chapter has the most
polynomial	 write the Taylor 	 natural logarithm, ln x 	point	You Tube	connection to Physics especially
A.APR.6	expansion for a polynomial	 power function 	 sketch the graph of a rational 		since students will think about the
Rewrite simple rational expression in	function about a point	 Removable discontinuity 	function, including asymptotes	Other:	relationship of factors and behaviors
different forms; write a(x)/b(x) in the	 find the equation of the 	 secant line 	and holes	http://www.epcc.edu/Officeof	of graph to calculate the rate of
form (q(x)+r(x))/b(x), where	tangent to a polynomial	 structure-preserving map 	 evaluate limits of rational 	StudentSuccess/tutorialservices	change over time but focusing
polynomials are with the degree of r(x)	curve at a point	 tangent line 	expressions	/tutorialsupportservicesMDP/D	informally on the
less than the degree of b(x) using	 sketch the graph of a 		• find the equation of the tangent	ocuments/Trigonometry%20Ha	
inspection, long division, or, for the	rational function including		to the graph of a rational function	ndouts%20(PDF)/Math%20Han	Biology:
more complicated examples, a	asymptotes and holes		at a point	dout%20(Trigonometry)%20Tri	Students start to build on the
computer algebra system	• evaluate limits of rational		• use matrices to write linear	g%20Formulas%20Web%20Pag	concept of the rate of change by
A.APR.7	expressions		fractional transformation of the	<u>e.pdf</u>	understand the concepts how the
Understand that rational expressions for	• find the equation of the		function $f(x) = 1/x$		rate of change is affected between
a system analogous to the rational	tangent to the graph of		• state the Change of Sign		two points the student are building
numbers, closed under addition,	rational function at a point		Theorem and the Intermediate		the relationship of the dependent
subtraction, multiplication, and division	• state and use the limit		Value Theorem for Polynomials		and independent variables.
by a nonzero rational expression; add,	and factorial definitions of e		and use the to analyze the graphs		
subtract, multiply, and divide rational	and e ^x		of polynomial functions		Algebra II:
expression.	• use the inverse		• find the equations of a line a		Students will learn how to graph
A.CED.2	relationship between e ^x and		secant to a polynomial function and the average rate of change of		functions na study the behavior of the functions to evaluate limits of
Create equations in two or more	In x to solve equationsfind the equation for the		a function between two points		rational expressions to look at
variables to represent relationships	line tangent to the graph of		 write the Taylor expansion for a 		asymptotes and roots.
between quantities; graph equations on	$y=e^x$ or $y=ln x$ at a point		Polynomial function bout a point		asymptotes and roots.
coordinate axes with labels and scales	y c or y mx ac a point		•find the equation of the tangent		Geometry:
			to a polynomial curve at a point		Students will think about how
A.REI.2					tangent functions work with
Solve simple rational and radical					connection to the rate of change
equations in one variable, and give			Habits and Skills		given two points on a function.
examples showing how extraneous			SWBAT:		Students are learning how the
solutions may arise			 develop a definition of 		behavior is limited by the two points
A.REI.11			continuously compounded		used to measure the rate of change.
Explain why the x-coordinates of the			interest		
points where the graphs of the equation			 visualize relationships between 		Trigonometry:
y=f(x) and y=g(x) intersect are the			the graphs of $f(x) = e^x$ and $g(x) = \ln x$		Students will view how concepts like
solutions of the equation f(x)=g(x) find			x and the slopes of the tangents		the tangent and secant line can be
the solutions approximately using			to these graphs		used to measure the rate of change
technology to graph the functions, make			 use functional equations to 		between two points to examine the
tables of values, or find successive			recognize the In function as a		relationship of the graph.
approximations. INclude cases where			logarithm		

f(t) and/or g(t) are linear, polynomials, rational, absolute value, exponential, and logarithmic functions. discontinuities, relating equations and their graphs erasion logarithmic functions. ASS.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression visualize different types of a rational function or visualize the graphs of a rational function or visualize the graphs of a polynomial function from its factored form or use the continuity of a polynomial function of a polynomial function or do a polynomial or conclusions about the function is factored form or about the stangent to the graph of a regioner graph of a regioner graph or do the function or the graph of a regioner graph or do the function or the graph of a regioner graph or do the graph of the function from a non invertible function from a non invertible function hore and busing the stangent or the graphs and the graphs and the stangent or the graphs and the stangent or the graph is and to equations of tangent lines in terrors of the quentity and
rational, absolute value, exponential, and logarithmic functions. A SEE 3 creasin logically to find limit at infinity of an expression to reveal and explain or find the equation of the tangent or be expression to the graph of a rational function properties of the quantity represented polynomial function from its factored form visualize of form identify the effect on the graph of replacing f(x) by f(x)+k, f(x), f(x), and f(rx+k) for specific values of k (both polynomial function to draw point and injustrate an explanation of the esplanation of the ergaph of a textmen values or and lilustrate an explanation of the esplanation of the effect on the graph big technology. F.BF.4 F.BF.4 long division to Taylor expansions find inverse functions F.BF.4 F.BF.4 replacing the uncert of rom a non invertible function from a solue graph of a relationship between two quantities, interpret key F.BF.4 fir a function that modes a relationship between two quantities, interpret key
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ASE:3 infinity infinity Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression • find the equation of the tangent to the graph of a rational function wits the continuity of a Polynomial function from its fractored form • usualize the graphs of a rational function from its fractored form replacing f(x) by f(x)+k, f(x), f(x), and • usualize the continuity of a polynomial function from its fractored form given the graphs. Experiment with cases and given the graph is graph using technology. • behavior fat extreme values or about the function's behavior fat extreme values or about the function and the function and the function of the graph is graph using technology. • on expension F.BF.4 Find Inverse function form a and to equations of tangent lines • of the function of tangent lines F.BF.4 Firs function from a anon invertible function from a non invertible function from a anon invertibl
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the quantities, and sketch graphs
the quantities, and sketch graphs
showing key features given a verbal
description of the relationship
F.IF.6
Calculate and interpret the average rate
of change of a function over a specified
interval. Estimate the rate of change
from a graph
F.F.7
Graph functions expressed symbolically
and show key feature of the graph, by
hand in simple cases and using
technology for more complicated cases
F.IF.7.c
Graph polynomial functions, identifying
zeros when suitable factorization are
available and showing end behavior
F.IF.7.d
Graph rational functions, identifying
zeros and asymptotes when suitable

