Mathematics

Brunswick School Department
Algebra II: Academic
Unit 5: Exponential Functions

Essential Understandings	▪ Exponential functions can be used to model real-life situations.
Essential Questions	▪ What are the properties of Algebra and how are these used to solve exponential functions? ▪ What natural phenomena are modeled by exponential functions? ▪ How do you solve exponential equations? ▪ How do you draw reasonable graphs of exponential functions?
Essential Knowledge	▪ Algebraic manipulation and the rules of exponents are used to solve exponential equations. ▪ An asymptote is a boundary line for a graph.
Vocabulary	▪ Terms: o exponential function, asymptote, exponential growth and decay, the number e, exponential regression
Essential Skills	▪ Apply order of operation. ▪ Identify exponential growth and decay. ▪ Manipulate exponential expressions. ▪ Solve exponential equations by various means. ▪ Sketch reasonable graphs of exponential functions.

Related Maine Learning Results	Mathematics
	A. Number
	  Real Number
	  A1.Students will know how to represent and use real numbers.
	    a. Use the concept of nth root.
	    b. Estimate the value(s) of roots and use technology to approximate them.
	    c. Compute using laws of exponents.
	    d. Multiply and divide numbers expressed in scientific notation.
	    e. Understand that some quadratic equations do not have real solutions and that there exist other number systems to allow for solutions to these equations.

Related Maine Learning Results	B. Data
	   Measurement and Approximation
	   B1. Students understand the relationship between precision and accuracy.
	    a. Express answers to a reasonable degree of precision in the context of a given problem.
	    b. Represent an approximate measurement using appropriate numbers of significant figures.
	    c. Know that most measurements are approximations and explain why it is useful to take the mean of repeated measurements.
	   Data Analysis
	   B2. Students understand correlation and cause and effect.
	    a. Recognize when correlation has been confused with cause and effect.
	    b. Create and interpret scatter plots and estimate correlation and lines of best fit.
	    c. Recognize positive and negative correlations based on data from a table or scatter plot.
	    d. Estimate the strength of correlation based upon a scatter plot.
	   B3. Students understand and know how to describe distributions and find and use descriptive statistics for a set of data.
	    a. Find and apply range, quartiles, mean absolute deviation, and standard deviation (using technology) of a set of data.
	    b. Interpret, give examples of, and describe key differences among different types of distributions: uniform, normal, and skewed.
	    c. For the sample mean of normal distributions, use the standard deviation for a group of observations to establish 90%, 95%, or 99% confidence intervals.
	   B4. Students understand that the purpose of random sampling is to reduce bias when creating a representative sample for a set of data.
	    a. Describe and account for the difference between sample statistics and statistics describing the distribution of the entire population.
	    b. Recognize that sample statistics produce estimates for the distribution of an entire population and recognize that larger sample sizes will produce more reliable estimates.
	    c. Apply methods of creating random samples and recognize possible sources of bias in samples.

Related Maine Learning Results	D. Algebra
	  Symbols and Expressions
	  D1.Students understand and use polynomials and expressions with rational exponents.
	    a. Simplify expressions including those with rational numbers.
	    b. Add, subtract, and multiply polynomials.
	    c. Factor the common term out of polynomial expressions.
	    d. Divide polynomials by (ax+b).

Related Maine Learning Results	Equations and Inequalities
	
	D2. Students solve families of equations and inequalities.
	   a. Solve systems of linear equations and inequalities in two unknowns and interpret their graphs.
	   b. Solve quadratic equations graphically, by factoring in cases where factoring is efficient, and by applying the quadratic formula.
	   c. Solve simple rational equations.
	   d. Solve absolute value equations and inequalities and interpret the results.
	   e. Apply the understanding that the solution(s) to equations of the form $f(x) = g(x)$ are x-value(s) of the point(s) of intersection of the graphs of $f(x)$ and $g(x)$ and common outputs in table of values.
	   f. Explain why the coordinates of the point of intersection of the lines represented by a system of equations is its solution and apply this understanding to solving problems.
	
	D3. Students understand and apply ideas of logarithms.
	   a. Use and interpret logarithmic scales.
	   b. Solve equations in the form of $x + b^y$ using the equivalent form $y = \log_b x$.
	
	Functions and Relations
	
	D4. Students understand and interpret the characteristics of functions using graphs, tables, and algebraic techniques.
	   a. Recognize the graphs and sketch graphs of the basic functions.
	   b. Apply functions from these families to problem situations.
	   c. Use concepts such as domain, range, zeros, intercepts, and maximum and minimum values.
	   d. Use the concepts of average rate of change (table of values) and increasing and decreasing over intervals, and use these characteristics to compare functions.
	
	D5. Students express relationships recursively and use iterative methods to solve problems.
	   a. Express the (n+1)st term in terms of the nth term and describe relationships in terms of starting point and rule followed to transform one terms to the next.
	   b. Use technology to perform repeated calculations to develop solutions to real life problems involving linear, exponential, and other patterns of change.

Sample Lessons And Activities	- Solve exponential equations using a variety of techniques. These include graphing, logarithms and changing bases. - Model real world data.
Sample Classroom Assessment Methods	- Evaluate homework. - Quizzes. - Chapter test.
Sample Resources	- Publications: - Holt Algebra 2 - McDougal Littell Algebra 2 - Other Resources: - Graphing calculators - The A+ learning system for remediation