

# 180 Days of Number Sense Routines Grade 3 Days 81-100





- WHY IS DEVELOPING NUMBER SENSE IMPORTANT? Number Sense is the foundational building block for all strands of mathematics. Students who struggle in mathematics do not lack mathematical ability, but rather, they simply do not have a strong number sense on which to build their knowledge. Just as we are not born knowing how to read, we are not born with Number Sense. It must be developed and nurtured over time through a progression of understandings about numbers and their relationships to one another. With time and focused practice, students come to understand that numbers are meaningful, and outcomes are sensible and expected. Number Sense development encourages students to think flexibly and promotes confidence with numbers.
- WHAT IS A NUMBER SENSE ROUTINE? A routine is an activity or event that occurs on a regular basis over time. Routines provide a framework for our day to support both the teacher and students. Routines help to build community and create a safe learning environment for students. Routines build a sense of belonging, ownership, and predictability which make the classroom a place to take risks. We learn through risk-taking; we take risks when we feel safe; we feel safe in a supportive learning environment; we create supportive learning environments through routines. Just as we have established routines for bus dismissal and fire drills, we must also establish routines that build mathematical thinking and discourse.





**HOW WILL THESE NUMBER SENSE ROUTINES BENEFIT ME AND MY STUDENTS?** What teachers do and how they do it is critically important and has a profound impact on the quality of the educational experience of our students. Effective pedagogy, the art and science of teaching, is a key element in the learning process. The Number Sense are models of effective pedagogy and ensure that the critical Number Sense instruction we provide is equitable to all our students regardless of geography, teacher experience, or student circumstance. As we prepare our students to be mathematically proficient in their lives beyond the classroom walls, these Number Sense routines will help to lay the critical foundation for all future mathematical endeavors.

#### WHAT ARE THE CCPS IMPLEMENTATION EXPECTATIONS? Number sense routines have been developed for all 180 instructional days in grades 1-5. These routines are to be used every day, including early dismissal, late arrival, and field trip days. Because the routines do not require a specific order, it is permissible to trade routines among days to best match the time available. Number Sense must be built over time. With consistency, we can build students' number sense creating a strong mathematical foundation. If students or the teacher is struggling with a routine, it is expected that the teacher collaborate with colleagues to build capacity in that routine – do not just choose to skip the routine. If additional help is needed, the teacher should seek the assistance of their content specialist or mathematics supervisor.







#### **PowerPoint or Smart Notebook?**

Since some of the slides include animation features, these slides will only work when using PowerPoint. Specifically, (1) **Estimation** when presented as images and (2) **Splat!** will <u>only</u> work correctly when you use the Slide Show feature in PowerPoint. Some teachers prefer the functionality of Smart Notebook and slides without animation can be used on this platform.

Download both the PowerPoint and the Smart Notebook versions from Schoology and place them on your computer's desktop so you can access the slides even without an internet connection.

#### **PowerPoint**

Animations for these two routines only work when presented in Slide Show mode

- Estimation
- Splat!

**PRO TIP:** You can write directly on any PowerPoint slide when it is in Slide Show mode by right clicking and selecting <Pointer Options>

#### How to Run PowerPoint in Slide Show mode:

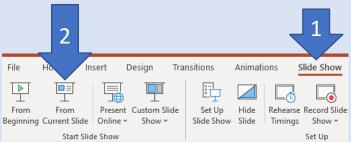
Slides with animation features, such as Splat!, must run in Slide Show mode of PowerPoint in order for the animations to work correctly.

- 1. Select <Slide Show> from the menu at the top
- 2. Select <From Current Slide>

#### **Smart Notebook**

Allows for easy annotation

- Decide & Defend
- Number Talk
- Open Number Line
- Quick Count
- Same But Different
- Which One Doesn't Belong?







#### Acknowledgements

We are grateful to those who have inspired this project – and there have been many. These slide decks were designed for Grades 1–5 with custom-built daily routines for each grade level. The nine routines blend original creations, adaptations, and borrowed OER materials. We have made our work available in Open Educational Resources so that others may benefit as we have. Our deepest gratitude and respect to all those who helped move our work forward, and a special thank you goes to the following whose own work had such a tremendous impact on our 180 Days of Number Sense Routines:

- Decide & Defend and Quick Count routines were adapted from templates created by Grace Kelemanik and Amy Lucenta at <a href="http://FosteringMathPractices.com">http://FosteringMathPractices.com</a>
- Estimation Clipboard, Esti-Mysteries, and Splat! templates created by www.SteveWyborney.com
- Same But Different discussion from Developing Grayscale Thinking by Looney Math Consulting at <a href="https://www.samebutdifferentmath.com">https://www.samebutdifferentmath.com</a>
- Which One Doesn't Belong tasks adapted from http://wodb.ca by Mary Bourassa

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# Adding 19

BEGIN WITH NUMBER:301COUNTING RULE:add 19

Say: "Today we will be counting by 19s. That seems pretty tough but let's think of some shortcuts we could use to count up by 19s more easily."

Give think time. Then discuss student ideas.

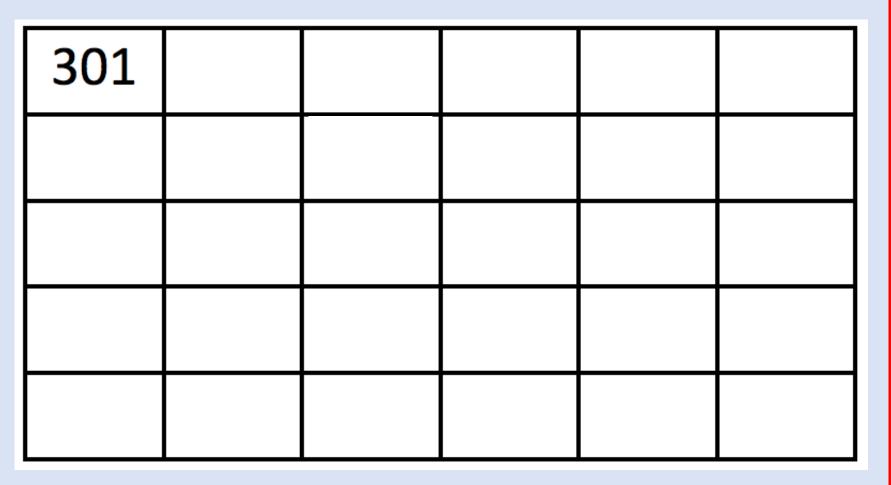
Use the chart on the next page to record the choral counting.