F.IF.7.e			
Graph exponential and logarithmic			
functions, showing intercepts and end			
behavior and trigonometric functions			
showing period, midline, and amplitude			
F.IF.8 Write a function defined by an			
expression in different but equivalent			
forms to reveal and explain different			
properties of the function			
F.LE.1.c			
Compose functions			
N.RN.2			
Rewrite expressions involving radicals and rational exponents using the			
properties of exponents			
properties of exponents			
N.VM.6			
Use matrices to represent and			
manipulate data oi represent payoffs or			
incidence relationships in a network			

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 4 "Combinatorics" (4) Weeks

Essential Questions	 What does it mean for two problems to be isomorphic? How many ways can you pick object in order from a set of n elements? How many combinations can be n ways given a certain number of n values? What is the connection between the Pascal's Paths problem and the entries in Pascal's Triangle? Why is the sum of the entries in row n of Pascal's Triangle 2ⁿ?
Learning Objectives for Unit	 Students will learn to: solve a simpler problem by aligning strategies to the recursive thinking identify and create isomorphic problems counting functions by counting the number of functions from one finite set to another know when to use particular counting strategies
Performance tasks: Formative and Summative	 SWBAT answer the following types of questions: What is the coefficient x¹³y³⁷term in the expansion of the (x+y)⁵⁰? What is the difference between a combination and a permutation? What is a isomorphic function? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to:

		 Formal ways to approate Count permutations (or Count anagrams (ordetermination) The coefficients in the or The number or The number or Students are responsible for develop only the properties mathematical discoveries. 	ach counting problem, like what p ordered choices) and combinations red choices with repetitions) expansion of (a+b) ⁿ are r in the nth row of Pascal's triangl r of combinations when choosing r a unit project that relies on using	e from n elements g the learned skills to use special cases to think about how isomorphic functio	how to count them of the covered material to
CC Standards/ Lawrence	Language Objectives	Academic	Content Objectives	Texts and	Cross-Content
Standards		Language		Supplemental	Connections
				Learnings	
A.CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales A.APR.5 Know and apply the Binomial Theorem for the expansion of (x+y) ⁿ in powers of x and y for a positive integer n, where x and y are any numbers, with coefficients determined for example by Pascal's Triangle Prepares for S.CP.9	 develop strategies for systematic combinatorics interpret what combinatorics means can be used and explain what kinds of problems can be used for combinatorics develop and use formulas for the number of permutations of n objects taken at k times model the formula for combinations for the number of combinations at n things taken at k at a time find the number of anagrams for a given word apply the counting strategies to solve the Pascal's Path problems Explain why finding the coefficients of a binomial expansion of Pascal's Triangle Model and show the entries of Pascal's Triangle from a variety of prospective present combinatorial problems with formal strategies 	• anagram • combination • isomorphic • permutation • ${}_{p}C_{k}$, number of combinations of n objects. Taken at k at a time • ${}_{n}P_{k}$, number of permutations of n objects, taken k at a time	Learning Goals SWBAT: • Apply counting strategies to solve the Pascal's Paths problem. • Explain why the coefficients of a binomial expansion are found in Pascal's Triangle. • See the entities of Pascal's Triangle from a variety of perspectives • Develop and use formulas for finding the number of permutation of n objects, taken k at a time • Find a formula for the number of combinations of n objects, taken k at a time • Find the number of anagrams for a word • Recognize the kids of problems that can solve using combinations • Develop your own strategies for systematic counting Habits and Skills SWBAT: • Use combinations to find binomial coefficients. • Use combinatorics to probe the Binomial Theorem. • Recognize isomorphic problems.	CME Project: Precalculus Common Core-Chapter 4 (pages 274-339) https://www.pearsonsuccessnet.c om/ http://cmeproject.edc.org/ Edmodo SMART Labs Khan Academy Youtube	All subjects: The students will consider the text/lecture and collaborative work to engage/learn with their notes. They will create interactive notebooks based off of readings, lectures, collaborative work, assignments, etc. Geometry/Trigonometry: Students will build the concept on patterns to better understand the Binomial Theorem as they analyze two or more variables which will represent the quantities between two relationship modeled on the coordinate axes with labels. Chemistry/Biology/Physics: Students will build equations in two or more variables to represent the relationship of the quantities using graphs and equation to find trend lines and behaviors similar to what students on chemistry/ biology/physics labs using excel.

