# Lesson 14

Objective: Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.

#### **Suggested Lesson Structure**

Total Time	(60 minutes)
Student Debrief	(10 minutes)
Concept Development	(38 minutes)
Fluency Practice	(12 minutes)



# Fluency Practice (12 minutes)

Sprint: Subtraction	from Teens	2.OA.2	(8 minutes)
Coin Drop 2.OA.2		(	(2 minutes)

More and Less 2.NBT.5 (2 minutes)

# Sprint: Subtraction from Teens (8 minutes)

Materials: (S) Subtraction from Teens Sprint

Note: Students practice subtraction from teens to gain mastery of the sums and differences within 20.

# Coin Drop (2 minutes)

Materials: (T) 10 dimes, 10 pennies, metal or plastic can

Note: In this activity, students practice adding and subtracting ones and tens using coins in preparation for Module 7.

- T: (Hold up a penny.) Name my coin.
- S: A penny.
- T: How much is it worth?
- S: 1 cent.
- T: Listen carefully as I drop coins in my can. Count along in your minds.

Drop in some pennies, and ask how much money is in the can. Take out some pennies, and show students. Ask how much money is still in the can. Continue adding and subtracting pennies for a minute or so. Repeat the activity with dimes and then with dimes and pennies.



4: Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.





#### More and Less (2 minutes)

Materials: (T) 10 dimes, 10 pennies

Note: In this activity, students practice adding and subtracting ones and tens using coins.

- T: Let's count by tens. (Move dimes to the side while counting.)
- S: 10, 20, 30, 40, 50, 60.
- T: How many dimes are shown?
- S: 6 dimes.
- T: What is the value of 6 dimes?
- S: 60 cents.
- T: What is 5 cents more? (Move 5 pennies.)
- S: 65 cents.
- T: Give the number sentence.
- S: 60 cents + 5 cents = 65 cents.
- T: What is 10 cents less? (Move one dime.)
- S: 55 cents.
- T: Give the number sentence.
- S: 65 cents 10 cents = 55 cents.

Repeat this line of questioning by starting with 7 dimes, removing 3 dimes, and asking for the number sentence. Continue by adding 3 pennies and asking for the number sentence, adding 4 dimes and asking for the number sentence, and so forth.

# **Concept Development (38 minutes)**

Materials: (T) Rectangles (Template) (S) Rectangles (Template), Problem Set, scissors

In this lesson, the Problem Set is used during the Concept Development.

T: Today, we're going to use the Problem Set for our lesson! We'll use the sentence frames to record our answers and to speak in complete sentences.

Pass out the template, Problem Set, and scissors. For each step of the instructions, model as students work. Circulate to be sure students are following the steps accurately.

- T: Cut Rectangle A into rows, and complete Problem 1. Share your responses and thinking with your partner. (Allow students time to work and share.)
- T: Cut Rectangle B into columns, and complete Problem 2. Share again.



#### NOTES ON MULTIPLE MEANS OF ACTION AND EXPRESSION:

Assist students in using appropriate math vocabulary by providing a list of current words used in the module and adding to the list as new words are introduced. Post these words with definitions or illustrations prominently in the classroom so students can refer to them during the lessons.



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Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.





- S: They both show the same amount, and they're both the same size and shape. → I can see the same rectangle different ways: It's 2 rows of 4, 4 columns of 2, or 8 squares. → They're both made up of rows and columns with the same total.
- T: You've recognized that we can decompose the same rectangle into rows, columns, or individual square units.
- T: Take both your rows of 4 and cut them to show 4 twos instead of 2 fours.
- T: (Demonstrate as necessary.) Put together your twos to form one long rectangle that has 8 columns of 2.
- T: Imagine we were going to put 2 rows on top to make the exact same rectangle. Talk to your partner. Explain what those rectangles would be.



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If there are students who miss lessons in the module and others who struggle to grasp the concept, ask those who struggle to explain the array concepts to the previously absent students. This helps students to clarify their thinking or discover what questions to ask to understand the concept better.