Remind students to count slowly and to keep pace with the numbers you are writing. Even if they can count faster, they should stay together as a group counting as you are ready to write the next number.

Once the chart is completed, spend most of the time discussing the patterns noticed on the chart and talking about efficient counting strategies (i.e. count on 20 then subtract 1 for this specific routine).

Day

# Adding 19



\*After the first row or two is completed, you may want to pause and have students begin looking for patterns that seem to be emerging from the counting routine.





Day 81

# Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!

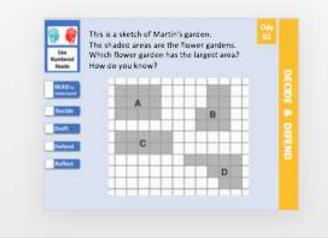


Image A has the greatest area.

At this point in the year, the goal is for students to recognize that area is the amount of space that is covered. A = 4+4+4 or 4x3 = 12 B = 4 + 6 = 10C = 5+5 or 5x2 = 10

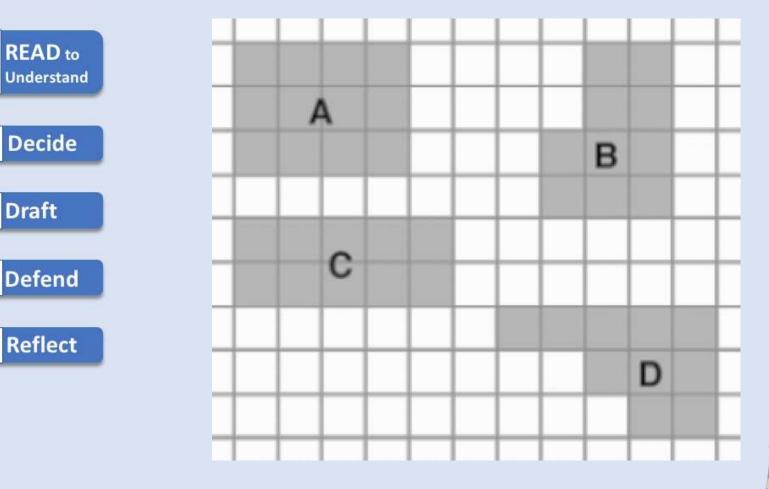
# DECIDE & DEFEND



Day



Use Numbered Heads This is a sketch of Martin's garden. The shaded areas are the flower gardens. Which flower garden has the largest area? How do you know?





Day

# **Reflect on Learning**

- What was mathematically important in the problem?
- What new math idea did you learn today?
- What suggestions can you offer someone who is trying to convince others of his/her mathematical ideas?

# **Estimation Activity**

When you are ready to use this activity, use the PowerPoint platform so the slides work properly.

PROMPT: How many dice are being held by the cup?



Day

Steve Wybomey

How many dice are being held by the cup?





#### **TEACHER NOTES**

#### **BEFORE**

This slide has the String of expressions that you will use for today's Number Talk. You can use Smart Ink, right click for PowerPoint Pen, or convert this slide to Smart Notebook so you can easily annotate on the slide. The annotation is an important part of the routine. The expressions should be presented one-at-a-time with skills building on one another.

#### DURING

#### Make A Ten: Decomposing

- 1) 40 + 24 Notice how easy it was to find the sum of these two values using just a mental calculation. Why was it easy? (because 40 is a decade number and is easy to add to)
- 2) 37+24 Hopefully, a student will suggest decomposing 24 into 3+21 so the 3 can be added quickly to the 37 to make 40. Continue to accept a wide range of ideas for solving, of course, but give special focus to the strategy of decomposing to make a quick ten for today's Number Talk as you work through the other problems.
- 3) 437+18 = 437 + 3 + 15 = 440 + 15 = 455 (a focusing question could be to ask students how many are needed to make 437 a decade number that is easier to work with)
- 4) 292+169 = 292 + 8 + 161 = 300 + 161 = 461 (again focus students to look for the amount needed to make 292 a decade number of 300)

Remember, students will come with a wide variety of strategies. Allow student sharing of these strategies and work toward determining which of the ways were most efficient and brain-friendly.

#### AFTER

After solving the expressions with various strategies, help students to understand how these expressions were all related.



Day

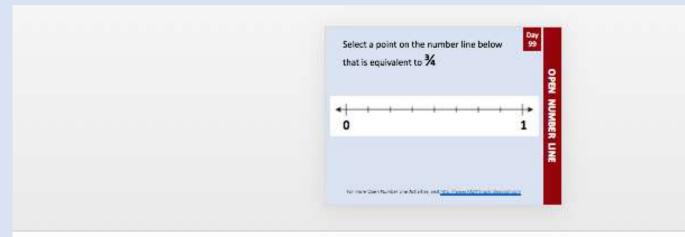
40 + 24

Calvert C

NUMBER TALK

## Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!



By counting the SPACES between the 0 and 1 on the number line, we can see that the number line is portioned into eighths. Students must recognize that each hash is 1/8. We would need to convert 3/4 to 6/8 and then count over 6 hash marks to find 3/4.

A common error would be to simply count over 3 hash marks.

Help students recognize that this is not reasonable since ¾ is GREATER than ½ and if we go over just 3 hash marks, we have moved LESS THAN ½ way to the 1.