	 Count the number of elements in a subset by counting the complement of the desired subset Use appropriate counting tools and formulas Relate different counting strategies to each other Use efficient strategies for counting Identify isomorphic problems apply counting strategies to functions defined on finite sets
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Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 5 "Functions and Tables" (5) Weeks

Essential Questions	 What is the Fundamental Law of Exponents? What are some of its corollaries? How do you extend the laws of exponents to define zero, negative, and rational exponents? For f(x) = b^x, why is it true that f(m) • f(n) = f(m+n)? Why must an exponential function have an inverse function? What are some reason to use logarithms? What is a logarithmic scale and when do you use it?
Learning Objectives for Unit	 Students will learn to (extension) by making strategic choices that preserve the laws of exponents to extend the set of numbers that can be used as exponents to include all real numbers (visualization) use the graphs of exponential and logarithmic functions to conjecture critical properties of these functions (logical reasoning) to solve problems by reasoning about exponential and logarithmic functions using the laws of exponents and the laws of logarithms
Performance tasks: Formative and Summative	 SWBAT answer the following types of questions: What are the simplified forms of the expressions 4°, 7°, and 5^{27/3}? If you invest \$1000 in an account at 6% interest, compounded annually, how much will you have after 30 years? If you invest \$1000 in an account at 6% interest, compounded annually, how many years will it take until your money grows to \$10000? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to: Develop the laws of exponents by extending from positive integers to include zero, negative, and rational numbers Use sequences to explore exponents Graph exponential functions and write rules for exponential functions given a table of inputs and outputs or two points on the graph of the function Evaluate logarithms of any base, to use logarithms in solving exponential equations and to graph logarithmic functions

		Students are responsible for a unit project that relies on using the learned skills to explore the functional equation that exponential functi satisfy: f(x + y) = f(x) • f(y)to build an understanding of how any function that satisfies this equation must behave. Assessments: Tests, quizzes, homework, classwork				
CC Standards/	Language Objectives	Academic	Content Objectives	Texts and Supplemental	Cross-Content	
Lawrence		Language		Learnings	Connections	
Standards				Ŭ		
A.REI.4 Solve quadratic equations in one variable A.REI.4.b Solve quadratic equations by inspection taking square roots, completing the square, the quadratic formula, and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write the as a+/- bi for real numbers a and b A.REI.6 Solve systems of linear equations exactly and approximately focusing on pairs of linear equations in two variables A.SSE.2 Use the structure of an expression to identify was to rewrite it A.SSE.3 Choose and produce an equivalent form of an expression A.SSE.3.a Factor a quadratic expression to reveal the zeros of the function it defines A.SSE.4 Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems F.BF.1.a	 evaluate expressions involving exponents, including zeros, negative, and rational exponents summarize how to find missing terms in a geometric sequence and generate geometric sequences to interpret expressions involving rational exponents model how to convert between exponential and radical forms for rational exponents discuss how to extend the laws of exponents to allow the evaluation of zero, negative, and rational exponents. reason logically and state how to verify that a particular interpretation of an exponent flows the laws of exponents. generalize from specific examples to develop and verify identities evaluate logarithm of any base using a calculator model the use logarithms to solve for exponential equations graph logarithmic functions discuss how to reason logically from the definition of a logarithmis to develop the laws of logarithms visualize and model the graph of a logarithmic function from the graph of the corresponding exponential function explain how to convert flexibly and strategically between logarithmic form and exponential form, and choose the best from to solve problems 	 arithmetic sequence bⁿ base change-of-base rule closed-form definition common logarithm, log x exponential function exponential growth extension by continuity functional equation geometric sequence inverse function laws of exponents laws of logarithms linear scale log-log graph paper logarithmic scale monotonic negative exponent one-to-one product model rational exponent recursive definition semilog graph paper strictly decreasing unit fraction exponent zero exponent 	Learning Goals SWBAT: • Review the laws of exponents • Evaluate expressions involving exponents, including zero, negative, and rational exponents • Find missing terms in a geometric sequence and generate sequences to interpret expressions involving rational exponents • Convert between exponential and radical forms for rational exponents • Graph an exponential function to determine the equation of an exponential function given two points on its graph • Identify an exponential function from the table it generates and use the table to create a closed-form or recursive definition of the function • Extend the laws of exponents and express the laws as function equations • Evaluate the inverse of the function y=b* either exactly or by approximation • Evaluate logarithms of any base using a calculator • Use logarithms to solve exponential equations • Graph functions using a logarithmic scale Habits and Skills SWBAT: • Reason logically to verify that a particular interpretation of an exponent follows the laws of exponents	CME Project: Precalculus Common Core-Chapter 5 (pages 340-437) https://www.pearsonsuccessnet.co m/ http://cmeproject.edc.org/ Edmodo SMART Labs Khan Academy YouTube	All subjects: The students will consider the text/lecture and collaborative work to engage/learn with their notes. They will create interactive notebooks based off of readings, lectures, collaborative work, assignments, etc. Physics: Students will learn to evaluate functions to reason laws of logarithmic functions and exponents. Biology: Logarithmic functions are used to better understand the decay and growth function in terms of cells or species. Algebra II: Students will use the basic knowledge learned about logarithmic function to build concepts. Trigonometry: Students will expand the knowledge of logarithmic functions by building the concept of exponents and how build geometric series and functions.	