- S: I see it would be 2 rows of 8.  $\rightarrow$  We need 2 eights.  $\rightarrow$  They would be 2 of the long skinny rectangles.
- T: We can decompose this rectangle into 2 rows of 8 or 8 columns of 2.
- T: Cut out all your squares from Rectangles A and B. How many squares do you have now?
- S: 16.

**MP.7** 

- T: Use your 16 squares to answer Problem 3.
- T: To answer Problem 4, cut out your squares from Rectangles A, B, and C.

Circulate as students experiment with their squares to form their rectangles. Ask them questions about each rectangle to support their spatial structuring, such as "How many rows do you see in this rectangle?" or "How many columns?" This lesson's intent is to give practice in seeing the same rectangle both as rows and columns. It is important for students to work with more tiles to increase the complexity of the work. Encourage them to view the array with 24 squares as a rectangle rather than as 24 individual squares. Students who struggle can work with fewer squares.



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Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



# **Student Debrief (10 minutes)**

**Lesson Objective:** Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson. At the end of the Debrief today, review and clarify the directions for the Homework to check for student understanding.

Any combination of the questions below may be used to lead the discussion.

- What did we learn about our rectangles by first cutting them into rows and columns before cutting out each individual square?
- If you were to write a repeated addition sentence to describe the work we did in Problem 2, what would it look like? Why? How does this relate to the columns you cut out?
- For Problem 3, what was your strategy for composing a new rectangle? How did the rows and columns change?
- For Problem 4, what strategy did you use to compose a new rectangle with 24 squares?
- How many different possibilities can you think of for composing a rectangle with 24 squares? How many different repeated addition sentences? How do they match the rows and columns of your array?

#### Exit Ticket (3 minutes)

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help with assessing students' understanding of the concepts that were presented in today's lesson and planning more effectively for future lessons. The questions may be read aloud to the students.

Name Roberto	Date		
Cut out Rectangles A, B, and C. Then cut according following using Rectangles A, B, and C. <sup>1</sup>	to directions. A	Inswer each of the	
1. Cut out each row of Rectangle A,			
a. Rectangle A has <u>2</u> rows.			
b. Each row has <u>4</u> squares.			
c 2 rows of 4 = 8			
d. Destande 4 has 8 several			
o. Rechangle x has <u>o</u> squares,			
<ol> <li>Cut out each column of Rectangle B.</li> </ol>			
a. Rectangle B has <u> </u>			
<li>b. Each column has <u>2</u> squares.</li>			
c columns of =			
d. Rectangle B has squares.			
<sup>1</sup> Note: This Problem Set is used with a template of three identics Rectangles A, B, and C.	al 2 by 4 arrays. The	e arrays are labeled as	
COMMON Lessen 34: Use scissors to partition a rectargle in control of arrives with the sources	to same-size squares, and	engage <sup>ny</sup>	666
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	Commission Consultants Mitchensing Star		
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NYS COMMON CORE MATHEMATICS CURRICULUM 3. Cut out each square from both Rectangles A a. Construct a new rectangle using all 16 squ	and B.	n 14 Problem Set	2*6
THIS COMMON CORE MATHEMATICS CURRECULUM 3. Cut out each square from both Rectangles A a. Construct a new rectangle using all 16 squ b. My rectangle has <u>2</u> rows of <u>8</u>	Lesso and B. Jares.	n 14 Problem Set	2*6
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THIS COMMON CORE MATHEMATICS CURRECULUM 3. Cut out each square from both Rectangles A a. Construct a new rectangle using all 16 squ b. My rectangle has <u>2</u> rows of <u>8</u> c. My rectangle also has <u>8</u> columns of d. Write two repeated addition number sen	Lesso and B. Jones. 2	n 14 Problem Set	2*6
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HYS COMMON CORE MATHEMATICS CURRICULUM 3. Cut out each square from both Rectangles A a. Construct a new rectangle using all 16 squ b. My rectangle has <u>2</u> rows of <u>8</u> c. My rectangle also has <u>8</u> columns of d. Write two repeated addition number sen 2+2+2+2+2+2+2+2+2+4 4. Construct a new array using the 24 squares a. My rectangle has <u>4</u> rows of <u>6</u> b. My rectangle also has <u>6</u> columns of c. Write two repeated addition number sen 4+4+4+4+4+4=24 Extension: Construct another array using the s a. My rectangle has <u>3</u> rows of <u>8</u>	Lesso and B. Jores. 2 tences to matc $2 = 1/\varphi$ from Rectangle 4 tences to matc 4 + (b + b + b) quares from Re - 3	In 14 Problem Set	2*6
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HYS COMMON CORE MATHEMATICS CURRICULUM 3. Cut out each square from both Rectangles A a. Construct a new rectangle using all 16 squ b. My rectangle has <u>2</u> rows of <u>8</u> c. My rectangle also has <u>8</u> columns of d. Write two repeated addition number sen 2+2+2+2+2+2+2+2+4 4. Construct a new array using the 24 squares a. My rectangle has <u>4</u> rows of <u>10</u> b. My rectangle also has <u>6</u> columns of c. Write two repeated addition number sen 4*4+4+4+4+4+24 Extension: Construct another array using the s a. My rectangle has <u>3</u> rows of <u>8</u> b. My rectangle has <u>8</u> columns of c. Write two repeated addition number sen 8+8+8=2.4	Lesso Lesso Lesso Lesso Jares. 2 tences to matc 2 = 1/p from Rectangle 2 = 1/p tences to matc b + (b + b + b) quares from Re 3 tences to matcl 3 + 3 + 3 + 3 + 3 + 3	h your rectangle. $8+8 = 10^{\circ}$ h your rectangle. $8+8 = 10^{\circ}$ s A, B, and C. h your rectangle. =2.4 ictangles A, B, and C. h your rectangle. =3+3+3+3=2.4	2+6