For more Open Number Line Activities, visit http://www.MathSnack.blogspot.com



Day

# Select a point on the number line below that is equivalent to $\frac{3}{4}$





Day

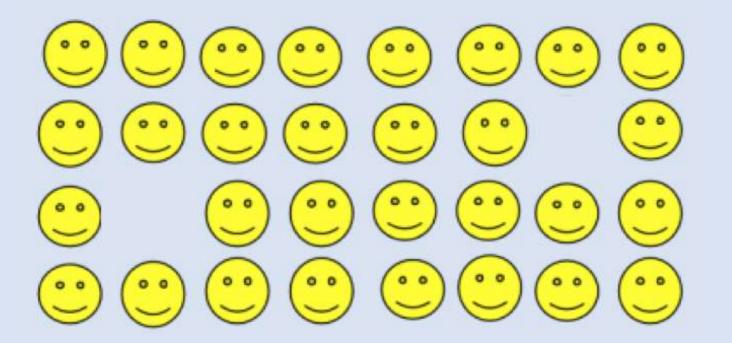
Intro

#### **Directions for QUICK COUNT routines**

Quick Count is an instructional routine designed to shift attention away from mindless calculations and toward necessary structural interpretations of mathematics. This routine fosters structural thinking, Math Practice 7, and promotes student discourse.

- 1. Pair students into Numbered Heads (or Peanut Butter Jelly partners, etc.)
- 2. Show students the first image slide for about 3-5 seconds depending on the complexity of the image and level/experience of the students.
- 3. With their partner, students discuss everything they can remember about the image.
- 4. After a minute of partner discussions, have students share ideas to the group.
- 5. Create a list of student ideas that students can refer to when the image is shown again.
- 6. Tell students that you are going to put the slide back up. Ask students to COUNT the images using some type of shortcut strategy (chunking, symmetry, arrays...)
- 7. Show the image again and leave it displayed as students look for counting shortcuts.
- 8. With their partner again, students discuss how many objects are in the image and how describe the shortcut counting strategy they used. Give time for partner discussions. Walk around and take notes about discussions to determine which students will share.
- 9. Use the slide with identical images as a comparative visual as students take turns explaining how they counted the objects in the image.
  - Use your notes to select different students with different approaches.
  - The student explains his/her shortcut as the teacher **gestures** over the image.
  - A different student is asked to REPEAT the original student's shortcut as the teacher annotates (circles, underlines) on the image to show the shortcut as the used.
  - Repeat the process using different student-generated shortcut strategies.

10 End by asking students to explain what was "mathematically important"



What do you NOTICE?

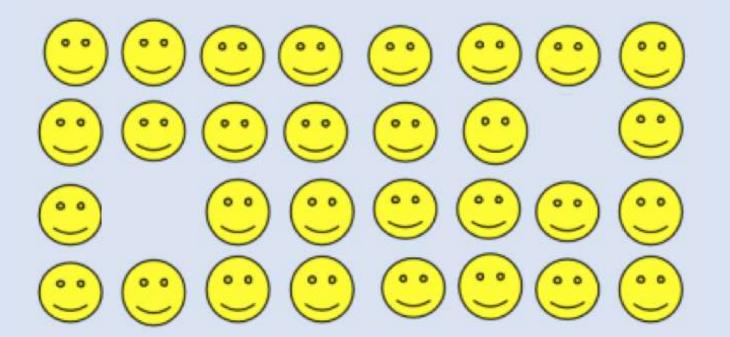


QUICK COUNT

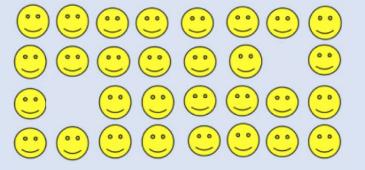
# What did you NOTICE?

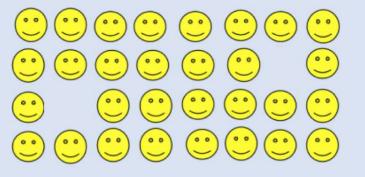
Day 86

Public Schools

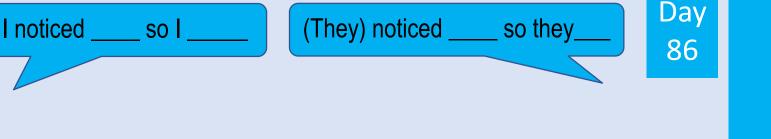


How many do you see? What counting shortcut did you use?









QUICK COUNT



# Reflect



What was mathematically important?



#### About the SAME BUT DIFFERENT Routine

Same But Different is a powerful routine for use in math classrooms. The Same but Different routine compares two things calling attention to <u>both</u> how they are the same <u>and</u> how they are different. This apparent paradox is the beauty of the activity. In this analysis, *instead of making a choice and trying to prove that these are the same or prove that they are different, students consider how two items can be <u>both</u>. This is a critically important distinction from many other tasks.* 

**One of the reasons students struggle in math is that they struggle to make connections**. Someone who has poorly developed number sense might see each number as its own thing, and not part of the larger network of mathematical ideas. A mathematical conversation using the language *same but different* that calls attention to how a new concept in math is the same as another familiar and comfortable concept but different in a specific way is a useful conversation in growing a student's network of connections. Building these connections could also reduce anxiety as children become the sense-makers in the conversation.

Source: www.samebutdifferent.net.com/about

#### Facilitating the SAME BUT DIFFERENT Routine

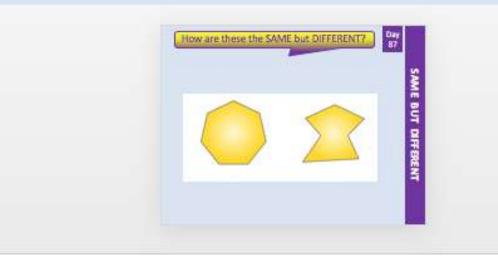
- 1. Present the slide
- 2. Ask students to THINK about how the two items are both the SAME AND DIFFERENT.
- 3. Do not allow conversation at this time -- give ample think time for students to consider the possibilities
- 4. After some time has been given (a minute or so), ask students to talk with their Number Head partner or small group about their ideas -- allow this conversation to dominate the time dedicated to this routine
- 5. As students talk with partners/groups, walk around and listen to the conversations. Resist jumping in; let them grapple with the ideas with their peers.
- 6. As you walk around listening, take notes. You will use these notes to help direct the whole group conversation.
- Refocus student attention to the front of the room for a whole group debriefing session. Ask students to share some of their ideas about how the two were both the SAME and DIFFERENT – use the notes you took to bring out important ideas that will benefit the entire room.



## Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!

- Students may simply recognize a component that makes them the "same" OR "different"
- Some students may state a same/different relationship and say that they are the "same because.... But different because...."



#### POSSIBLE RESPONSES

- Both are polygons (closed shapes made from straight lines that connect at the endpoints)
- Both are the same color
- Both have 7 sides (a seven-sided polygon is called a heptagon)
- The one on the left has equal sized sides. The one on the right does not.
- The one on the left has equal sized interior angles. The one on the right does not.
- The one on the left is called a "REGULAR heptagon. The one on the right is not, it is irregular.

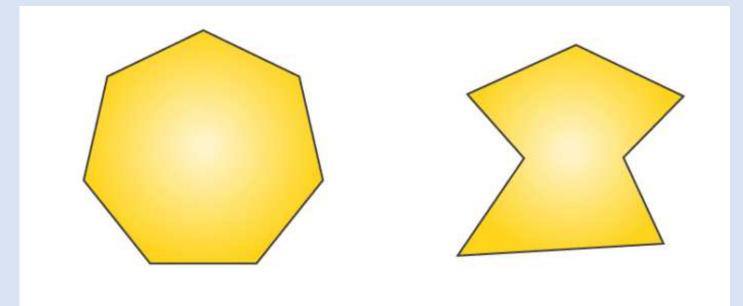


Day

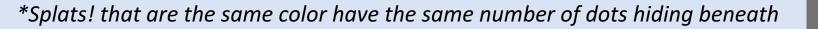
# How are these the SAME but DIFFERENT?

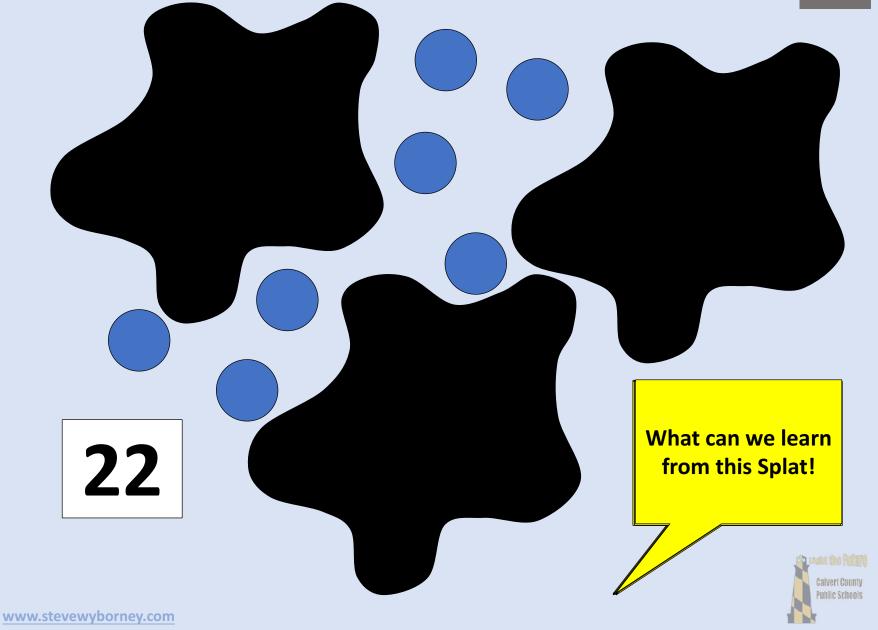


# SAME BUT DIFFERENT



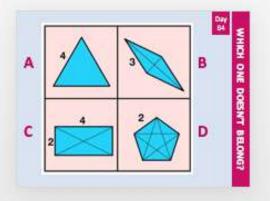






# Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!