Determine en evelieit	Г	• Companyaliza forma en esifie en esta	
Determine an explicit		• Generalize form specific examples	
expression, a recursive		to develop and verify identities	
process, or steps for		• Reason by continuity to extend the	
calculations from a context		definition of exponent to include all	
F.BF.2		real numbers	
Write arithmetic and		 Visualize exponential growth by 	
geometric sequences both		examining graphs and tables of	
recursively and with an		exponential functions	
explicit formula, use them to		 Draw logical conclusions from the 	
model situations, and		laws of exponents and properties of	
translate between the two		exponential functions to solve	
forms		problems and probe conjectures	
		 Reason logically from the definition 	
F.IF.3		of a logarithmic function and from the	
Recognize that sequences are		laws of exponents to develop the laws	
functions sometimes defined		of logarithms	
recursively, whose domain is		 Visualize the graph of a logarithmic 	
a subset of the integers		function from the graph of the	
F.IF.4		corresponding exponential function	
For a function that models a		 Convert flexibility and strategically 	
relationship between two		between logarithmic form and	
quantities, interpret key		exponential form, and choose the	
features of graphs and tables		best form to solve problems	
in terms of the quantities,			
and sketch graphs showing			
key features given a verbal			
description of the			
relationship.			
F.IF.8			
Write a function defined by			
an expression in different but			
equivalent forms to reveal			
and explain different			
properties of the function			

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 6 "Analytic Geometry" (4) Weeks

Essential Questions	 What are the basic graphs and their equations (parent functions)? What are the effects on both the graphs and their equations when the graphs are translated, stretched, shrunk, or reflected? Why do dilations commute under function composition? How do you compute the inverse of an affine translation? How do you use the computed inverse of affine transformation to graph the original equation? How do describe the effect of an affine transformation on an axis and the effect of changes in the axes on the graph of the equation? How you identify the fixed points of an affine transformation and the set of affine transformations that fix a particular point?
Learning Objectives for Unit	Students will learn to

Performance tasks: For	rmative and Summative	compositions of these • (making connections equation • (logical reasoning) a translations—to devel SWBAT answer the fo • How are the gravely • What does the gravely • How do you transcored gravely • How do you use • How do you use • What is the fixed • Students will have to • Relate the effect • Write any compo- affine transform • Transform an eq appoint on an affine transform • Students are responsis resembles abstract algorithm	transformations s) experiment with changes to an equal sk questions about the algebraic struc lop conjectures to answer those quest llowing types of questions: phs of $y = x^2$ and $y = (x - 3)^2$ related? graph of $(x + 1)^2 + (y - 3)^2 = 36$ look like graph of $-2y = x^3 - x$ look like? isform an equation of the form $y = ax$ ions and translations? the replacing-the-axes method to ske the replacing-the-axes method to exp d point for $A_{(5,3)}$? complete Mathematical Reflections for ts on a basic graph and on the equation osition of translations and dilations as lation juation into one the basic graphs, desi- fine transformation ble for a unit project that relies on us gebra. Students will receive practice v	³ + bx ² + cx + d into one of the equations y	the graph to the type of change in the as —translations, dilations, and affine r conjectures = x^3 , $y = x^3 + x$, or $y = x^3 - x$ by of $y = x^2$ and $y = (x - 3)^2$? dents think and write about how to: or a reflection of the graph erse of a dilation, a translation, or an n on an axis, and identify the fixed rties that define a group through it
CC Standards/ Lawrence Standards	Language Objectives	Academic Language	Content Objectives	Texts and Supplemental Learnings	Cross-Content Connections
A.REI.2	 sketch basic graphs 	• affine recursive	Learning Goals	CME Project: Precalculus Common	All subjects:
Solve simple rational and radical equations in one variable, and	 describe the effect of translation of one of the basics graphs on both the graph and the gruption of the 	function affine 	SWBAT: • Sketch basic graphs	Core-Chapter 6 (pages 438-535)	The students will consider the text/lecture and collaborative work to

CC Standards/	Language Objectives	Academic	Content Objectives	Texts and Supplemental	Cross-Content
Lawrence Standards		Language		Learnings	Connections
A.REI.2	 sketch basic graphs 	 affine recursive 	Learning Goals	CME Project: Precalculus Common	All subjects:
Solve simple rational and radical	 describe the effect of translation 	function	SWBAT:	Core-Chapter 6 (pages 438-535)	The students will consider the
equations in one variable, and	of one of the basics graphs on both	• affine	 Sketch basic graphs 		text/lecture and collaborative work to
give examples showing how	the graph and the equation of the	transformation	 Describe the effect of a 	https://www.pearsonsuccessnet.co	engage/learn with their notes. They
extraneous solutions may arise	graph	 completing the 	translation of one of the basic	<u>m/</u>	will create interactive notebooks
A.REI.4	 describe and model the effect of 	square	graphs on both the graph and the	http://cmeproject.edc.org/	based off of readings, lectures,
Solve quadratic equations in one	scaling an axis or reflection on both	 dilation 	equation of the graph		collaborative work, assignments, etc.
variable	the graph and the equation of the	 even function 	 Describe the effect of scaling an 		
A.REI.10	graph	 fixed point 	axis or reflections of one of the	Edmodo	Physics:
Understand that the graph of an	 compose transformations and 	 identity 	basic graphs on both the graph	SMART Labs	Students will learn the importance of
equation in two variables is the	sketch/model the effect of such a	transformation	and the equation of the graph	Khan Academy	scaling this is a transferable skill to
set of all of solutions plotted in	composition	 intercept 	 Compose transformation and 	YouTube	zoom in and out of aspect of
the coordinate plane, often	 visualize and explain variations of 	 iterations 	sketch the effect of such a		functions or concepts. Students will
forming a curve (which could be a	the basic graphs under translations,	 odd function 	composition on one of the basic	Glencoe Common Core Precalculus	learn how see one aspect in a bigger
straight line).	reflections, scaling, and	 reflection 	graphs		or smaller picture depending on the
A.REI.11	compositions of those	transformation	 Write any composition of 		analyses of the concept.
Explain why the x-coordinates of	transformations	 replacing-the-axes 	translations and dilations as an		
the points where the graphs of	 explore and identify 	method	affine transformation and write		Biology:
the equations y=f(x) and y=g(x)	transformations to a graph to a	 socks and shoes 	any affine transformation as a		Students will learn how to predict
intersect are the solutions of the	corresponding transformation of its	method	composition of a dilation and a		transformations and behaviors of
equation f(x)=g(x) find the	equation	 stabilizer 	translation		function based on what they have

