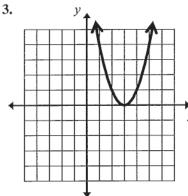
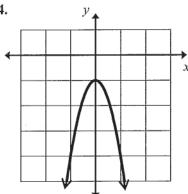
What does "find the zeros of the function" mean? To find the x-value(s) that make the function f(x) = 0

When you are solving a quadratic equation by graphing, what do you look for on the graph?

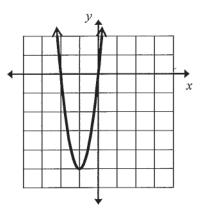
The x-intercepts

#3 - 5: Determine whether the quadratic functions have two real roots, one real root, or no real roots. If possible, list the zeros of the function.





5.



Period

Number and type

of roots: 1 real root

Zeros: $\chi = 3$

Number and type

Zeros: None

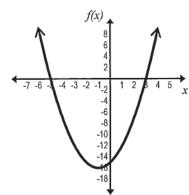
Number and type

of roots: no real roots of roots: 2 real roots

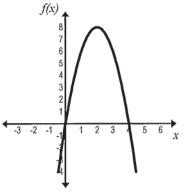
Zeros: X = 0 or X = -3

#6-7: Use the graph to find the zeros of the following quadratic functions. Check that the solutions work.

 $f(x) = x^2 + 2x - 15$



7. $f(x) = -2x^2 + 8x$



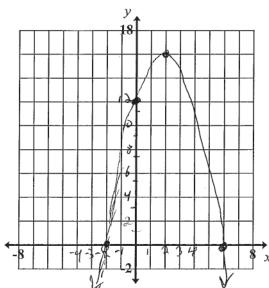
Solution(s):

Solution(s): $f(0) = -3(0)^3 + 8(0) = 0$ Check: $f(4) = -3(4)^3 + 8(4)$ -33 + 33 = 0

5.1A Solving Quadratic Equations by Graphing

#8 - 9: Graph each of the following quadratic functions and use the graph to find the zeros. Create a table of values if necessary. Verify that the values truly are solutions.

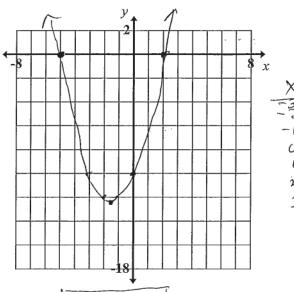
8.
$$f(x) = -x^2 + 4x + 12$$



Solution(s): X = -2, 6

Verify: f(-2) = -(-2) + 4(-2) + 12 = -(4) + -8 + 12

9. $f(x) = x^2 + 3x - 10$



to the nearest hundredth. Question #13 - 15, verify that the values truly are solutions.

10.
$$x^2 - 7x = 11$$

 $x^3 - 7x - 11 = 0$

$$Solution(s):$$

12.
$$5x^2 - 7x - 3 = 8$$

10. $x^{2} - 7x = 11$ $\chi^{2} - 7x - 11 = 0$ 11. $6x^{2} = -19x - 15$ $6x^{2} + 19x + 15 = 0$ 12. $5x^{2} - 7x - 3 = 8$ $5x^{2} - 7x - 3 = 8$ $5x^{2} - 7x - 11 = 0$ Solution(s): $\chi = -1.32$, $\chi = -1.6$, $\chi =$

Solution(s):
$$X = 7.6$$
, -1.5

Solution(s):
$$\chi = -0.99$$
, 2,34

13.
$$\frac{1}{2}x^2 - x = 8$$

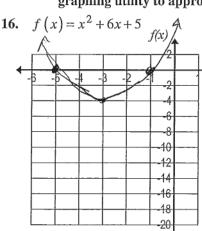
Solution(s):
$$\chi = -3.12$$
, 5.12 (Solution(s): $\chi = -5.16$, 1.16) (Solution(s): $\chi = -1.16$, 2.16)

Verify: $2 \times (-3.12) - (-3.12)$

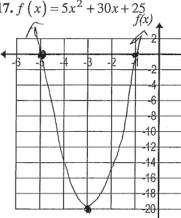
5.1 I CAN USE TABLES AND GRAPHS TO SOLVE QUADRATIC EQUATIONS INCLUDING REAL-WORLD SITUATIONS AND TRANSLATE BETWEEN REPRESENTATIONS.