Lesson 14



Lesson 14:

Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



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# Α

Subtraction from Teens

Number Correct: \_\_\_\_\_

1.	11 - 10 =	
2.	12 - 10 =	
3.	13 - 10 =	
4.	19 - 10 =	
5.	11 - 1 =	
6.	12 - 2 =	
7.	13 - 3 =	
8.	17 - 7 =	
9.	11 - 2 =	
10.	11 - 3 =	
11.	11 - 4 =	
12.	11 - 8 =	
13.	18 - 8 =	
14.	13 - 4 =	
15.	13 - 5 =	
16.	13 - 6 =	
17.	13 - 8 =	
18.	16 - 6 =	
19.	12 - 3 =	
20.	12 - 4 =	
21.	12 - 5 =	
22.	12 - 9 =	

23.	19 - 9 =	
24.	15 - 6 =	
25.	15 - 7 =	
26.	15 - 9 =	
27.	20 - 10 =	
28.	14 - 5 =	
29.	14 - 6 =	
30.	14 - 7 =	
31.	14 - 9 =	
32.	15 - 5 =	
33.	17 - 8 =	
34.	17 - 9 =	
35.	18 - 8 =	
36.	16 - 7 =	
37.	16 - 8 =	
38.	16 - 9 =	
39.	17 - 10 =	
40.	12 - 8 =	
41.	18 - 9 =	
42.	11 - 9 =	
43.	15 - 8 =	
44.	13 - 7 =	



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Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



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# B

# Subtraction from Teens

1.	11 - 1 =	
2.	12 - 2 =	
3.	13 - 3 =	
4.	18 - 8 =	
5.	11 - 10 =	
6.	12 - 10 =	
7.	13 - 10 =	
8.	18 - 10 =	
9.	11 - 2 =	
10.	11 - 3 =	
11.	11 - 4 =	
12.	11 - 7 =	
13.	19 - 9 =	
14.	12 - 3 =	
15.	12 - 4 =	
16.	12 - 5 =	
17.	12 - 8 =	
18.	17 - 7 =	
19.	13 - 4 =	
20.	13 - 5 =	
21.	13 - 6 =	
22.	13 - 9 =	