				· · · · · · · · · · · · · · · · · · ·
solutions approximately using	 analyze the operation of function 	 translation 	• Find the inverse of a dilation, a	observed to analyzing how inverses
technology to graph the	compositions on transformations	 unit circle 	translation, or an affine	work. This is important to biology in
functions, make tables of values,	 write any composition of 		transformation and use that	the way that students view concepts
or find successive	translations and dilations as an		inverse as a tool to solve	like genetic mutation or inheritance.
approximations. Include cases	affine transformation and write any		equations	
where f(x) and/org(x) are linear,	affine transformation as a		 Find transformations for 	Algebra II:
polynomial, rational, absolute	composition of a dilation and a		converting a general quadratic or	Students will learn to think about the
value, exponential, and	translation		cubic into one of the basic graph	quadratic function and how the roots
logarithmic functions	 explain how to find the inverse of 		forms	relate to functions depending on if
	a dilation, a translation, or an affine		 Use the techniques learned to 	the function is even or odd.
A.SSE.3	transformation and use that inverse		transform an equation into one	
Choose and produce an	as a tool to solve equations		of the basic graph forms and use	Geometry:
equivalent form of an expression	 model and describe how to find 		the information to graph the	Students will start to think of how to
to reveal and explain properties	transformations for converting a		original equation	use functions and their behaviors to
of the quantity represented by an	general quadratic or cubic into one		• Describe the effect of an affine	relate to values like roots and
expression	of the basic graph forms		transformation on an axis and the	exponential functions that alight to
A.SSE.3.a	 generalize from a series of 		effect of changes in axes on the	said roots.
Factor a quadratic expression to	numerical calculations to produce a		graph of an equation	
reveal the zeros of the function it	proof for a property of		 Identify the fixed points of an 	Trigonometry:
defines	transformations		affine transformation and the set	Students will start to think about odd
A.SSE.3.b	 summarize how to extend the idea 		of affine transformations that fix	and even function to think about how
Complete the square in a	of finding an inverse of a function by		a particular point	functions have roots that are
quadratic expression to reveal	undoing its steps in reverse order to			solutions and how the solutions
the maximum or minimum value	find the inverse of an affine			affect the behavior of the functions.
of the function it defines	transformation			anect the behavior of the functions.
of the function it defines	 create connections between 		Habits and Skills	
F.BF.3			SWBAT:	
	algebraic calculations, such as using		Visualize variations of the basic	
Identify the effect on the graph of	substitutions to make an equation			
replacing $f(x)$ = by $f(x)+k$, $k f(x)$,	monic or to complete the square and the affine transformations of		graphs under translations,	
f(kx), and $f(x + k)$ for specific			reflections, scaling, and	
values of k (both positive and	translations and dilation		compositions of these	
negative values); find the value of	 describe the effect of an affine 		transformations	
<i>k</i> given the graphs. Experiment	transformation on an axis and the		Match a transformation of a	
with the cases and illustrate an	effect of changes in axes on the		graph to a corresponding	
explanation of the effects on the	graph of an equation		transformation of its equation	
graph using technology	• identify the fixed points of an		• Analyze the operation of	
	affine transformation and the set of		function composition on	
F.IF.4	affine transformations that fix a		transformations	
For a function that models a	particular point		• Generalize from a series of	
relationship between two	 model transformations both as 		numerical calculations to produce	
quantities, interpret key features	operations on graphs and as		a proof for a property of	
of graphs and tables in terms of	operations on coordinate axes		transformations	
the quantities, and sketch graphs	 discuss how to think algebraically 		• Extend the idea of finding an	
showing key features given a	to further examine the structure of		inverse of a function by undoing	
verbal description of the	the set of affine transformations		its steps in reverse order to find	
relationship.	 summarize how to make 		the inverse of an affine	
	connections between		transformation	
G.GMD.4	transformations on graphs and on		 Find connections between 	
Identify the shapes of two-	coordinate axes		algebraic calculations, such as	
dimensional cross sections of			using substitutions to make an	
three-dimensional objects, and			equation monic or to complete	
identify three-dimensional			the square, and the affine	
objects generated by rotations of			transformation of translation and	
two-dimensional objects			dilation	

			1
G.GPE.1		 Visualize transformations both 	
Derive the equation of a circle of		as operations on graphs and as	
given center and radius using the		operations on coordinate axes	
Pythagorean Theorem; complete		 Make connections between 	
the square to find the center and		transformations on graphs and	
radius of a circle given by an		on coordinate axes	
equation		Think algebraically to further	
G.GPE.2		examine the structure of the set	
Derive the equation of a parabola		of affine transformations	
given a focus and directrix			
G.GPE.3			
Derive the equation of ellipses			
and hyperbolas given foci and			
directives			
G.GPE.4			
Use coordinates to prove simple			
geometric theorems algebraically			
G.GPE.6			
Find the point on a directed line			
segment between two given			
points that partitions the			
segment in a given ratio			
N.Q.2			
Define appropriate quantities for			
the purpose of descriptive			
modeling			
N.VM.1			
Recognize vector quantities as			
having both magnitude and			
direction. Represent vector			
quantities by directed line			
segments, and use appropriate			
symbols for vectors and their			
magnitudes			
N.VM.2			
Find the components of a vector			
by subtracting the coordinates of			
an initial point from the			
coordinates of a terminal point			
N.VM.3			
Solve problems involving velocity			
and other quantities that can be			
represented by vectors			
N.VM.4			
Add and subtract vectors			
N.VM.4.a			
Add vectors end to end			
components-wise and by the			
parallelogram rule. Understand			
that the magnitude of a sum of			
two vectors is typically not the			
sum of the magnitude			
N.VM.4.c			
			•

