

2-6 Algebraic Proofs

Geometry

Name _____

Period _____

A two-column proof or _____ contains statements and reasons organized in two- columns.

One type of two-column proof is an _____. An algebraic proof is made up of a series of algebra statements. We can use properties of real numbers in algebraic proofs.

| Property | Definition |
|-------------------------------------|------------|
| Addition Property of Equality | |
| Subtraction Property of Equality | |
| Multiplication Property of Equality | |
| Division Property of Equality | |
| Transitive Property of Equality | |
| Substitution Property of Equality | |
| Distributive Property | |

Example 1:

Given: $8x - 5 = 2x + 1$

Prove: $x = 1$

Proof:

| Statements | Reasons |
|---------------------------------|--------------------------|
| a. $8x - 5 = 2x + 1$ | a. _____ |
| b. $8x - 5 - 2x = 2x + 1 - 2x$ | b. _____ |
| c. _____ | c. Substitution Property |
| d. _____ | d. Addition Property |
| e. $6x = 6$ | e. _____ |
| f. $\frac{6x}{6} = \frac{6}{6}$ | f. _____ |
| g. _____ | g. _____ |

Example 2:

Given: $\frac{4x + 6}{2} = 9$

Prove: $x = 3$

Proof:

| Statements | Reasons |
|--|-----------------|
| a. $\frac{4x + 6}{2} = 9$ | a. _____ |
| b. $2\left(\frac{4x + 6}{2}\right) = 2(9)$ | b. Mult. Prop. |
| c. $4x + 6 = 18$ | c. _____ |
| d. $4x + 6 - 6 = 18 - 6$ | d. _____ |
| e. $4x =$ _____ | e. Substitution |
| f. $\frac{4x}{4} =$ _____ | f. Div. Prop. |
| g. _____ | g. Substitution |

Example 3:

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PROOF Write a two-column proof to verify each conjecture.

1. If $m\angle ABC + m\angle CBD = 90$, $m\angle ABC = 3x - 5$,
and $m\angle CBD = \frac{x + 1}{2}$, then $x = 27$.