5.1A Solving Quadratic Equations by Graphing

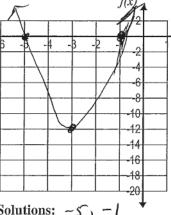
#16 - 18: Use a graphing utility to graph the following functions. Draw the graph of the function. Use the graphing utility to approximate the zeros to the nearest tenth.



17. $f(x) = 5x^2 + 30x + 25$



18. $f(x) = 3x^2 + 18x \pm 15$

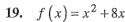


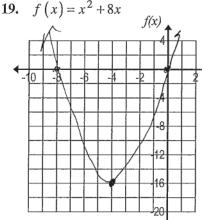
Solution(s): -5,-1

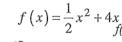
Solution(s): -5, -1

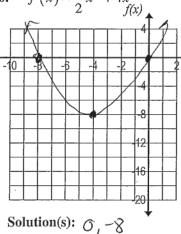
Solutions: -5, -1

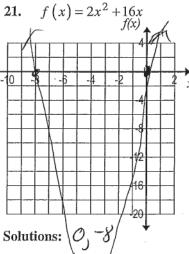
#19 - 21: Use a graphing utility to graph the following functions. Draw the graph of the function. Use the graphing utility to approximate the zeros to the nearest tenth.











Solution(s): $\mathcal{O}_1 - \mathcal{V}$

- 22. Investigation:

 - a) Looking to Question #16 18, record the following: Function in #16 $f(x) = x^2 + 6x + 5$ Solution

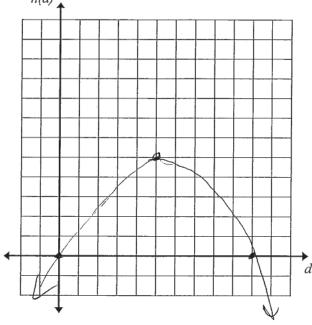
 - Function in #17 $f(x) = 5x^2 + 30x + 25$
- Solutions in #16 $\times = -5$, -/
 Solutions in #17 $\times = -5$, -/
 Solutions in #18 $\times = -5$, -/
- > Function in #18 $f(x) = 3x^3 + 18x + 15$
- b) Looking to Question #19 21, record the following:
 - > Function in #19 $f(x) = x^2 + 8x$ Solutions in #19 x = 6, -8> Function in #20 $f(x) = \frac{1}{2}x^2 + 4x$ Solutions in #20 x = 0, -8> Function in #21 $f(x) = 3x^2 + 16x$ Solutions in #21 x = 0, -8

- c) Comparing the functions in questions 16, 17, and 18, and then again in 19, 20, and 21, write a conjecture about the relationship of the functions within each set of questions and the solutions of those functions.

5.1A Solving Quadratic Equations by Graphing

23. A bottlenose dolphin jumps out of the water. The path the dolphin travels can be modeled by the function $h(d) = -0.2d^2 + 2d$, where h represents the height, in feet, of the dolphin and d represents the horizontal distance, in feet, the dolphin traveled. h(d)

a) Sketch a graph of the quadratic equation.



- b) What is the maximum height the dolphin reaches? Where is this represented on the graph of the function? 5ft; the vertex
- c) What is the horizontal distance that the dolphin jumps? Where is this represented on the graph of the function?

 10 ft; the x in tercept > 0

Section 5.1A

5.1B Answering Real-World Questions by Graphing Quadratic Functions

#1 - 10: Use your graphing utility to solve the following problems.

- 1. Phillip, Peter and Pablo each throw a ball over a fence. The height of Phillip's ball with respect to time can be modeled by the equation $y = -16t^2 + 60t$. The height of Peter's ball with respect to time can be modeled by the equation $y = -16t^2 + 50t$. The height of Pablo's ball with respect to time can be modeled by the equation $y = -16t^2 + 40t$, where y is the height in feet and t is the time in seconds for each of the three models.
 - a) Phillip, Peter and Pablo want to know whose ball hit the ground first. Peter thinks that they should find the *x*-intercept of the graphs to determine this. Phillip thinks that they should find the vertex of each graph to find which ball hit the ground first. Which one is correct? Explain your answer.

Peter is correct; the xint gives the time (t) when y=0, which is where the ball has a height of o on the ground!

b) Whose ball hit the ground first? How long did it take?