Understand vector subtraction v- was v 4(w), where v- wis the additive inverse of w, with the same magnitude as w and point in the opposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise N.VM.5 Multiply a vector by a scalar N.VM.5a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = [1 v] Compute the direction of cv knowing that when [C] cannot equal 0. the direction of cv is either along v or against v.
additive inverse of w, with the same magnitude as w and point in the apposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise N.VM.5 Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along vor
same magnitude as w and point in the opposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise N.VM.5 NUML5 Vy a vector by a scalar N.VM.5 .a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication vusing cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along vor
in the opposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise N.VM.5 Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication c using cv = c v Compute the direction of cv k solving that when C cannot equal 0. the
Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise N.VM.5.5 Multiply a vector by a scalar N.VM.5.a represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication componet-wise N.VM.5.5 Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannet equal 0. the direction of cv is either along v or
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in the appropriate order, and perform vector subtraction component-wise N.VM.5 Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
perform vector subtraction component-wise N.VM.5 Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of v is either along v or
component-wise N.VM.5 N.VM.5.a Hultiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b N.VM.5.b Compute the magnitude of a scalar multiplication cv using I = 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1
N.VM.5. Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of v is either along v or
Multiply a vector by a scalar N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
N.VM.5.a Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cr using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
possibly reversing their direction; perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
perform scalar multiplication component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
component-wise N.VM.5.b Compute the magnitude of a scalar multiplication cv using $ cv = c v $ Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
N.VM.5.b Compute the magnitude of a scalar multiplication cv using $ cv = c v $ Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
Compute the magnitude of a scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
scalar multiplication cv using cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
cv = c v Compute the direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
direction of cv knowing that when C cannot equal 0. the direction of cv is either along v or
when C cannot equal 0. the direction of cv is either along v or
direction of cv is either along v or
against v.

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 7 "Probability and Statistics" (5) Weeks

 How you notice and explain patterns in Pascal's Triangle? How do you use the Binomial Theorem for expanding expression of the form (a + b)ⁿ?
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Learning Objectives for Unit Performance tasks: Formative and Summative		Students will learn to • (visualize sums) use pictures of arrays of squares and dots to make sense of the closed forms for various sums • (reason about linearity) verify that the Σ operation meet the functional equation requirements of linearity— Σ (f+g)= Σ f+ Σ g and Σ (kf)=k(Σ f) • (passing to the limit) develop intuition about the process of finding a limit of a function as one variable get arbitrarily large through experiment and reasoning SWBAT answer the following types of questions: • Describe Gauss's method for summing all integers from 1 to n. • Find a formula for $\Sigma_{j=0}^{n}$ 2^{j} in terms of <i>n</i> .				
		 What is a closed form What is an arithmetic What is a geometric so How do you write the What is the sum of the What is the expanded What is the expanded What is the coefficien Students will have to comp Make a sum table for Use Gauss's method the constant ratios Find closed-form definit closed-form for a Generate Pascal's Triation 	le for the series associated with $f(n) = 3n + 6$ having initial t for the following recursive rule? $f(n) \{5, if n = 0 \ f(n-1) + 2n^2 + 3n\}$ sequence? equence? repeating decimal 0.121212121212 as a fraction? e entries in row 10 of Pascal's Triangle? I form of $(2d + 7)^8$? t of $x^7 y^3$ in the expansion of $(x + y)^{10}$? lete Mathematical Reflections for the various investigation a function, write closed-form rules for the sum column, and o find the sum of a sequence with constant differences and initions for indefinite sums and to use the definitions to eval on for the series associated with a function withmetic and geometric sequences and their associated set ingle, to find and explain patterns in Pascal's Triangle, and or a unit project that relies on using the learned skills to use ine of best fit for a data set.	x + 2, if $n > 0is that have students thinkd use \Sigma notationl Euclid's method to find theluate definite sums, develeriesto use the Binomial Theore$	ne sum of a sequence with op and use∑identities, and find em to expand expressions	
CC Standards/	Language	Academic	Content Objectives	Texts and	Cross-Content	
Lawrence Standards	Objectives	Language		Supplemental	Connections	
				Learnings		
 A.APR.5 (+) Know and apply the Binomial Theorem for the expansion of (x+y)ⁿ in powers of x and y for a positive integer n, where x and y are any numbers, with coefficients determined for example by Pascal's Triangle F.BF.1.a Determine an explicit expression, a 	 reason logically to understand how both Gauss's method and Euclid's methods work and choose which method to used for finding a sum and explain why, both verbally and in writing visualize and model a sum geometrically to make sense of an algebraic pattern generalize and explain a 	 arithmetic sequence arithmetic series associated series Bernoulli's formulas Binomial Theorem common difference common ratio constant differences definite sum Euclid's method figurate numbers 	Learning Goals SWBAT: • Make a sum table for a function and write a closed- form rule for the sum column where appropriate • Use Gauss's method to find the sum of a sequence with a constant difference between successive terms • Use Euclid's method to find the sum of a sequence with a constant ration between success terms • Expand ∑ notation or convert an expanded sum back to ∑ notation • Find closed-form expression for indefinite sums and	CME Project: Precalculus Common Core-Chapter 7 (pages 536-663) <u>https://www.pearson successnet.com/ http://cmeproject.edc</u> .org/	All subjects: The students will consider the text/lecture and collaborative work to engage/learn with their notes. They will create interactive notebooks based off of readings, lectures, collaborative work, assignments, etc. Physics:	
recursive process, or steps for calculations from a context	result from a series of numerical examples	Gauss's method geometric sequence geometric series	 sued them to evaluate definite sums Find closed-form expression for the series associated with a function 	Edmodo SMART Labs Khan Academy	This uit considers the probabilit and accuracy of data introducing concepts of how	