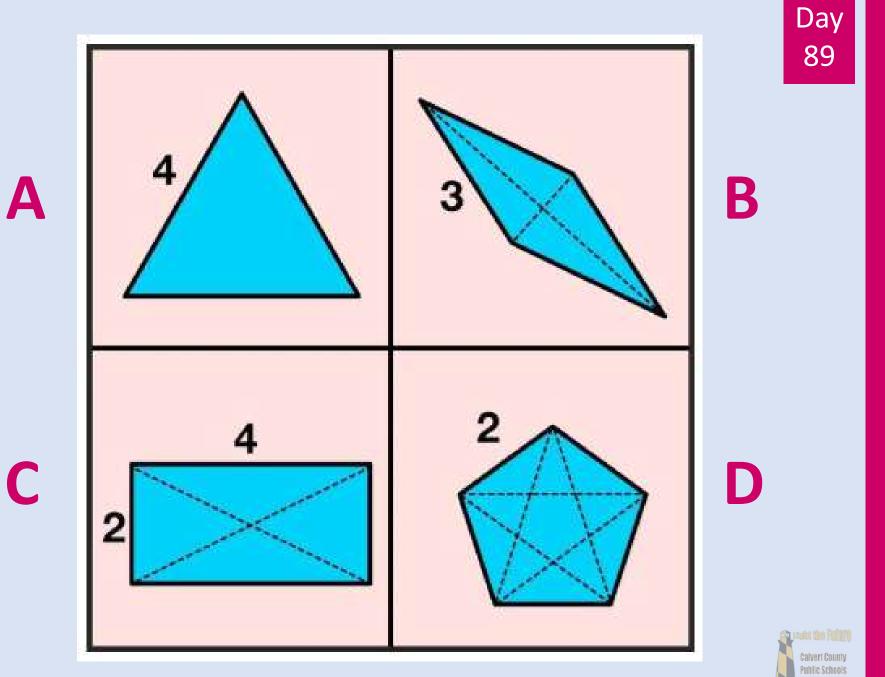


- A Triangle Three of the shapes have a dotted line that connects two of the corners (these are called "diagonals", a term that
  students will learn in middle/high school). Shape A does not have any diagonals since diagonals only attach non-adjacent vertices
  and all vertices in a triangle are adjacent to each other
- B Rhombus Three of the shapes were made with all equal-sized angles. Shape B does not have all equal angles, it has two
  different sized angles.
- C Rectangle Three of the shapes have all equal-sized edges. The side on Shape C are not all equal-sized. (NOTE: If students say that the rectangle is the only one with two different numbers, probe further and ask WHY it is the only one that has two different numbers to get to the idea that the sides on the other 3 figures are equal lengths: 4,4,4 or 3,3,3,3 or 2,2,2,2,2 instead of 2,2,4,4)
- D Pentagon Three of the shapes have interior shapes of triangles. Shape D is the only one that was portioned into shapes that
  were not all triangles (the center shape is a pentagon surrounded by ten triangles)



Day

# WHICH ONE DOESN'T BELONG?

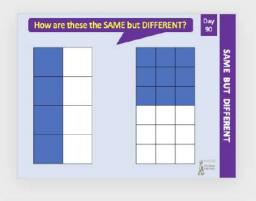


#### Use the NEXT SLIDE with students.

**TODAY'S GOAL:** Since Day 90 marks the halfway point of the schoolyear, we will use our Number Sense Routine today to explore the concept of halves on the number line.

\*\*Before beginning today's Number Sense Routine, set the stage by explaining why today is a special day:

Today is Day 90 of school. We go to school 180 days each year. The number **90 is HALF of 180**, so today marks the HALFWAY point of our school year. To celebrate the HALFWAY point of school, we will focus our Number Talk today on HALF.



Possible Responses:

- BOTH REPRESENT HALF (remember the theme of the day)!
- Both have half shaded but one is represented by 4/8 and the other is represented by 9/18
- Both have half shaded but one shows the left side shaded and the other shows the top half shaded
- Both have the same amount of AREA shaded but one is a long, shaded rectangle and the other is a shaded square





Dav

# How are these the SAME but DIFFERENT?



Day

# **Estimation Activity**

A new type of Estimation FUN!

Students use clues to solve the estimation mystery. After all of the clues are revealed, students will have enough information to determine if their initial estimate was correct.





Before seeing the clues, estimate how many erasers are in the cup.

As the clues appear, use the information to narrow the possibilities to a smaller set. Then use estimation to determine which of the remaining answers is the most reasonable.

\*Esti-Mysteries will only work correctly in Slide Show mode of PowerPoint – select "Play from Current Slide"





<u>Clue #1</u>

Count by 2's from 2 to 30. The answer is one of those numbers.

<u>Clue #2</u> The answer is greater than 10.

<u>Clue #3</u> The answer is less than 30.

<u>Clue #4</u> One of the digits is a 4.

<u>Clue #5</u> There are now two possibilities. Which one do you think it is?



By combining the clues and estimation, you now have enough information to determine the answer.





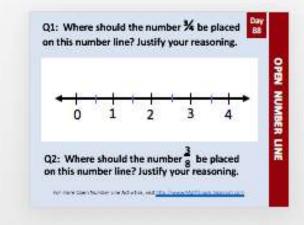
## The Reveal Click to see the answer.



www.stevewyborney.com

### Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!



Q1: ¾ would fall between 0 and 1 since it is a value that is greater than 0 but less than 1 whole. More specifically, it should fall halfway between the ½ hash mark and 1.

Two common misconceptions to look out for and to help build students conceptual understanding:

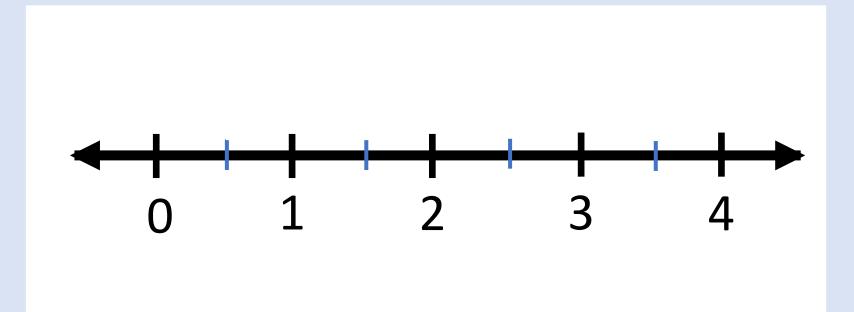
- Fractions have a value that is less than one
- The fraction <sup>3</sup>/<sub>4</sub> will fall between the 3 and 4 on the number line

Q2: The number 3/8 would again fall between 0 and 1 because it is a fraction that has a value of less than 1. Imagine that the section between 0 and 1 is partitioned into 8 equal parts. 3/8 would use 3 of those 8 parts. Students should reason that 3/8 is LESS than half (4/8 is half), so it should fall just slightly left of the halfway mark between 0 and 1.