23.	16 - 6 =	
24.	14 - 5 =	
25.	14 - 6 =	
26.	14 - 7 =	
27.	14 - 9 =	
28.	20 - 10 =	
29.	15 - 6 =	
30.	15 - 7 =	
31.	15 - 9 =	
32.	14 - 4 =	
33.	16 - 7 =	
34.	16 - 8 =	
35.	16 - 9 =	
36.	20 - 10 =	
37.	17 - 8 =	
38.	17 - 9 =	
39.	16 - 10 =	
40.	18 - 9 =	
41.	12 - 9 =	
42.	13 - 7 =	
43.	11 - 8 =	
44.	15 - 8 =	

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Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



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Number Correct: \_\_\_\_\_

Improvement: \_\_\_\_\_

Name

Cut out Rectangles A, B, and C. Then, cut according to directions. Answer each of the following using Rectangles A, B, and  $C^{1}$ .

- 1. Cut out each row of Rectangle A.
  - a. Rectangle A has \_\_\_\_\_ rows.
  - b. Each row has \_\_\_\_\_ squares.
  - c. \_\_\_\_\_ rows of \_\_\_\_\_ = \_\_\_\_\_
  - d. Rectangle A has \_\_\_\_\_ squares.
- 2. Cut out each column of Rectangle B.
  - a. Rectangle B has \_\_\_\_\_ columns.
  - b. Each column has \_\_\_\_\_ squares.
  - c. \_\_\_\_\_ columns of \_\_\_\_\_ = \_\_\_\_\_
  - d. Rectangle B has \_\_\_\_\_ squares.

 $<sup>^1</sup>$ Note: This Problem Set is used with a template of three identical 2 by 4 arrays. These arrays are labeled as Rectangles A, B, and C.



Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



- 3. Cut out each square from both Rectangles A and B.
  - a. Construct a new rectangle using all 16 squares.
  - b. My rectangle has \_\_\_\_\_ rows of \_\_\_\_\_.
  - c. My rectangle also has \_\_\_\_\_ columns of \_\_\_\_\_.
  - d. Write two repeated addition number sentences to match your rectangle.
- 4. Construct a new array using the 24 squares from Rectangles A, B, and C.
  - a. My rectangle has \_\_\_\_\_ rows of \_\_\_\_\_.
  - b. My rectangle also has \_\_\_\_\_ columns of \_\_\_\_\_.
  - c. Write two repeated addition number sentences to match your rectangle.

Extension: Construct another array using the squares from Rectangles A, B, and C.

- a. My rectangle has \_\_\_\_\_ rows of \_\_\_\_\_.
- b. My rectangle also has \_\_\_\_\_ columns of \_\_\_\_\_.
- c. Write two repeated addition number sentences to match your rectangle.

Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



Name	Date

With your tiles, show 1 rectangle with 12 squares. Complete the sentences below.

I see \_\_\_\_\_ rows of \_\_\_\_\_.

In the exact same rectangle, I see \_\_\_\_\_ columns of \_\_\_\_\_.



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Name	Date

- 1. Imagine that you have just cut this rectangle into rows.
  - a. What do you see? Draw a picture.

How many squares are in each row?

b. Imagine that you have just cut this rectangle into columns. What do you see? Draw a picture.

How many squares are in each column?

2. Create another rectangle using the same number of squares.

How many squares are in each row?

How many squares are in each column?



Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



- 3. Imagine that you have just cut this rectangle into rows.
  - a. What do you see? Draw a picture.

How many squares are in each row?

b. Imagine that you have just cut this rectangle into columns. What do you see? Draw a picture.

How many squares are in each column?

4. Create another rectangle using the same number of squares.

How many squares are in each row?

How many squares are in each column?



Use scissors to partition a rectangle into same-size squares, and compose arrays with the squares.



Rectangle A

Rectangle B

Rectangle C



rectangles



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