with a function

Khan Academy

YouTube

introducing concepts of how

geometric series

identity

N.Q.1

Use units as a way to understand	 develop a list of ∑ identities 	• indefinite sum	• Find a closed-form representation for an arithmetic		data is used in a distribution
problems, and to guide the solution	and recognize situation in	• index	sequence and its associated series	Glencoe Common	curve
of multi-step problems; choose and	which to apply them	● limit	• Find a closed-form representation for a geometric	Core Precalculus	
interpret units consistently in	 find and model closed-form 	 Pascal's Triangle 	sequence and its associated series		Biology:
formulas; choose and interpret the	expression for the series	 repeating decimal 	• Convert a repeating decimal into an exact fraction		Students will think about the
scale and the origin in graphs and	associated with a function	 series associated with f 	• Use the Binomial Theorem for expanding expressions		concepts of sampling and how
data display	• generalize the steps in	• term	of the form (a+b) ⁿ		samples can be used to study
N.Q.3	calculating definite sums to	• sigma			the chance of something
Choose a level of accuracy	find a closed form for the	 summation 	Habits and Skills		happening or the likelihood of
appropriate to limitations on	indefinite sum	• summation	SWBAT:		something like a virus can affect
			-		°.
measurement when reporting	 reason logically using a recursive definition of a 		Reason logically to understand how both Gauss's method and Evaluate and exactly and shapes which		a population
quantities			method and Euclid's method work, and choose which		
	function to develop a closed-		method to use for finding a particular sum		Algebra II:
S.CP.1	form definition		• Visualize a sum geometrically to make sense of an		Students will apply the concepts
Describe events as subsets of a	 distinguishes between a 		algebraic pattern		of probability to think about
sample space using characteristics	geometric and a arithmetic		 Generalize a result from a series of numerical 		the independence of trails and
of the outcomes, or as unions,	sequence and find its closed-		examples		how likely the event is to
intersections, or complements of	form		 Visualize a complicated sum as a combination of 		happen given certain situations
other events	 determine whether a 		different simpler sums		
S.CP.2	geometric sequence has a		 Generalize the steps in calculating definite sums to 		Geometry:
Understand that two events A and B	limit, and if it does, how to find		find a closed form for an indefinite sum		Students will make sense of
are independent if the probability of	the limit		 Visualize arithmetic and geometric series to better 		geometric patterns that will
A and B occurring together is the	 reason logically to 		understand their behavior		apply to make algebraic ones so
product of their probabilities and	understand, write, and analyze		 Think about extreme cases as values of n become 		that students can model
use this characterization to	proofs		very large or terms of a sequence become very small		summations and build an
determine if they are independent	 generate Pascal's Triangle 				understanding about value
S.CP.3	and evaluate the nth row, kth				C C
Understand that conditional	column entry as $\binom{n}{-}$				Trigonometry:
probability of A given B as P(A and	• notice and explain patterns				Students will think logically
B)/P(B), and interpret independence	• notice and explain patterns in Pascal's Triangle				about the probability and
of A and B as saying that the	 seek invariants or regularity 				statistics as they see the
conditional probability of A given B	in calculation to develop a				possibility of an outcome using
is the same as the probability of A,	conjecture				concepts learned to draw
and the conditional probability of B					conclusions
given A is the same as the	 reason logically to prove 				
probability of B	conjectures				Chemistry:
S.CP.4	•				Students will learn about
Construct and interpret two-way					sample size and how data is
frequency tables of data when two					relevant. Students will learn
categories are associated with each					about the normal distribution
object being classified. Use the two-					curve and what the
way table as a sample space to					expectations and variations
decide if events are independent					might be.
and to approximate conditional					
probabilities					History:
S.CP.5					Students will learn how to read
Recognize and explain the concepts					information as factual and how
of conditional probability and					the data can be interpreted to
independence on everyday language					see the validity given the
and everyday situations					population/sample size.
S.CP.6					
Find the conditional probability of A					English/Speech:
given B as the fraction of B's					Students will learn how to
outcomes that also belong to A, and					validate the information given
					the sample size and the spread
	1	L	1	1	