Day

# Q1: Where should the number $\frac{3}{4}$ be placed on this number line? Justify your reasoning.



# Q2: Where should the number $\frac{3}{8}$ be placed on this number line? Justify your reasoning.



Day

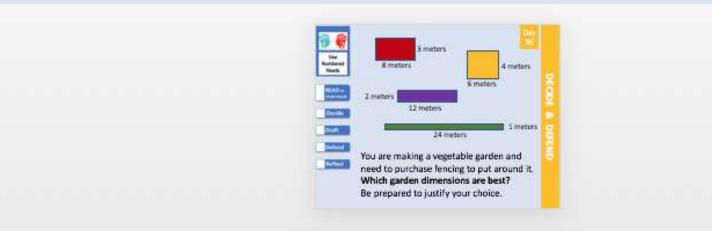
92

OPEN NUMBER LINE

### Use the NEXT SLIDE with students.

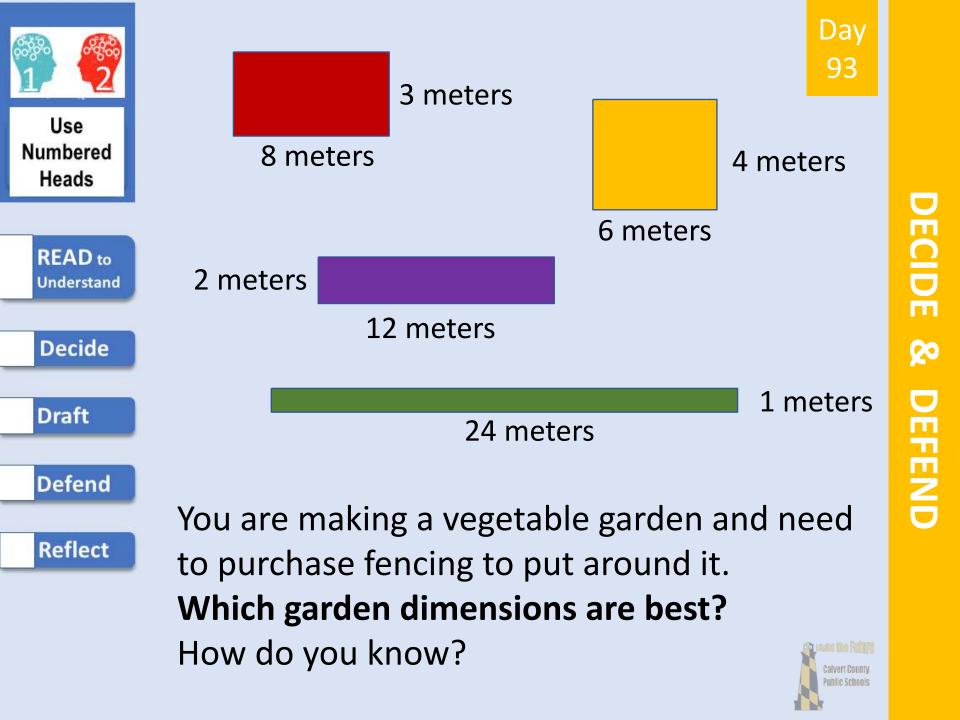
Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!





All of the gardens have an area of 24 square meters, so the amount of space to plant vegetables is equal. The difference is in the amount of fencing (and subsequent cost) you are required to purchase to go around the fence. Red = 22 meters (8+3=11 then 11+11=22) Yellow = 20 meters Purple = 28 meters Green = 50 meters





## **Reflect on Learning**

- What was mathematically important in the problem?
- What new math idea did you learn today?



CHORAL COUNTING

#### Multiplying by Multiples of 10 (3.NBT.A.3)

#### This activity will only run in **PowerPoint** use Slide Show mode

Across the top of the game board are multipliers; each is a multiple of ten (10, 20, 40, 80). When the teacher clicks the mouse or presses the RETURN key on the keyboard, a single-digit number will appear on the game board. As the number appears, students multiply the single digit number with the multiple of ten at the top of the column (2 x 10). The teacher says "2x10" and the students respond in chorus "20".

When all of the slides have been revealed, the actual math fun begins! The power of Choral Counting is not in the counting part, but rather, in the discussion of patterns and number relationships. Ask students to look for patterns that they notice. Discuss with a partner. Then share with the class. Be sure to discuss WHY that pattern is occurring – what MATH led to that pattern/relationship of numbers? Below are some of the patterns they may notice:

- All products end in zero
- Each column is double of the previous column (because the multiplier x10, x20, x40 is double of the previous column)
- Each row is multiplied by the same number. Follow up with the question, "so what patterns of sums do we see?" (the tens place is a multiple of the multiplier on the 3 row, for example, there are 3 tens, 6 tens, 12 tens, 24 tens)
- 3x40 and 6x20 have the same product (explore why! This is the rule of *halves and doubles*: If we half one number and double the other in multiplication, the product is the same).



### Multiplying by Multiples of 10

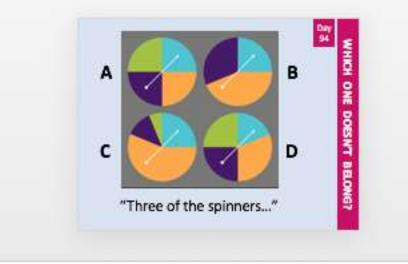
x 10	x 20	x 40	x 80
2 x 10	2 x 20	2 x 40	2 x 80
20	40	80	160
3 x 10	3 x 20	3 x 40	3 x 80
30	60	120	240
4 x 10	4 x 20	4 x 40	4 x 80
40	80	160	320
5 x 10	5 x 20	5 x 40	5 x 80
50	100	200	400
6 x 10	6 x 20	6 x 40	6 x 80
60	120	240	480
7 x 10	7 x 20	7 x 40	7 x 80
70	140	280	560



\*Remember: This slide only runs in PowerPoint Slide Show (select Play from Current Slide)

### Use the NEXT SLIDE with students.

Here is are some possible responses. This list is not all-inclusive. Additional ideas encouraged!

