

Practice Quiz Derivatives 2018
Introduction to Calculus

Name _____

Find the derivative of each function. Simplify each answer.

1) $y(x) = x^4 - 6\sin(x) + 8(7)^x$

$$y'(x) = 4x^3 - 6\cos(x) + 8(\ln 7)(7^x)$$

2) $g(x) = e^x \cos(x)$

$$g'(x) = e^x \cos(x) + e^x (-\sin(x))$$

$$g'(x) = e^x \cos(x) - e^x \sin(x)$$

$$\text{OR } g'(x) = e^x (\cos(x) - \sin(x))$$

4) $f(x) = \frac{1}{\sqrt{2x-1}}$

$$f'(x) = \frac{-\frac{1}{2}(2x-1)^{-1/2} \cdot 2}{(\sqrt{2x-1})^2}$$

$$f'(x) = \frac{-1}{(2x-1)^{3/2}}$$

6) $f(x) = 2\sqrt{10x}$ (Careful: Use chain rule!)

$$f'(x) = 2 \cdot \frac{1}{2}(10x)^{-1/2} \cdot 10$$

$$f'(x) = \frac{10}{(10x)^{1/2}}$$

3) $J(x) = \frac{1}{2}(6)^{8x-1}$

$$J'(x) = \frac{1}{2}(\ln 6)6^{8x-1} \cdot 8$$

$$J'(x) = 4(\ln 6)6^{8x-1}$$

5) $y = \frac{5x^{2/3}}{7} = \frac{5}{7}x^{2/3}$

$$y' = \frac{10}{21}x^{-1/3}$$

$$\text{OR } y' = \frac{10}{21x^{1/3}}$$

7) $f(x) = \frac{-3}{2x^4} = -\frac{3}{2}x^{-4}$

$$f'(x) = 6x^{-5}$$

$$f'(x) = \frac{6}{x^5}$$

$$8) f(x) = \frac{(7x^2 - x + 5)^4}{2} = \frac{1}{2}(7x^2 - x + 5)^4$$

$$f'(x) = 2(7x^2 - x + 5)^3 (14x - 1)$$

$$9) f(x) = \tan^4(3x - 1) = (\tan(3x - 1))^4$$

$$f'(x) = 4(\tan(3x - 1))^3 (\sec^2(3x - 1)) (3)$$

$$f'(x) = 12 \cdot \tan^3(3x - 1) \cdot \sec^2(3x - 1)$$

$$10) y(x) = \frac{(2)^{3x}}{(6 - 2x)^3} \quad y'(x) = \frac{(\ln 2) 2^{3x} \cdot 3 \cdot (6 - 2x)^3 - 2^{3x} \cdot 3(6 - 2x)^2(-2)}{(6 - 2x)^6}$$

$$y'(x) = \frac{(3)(2^{3x})(6 - 2x)^2 [(\ln 2)(6 - 2x) + 2]}{(6 - 2x)^4}$$

$$y'(x) = \frac{(3)(2^{3x}) [(\ln 2)(6 - 2x) + 2]}{(6 - 2x)^4}$$

Find the derivative of each function. Do NOT simplify answers.

11) $f(x) = 2x^3(6x^3 - x)^3$

$$f'(x) = 6x^2(6x^3 - x)^3 + 2x^3 \cdot 3(6x^3 - x)^2(18x^2 - 1)$$

12) $f(x) = \frac{(5x^6 - 8)^4}{5^{3x-2}}$

$$f'(x) = \frac{4(5x^6 - 8)^3(30x^5)(5^{3x-2}) - (5x^6 - 8)^4(\ln 5)(5^{3x-2})(3)}{(5^{3x-2})^2}$$

13) $f(x) = \left(\frac{\sin x}{9x^2 + 1} \right)^{12}$

$$f'(x) = 12 \left(\frac{\sin x}{9x^2 + 1} \right)^{11} \left(\frac{\cos x(9x^2 + 1) - \sin x(18x)}{(9x^2 + 1)^2} \right)$$

$$14) f(x) = \overbrace{\cos(3x)}^a \cdot \overbrace{(4x-1)^6}^b \cdot \overbrace{(2^x)}^c$$

$$f'(x) = \underbrace{-\sin(3x)(3)}_{a'} \cdot \underbrace{(4x-1)^6}_{b'} \cdot \underbrace{(2^x)}_c +$$

$$\underbrace{\cos(3x)}_a \cdot \underbrace{6(4x-1)^5(4)}_{b'} \cdot \underbrace{(2^x)}_c +$$

$$\underbrace{\cos(3x)}_a \cdot \underbrace{(4x-1)^6}_b \cdot \underbrace{(\ln 2) 2^x}_{c'}$$