interpret the answers in terms of				of the confidence interval by
the model				applying validity to the
S.CP.7				information given and
Apply the Additional Rule P(a or B)=				understanding how probability
P(A)+P(B)-P(A or B), and interpret				works give the distribution
the answers in terms of the model				works give the distribution
S.CP.8				
Apply the general Multiplication				
Rule in a uniform probability model,				
P(A and B)=P(A) P(A B)=P(B)P(A B),				
and interpret the answer in terms of				
the model				
S.CP.9				
Use permutations and combinations				
to compute probabilities of				
compound events and solve				
problems				
prosicilis				
5163				
S.IC.2				
Decide if a specified model is				
consistent with results from a given				
data-generating process using				
simulation				
S.IC.4				
Use data from a sample survey to				
estimate a population mean or				
proportion; develop a margin of				
error through the use of simulation				
models for random sampling				
S.IC.5				
Use data from a randomized				
experiment to compare two				
treatments; use simulations to				
decide if differences between				
parameters are significant				
S.IC.6				
Evaluate reports based on data				
S.ID.1				
Represent data with plots on the				
real number line				
S.ID.3				
Interpret differences in shape,				
center, and spread in the context of				
the data sets, accounting for				
possible effects of extreme data				
points (outliers)				
S.MD.1				
Define a random variable for a				
quantity of interest by assigning a				
numerical value to each event in a				
sample space; graph the				
corresponding probability				
distribution using the same				
o the stante	1	1		

distributions SMD2 Calculate the expected value of a random variable; interpret it as the mean of the probability distribution For a random variable defined for a sample space in which theoretical probabilities are assigned empirically; find the expected value SMD.4 Develop a probability distribution for a random variable defined for a sample space in which theoretical a random variable defined for a sample space in which theoretical a sample space in which theoretical a sample space in which theoretical sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a sample space in which probabilities a random variable defined for a sample space in which probabilities a random variable defined for a sample space in which probabilities a sample space in which probabilities a random variable defined for a sample space in which probabilities a cates in the space in which probabilities a decision y sample space in which probabilities a decision y s		1		1
SMD2 Control Contro Control Control	graphical displays as for data			
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using probability concepts	Analyze decisions and strategies			
	using probability concepts			

Abbott Lawrence Academy 2018-2019 Curriculum Map: Subject: Advanced Honors Precalculus Grade: 11th Unit 8 "Ideas of Calculus" (6) Weeks

Essential Questions	 How you find the area under an irregular shape? What is the area under a curve? How do can I find said area exactly? What is Fermat's approach to finding the area under the graph given two points? How can areas under a curve be used to gram new perspectives on familiar functions? How is area related to logarithmic functions?
Learning Objectives for Unit	 Students will learn to (approximation) apply given information to approximate values leading that approximations can lead to exact values.

Performance tasks: Formative and Summative		 (passing to the limit) view the limit of a sequence by getting as close to the value as possible. (reasoning continuity) learn about the area of the curve and how it is reasonable to suppose that the function is continuous and small changes will also produce changes in the area of said curve SWBAT answer the following types of questions: How can you find the area of an irregularly-shaped figure? How can you estimate the area under a curve? What is the area under a curve given a boundary? Students will have to complete Mathematical Reflections for the various investigations that have students think and write about how to: approximate the areas of irregular shapes and regions under curves by using squares and rectangles use Cavalieri extended Archimedes's result to find the area under the graph for integers follow the historical approach taken by two mathematicians to find the area under certain curves Students are responsible for a unit project that relies on using the learned skills to use the sequence of polynomials called the Chebyshev polynomials to produce multiple angle formulas for cosine Assessments: Tests, quizzes, homework, classwork			
CC Standards/	Language Objectives	Academic	Content Objectives	Texts and Supplemental	Cross-Content
Lawrence Standards		Language		Learnings	Connections
 A.CED.3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context A.SSE.4 Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems F.BF.5 Understand the inverse relationship between exponents and logarithms and use this relationship to solve problems and exponents 	 write a program to compute upper and lower area approximations find a closed form expression for an area approximation model a recursive function definition use the Archimedes' method to approximate an area Use Fermat's method to approximate an area define the area under the graph and measure the area define Cavalieri's method of dividing intervals into rectangles to derive the formula for the sums of power explain how to use rectangles to estimate the areas of irregular shapes 	 Fermat lower sum Fermat upper sum lower sum upper sum 	Learning Goals SWBAT: • Estimate the areas of irregularly-shaped objects • Estimate the area under the graph of y=x ² between x=0 and x=1 • Calculate the area under the graph of y=x ² between x=0 and x=1 exactly • Find the area under the graph of y=x ³ between x=0 and x-1 • Calculate the area under the graph of y=x ^m between x=0 and x=1 for any positive integer m • Develop formulas for calculating S[1,a](x ^m) where m is any integer • investigate a mysteriously familiar function L(a) • Find the area under the graph of y=e ^x between x=0 and x=1 Habits and Skills SWBAT: • Use rectangles to estimate the area of irregular shapes • Use approximations to find areas to any desired level of accuracy • Use the formula for the sum of squares to find areas	CME Project: Precalculus Common Core-Chapter 8(pages 664-737) https://www.pearsonsuccessnet.com / http://cmeproject.edc.org/ Edmodo SMART Labs Khan Academy YouTube Glencoe Common Core Precalculus	All subjects: The students will consider the text/lecture and collaborative work to engage/learn with their notes. They will create interactive notebooks based off of readings, lectures, collaborative work, assignments, etc. Physics: Finding the area under the curve can reveal key concepts like the velocity an object is traveling Biology: The area under the curve can be used to find concepts of how much water is in a pool for a tad pool or if students need to find the volume of a liquid when there is a certain shape Algebra II: Students will use the concepts learned in Algebra II to extend the concept of functions

	 Use the closed forms for summations find areas Use a historical perspective to make sense of the most important ideas of calculus Use a CAS to make short work of complicated calculations Use properties of a mystery function identify the function Use areas under the curves to gain ne perspectives on familiar functions 	to Continue to Con
		Students will learn key concepts to approximate values to better understand