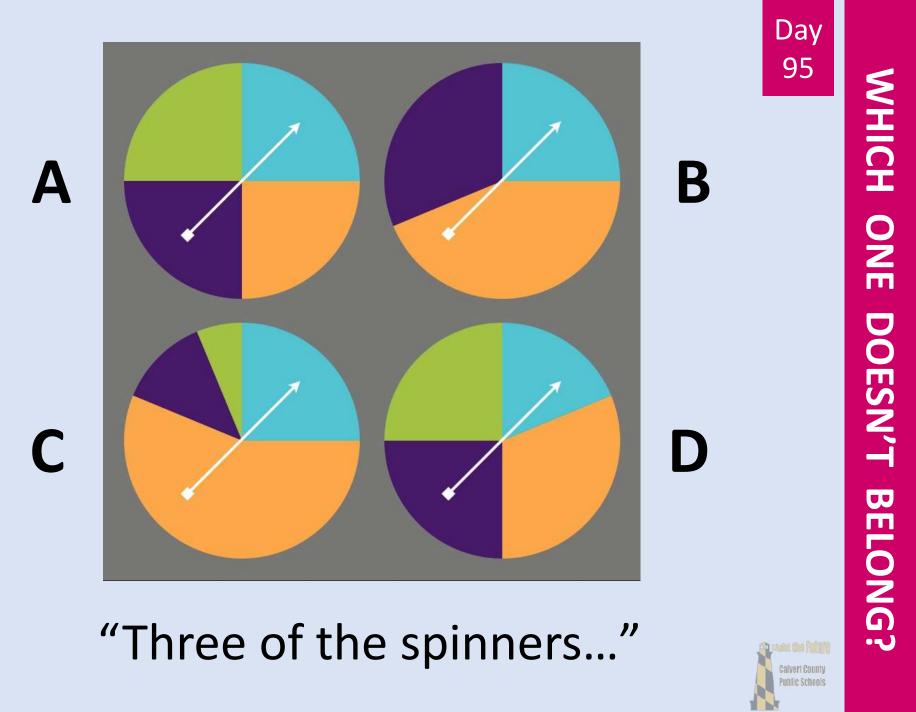


Possible Responses:

- A Three of the spinners are partitioned into Unequal parts. Spinner A is not partitioned into unequal parts, they are equal parts.
- · B Three of the spinners have 4 colors. Spinner B does not have 4 colors, it only has 3 colors
- C Three of the spinners have the orange color covering less than half of the spinner. Spinner C has the orange covering more than half.
- D Three of the spinners have the blue color covering exactly ¼ of the circle. On Spinner D, the blue is less than ¼ of the circle.



Day



#### **TEACHER NOTES**

This slide has the String of expressions that you will use for today's Number Talk. You can use Smart Ink, right click for PowerPoint Pen, or convert this slide to Smart Notebook so you can easily annotate on the slide. The annotation is an important part of the routine. The expressions should be presented one-at-a-time with skills building on one another.

#### DURING

Making Landmark or Friendly Numbers – use numbers that are one away from a landmark or friendly number.

This string of expressions all contain values that are just one or two numbers away from a landmark number. Help student to recognize that decomposing numbers to make landmark numbers is an easy way to find the sum using mental calculations.

- 39 + 16 = 39 + 1 + 15 = 40 + 15 = 55
- 28 + 39 = 27 + 1 + 39 = 27 + 40 = 67 (notice that it may be easier to adjust 39 to an easier tens value in this one)
- 59 + 13 = 59 + 1 + 12 = 60 + 12 = 72
- 23 + 49 = 22 + 1 + 49 = 22 + 50 = 72 (again notice that it was easier to adjust the second value)

Remember, students will come with a wide variety of strategies. Allow student sharing of these strategies and work toward determining which of the ways were most efficient and brain-friendly.

#### AFTER

After solving the expressions with various strategies, help students to understand how these expressions were all related. Explicitly discuss the strategy of making landmark/friendly numbers.



Day

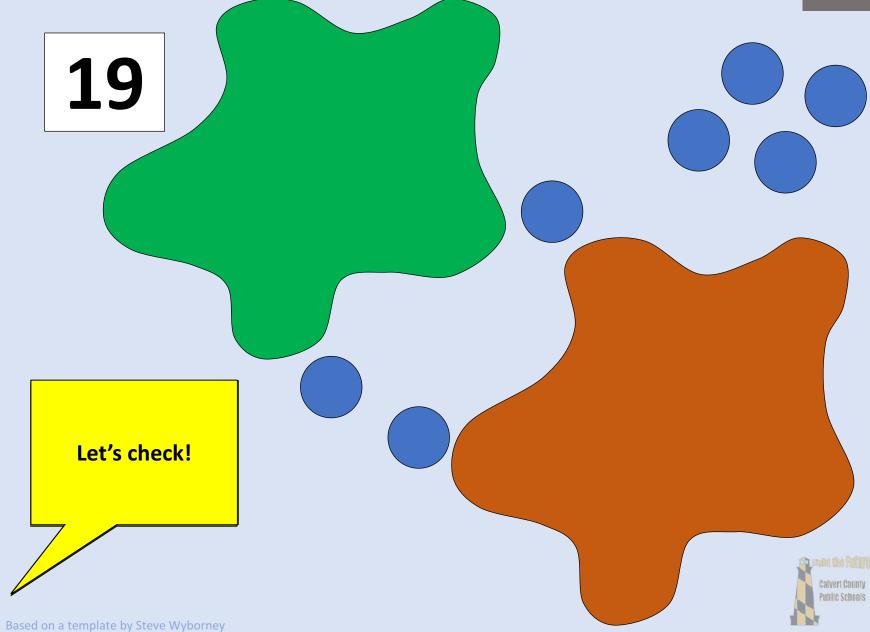




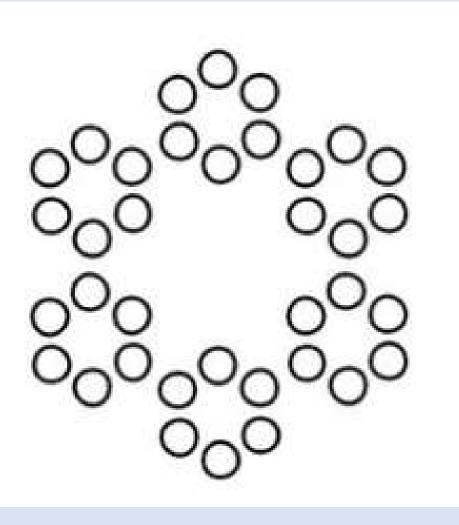
\*Splats! that are different colors have different quantities of dots hiding.

Day 97

**SPLAT!** 







### What do you NOTICE?

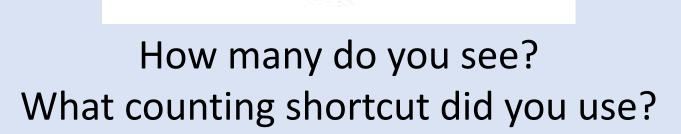


Day

# What did you NOTICE?



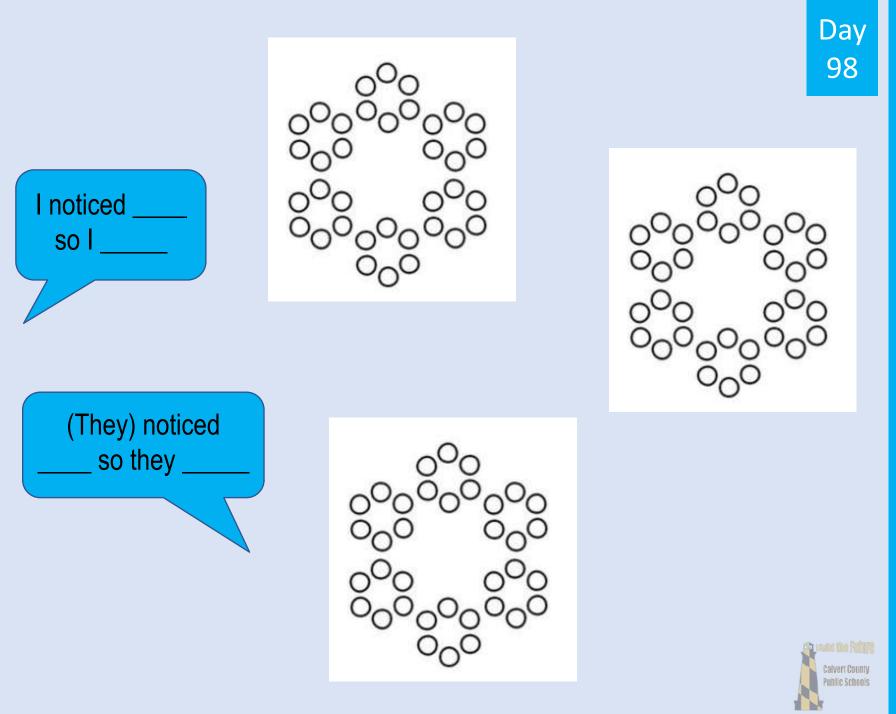






Day





### Reflect



What was mathematically important?



#### **TEACHER NOTES**

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#### DURING

Multiplying with Multiples of Ten

This string of equations is designed to help students recognize that they can use their basic multiplication facts to help them solve equations that multiply by a multiple of ten (10, 20, 30, 40....)

- Since 7x4=28, 70x4=280
- Since 2x4=8, 2x40=80
- Since 9x9=81, 9x90=810

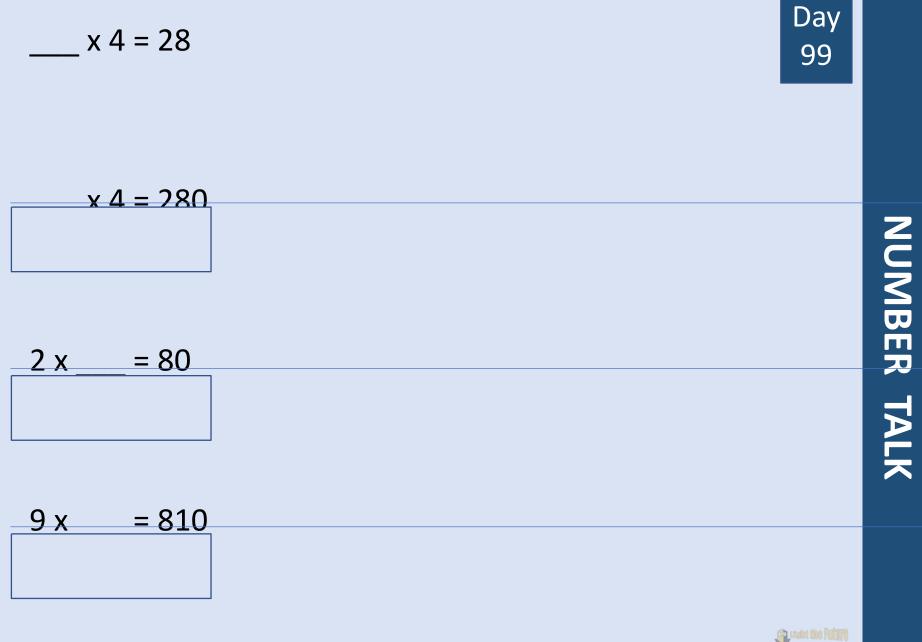
Remember, students will come with a wide variety of strategies. Allow student sharing of these strategies and work toward determining which of the ways were most efficient and brain-friendly.

#### **AFTER**

After solving the expressions with various strategies, help students to understand how these expressions were all related.



Dav



Calvert County Public Schools



Use Numbered Heads

> READ to Understand

Since today is the 100<sup>th</sup> day of school, let's talk about the number 100.

These 15 full size marshmallows weigh exactly 100 grams.

Decide Draft Defend Reflect

Look at the items on the next page. Decide which ones weigh more than 100 grams. Be ready to justify your predictions.



Day

100

100 grams



### Which of these weigh MORE THAN 100 grams?

Use Numbered Heads



Decide







A pair of reading glasses



Salt & pepper shakers



Three packs of granola bars



Day

100

DECIDE & DEFEND



### Which of these weigh MORE THAN 100 grams?

Use Numbered Heads



Decide





7 baby carrots 82 grams



A pair of reading glasses **17 grams** 



Salt & pepper shakers 252 grams



Three packs of granola bars 130 grams



Day

100

DECIDE & DEFEND



Use Numbered

Heads







About how many more carrots are needed to weigh a total of 100 grams?

How do you know? What calculation did you use to determine that amount?



## **Reflect on Learning**

- What was mathematically important in the problem?
- What new math idea did you learn today?
- What suggestions can you offer someone who is trying to convince others of his/her mathematical ideas?