Pablo; 2,5 sec

c) Whose ball hit the ground second? How long did it take?

Peter, 3,125 sec

- 2. A quarterback throws a football at an initial height of 5.5 feet with an initial upward velocity of 35 feet per second. The height of a tossed ball with respect to time can be modeled by the quadratic function $h(t) = -16t^2 + v_0 \cdot t + h_0$ where v_0 is the initial upward velocity, h_0 is the initial height and h(t) is the height of the ball after t seconds.
 - a) Write the function that models the height of the ball with respect to time. $h(\ell) = -16 \ell^2 + 35 \ell + 5.5$
 - b) How high will the football be after 1 second? (Consider what the 1 second represents.)

 44.5 Pt (the 1 sec vepr the x value)
 - c) When will the football be 10 feet high? (Consider what the 10 feet represents.) (The 10 is the y value)
 After O.14 secs and again after 2.05 secs
 - d) When will the football reach its maximum height? (When graphing the function, consider what significant feature of the graph represents this concept.)

 After 1.09 Secs
 - e) What is the maximum height of the football?

24,64 ft

f) When will the football hit the ground if no one catches it? (When graphing the function, consider what significant feature of the graph represents this concept.) (the x int)

233 seconds

5.1B Answering Real-World Questions by Graphing Quadratic Functions

#1-10 (continued): Use your graphing utility to solve the following problems.

- 3. Suppose a batter hits a baseball, and the height of the baseball above the ground can be modeled by the function $h(t) = -16t^2 + 50t + 2$. Where is the vertex of the graph? Explain the meaning of the vertex in the context of this situation.

 The vertex reveals how long it takes (1.56 sec), to reach the maximum height (41.06 ft)

- 5. The driver of a car traveling downhill on a road applied the brakes. The speed of the car, s(t), in kilometers per hour t seconds after the brakes were applied is modeled by the function rule $s(t) = -4t^2 + 12t + 80$.
 - a) After how many seconds did the car reach its maximum speed?

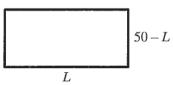
b) What was the maximum speed reached?

c) How long will it take the car to stop?

Answering Real-World Questions by Graphing Quadratic Functions 5.1B

#1 - 10 (continued): Use your graphing utility to answer the following problems.

Andrew has 100 feet of fence to enclose a rectangular tomato patch. He wants to find the dimensions of the rectangle that encloses the most area. The width of the rectangle can be found by the expression 50 - L where L is the length of the rectangle.

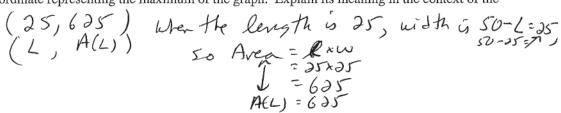


a) In the expression representing the width of the rectangle (50-L), what does the 50 represent? Explain your thinking clearly.

50 is half the perimeter, so one length + one with = 50.

b) Write a function rule to model the area of the rectangle. A(L) represents the Area of the rectangular tomato patch base on the length (L) of one side.

 $A(L) = \frac{L(50-L)}{A(L)} = \frac{L(50-L)}{L^2 + 50L}$ c) Find the coordinate representing the maximum of the graph. Explain its meaning in the context of the

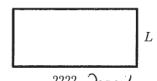


d) What size should Andrew make the tomato patch in order to enclose the most area within the fencing?

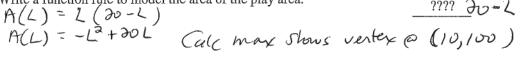
a Square Shape, 25 ft x 25 ft

- Sharon needs to create a fence for her new puppy. She purchased 40 feet of fencing to enclose the four sides of a rectangular play area.
 - a) Determine the dimensions the enclosure play area should be to produce the greatest area for her

According to #6d, she should make a square with her 40 ft of feneral, 50 40:4 = 10 ft or each side.



b) Write a function rule to model the area of the play area.



c) What are the dimensions of the enclosure that will create the greatest area for her puppy to play?

Longth L = 10 ft with 20-L = 10 ft Area = 100 ft >

5.1B Answering Real-World Questions by Graphing Quadratic Functions

#1 - 10 (continued): Use your graphing utility to answer the following problems.

8. Karen is throwing an orange to her brother Jim, who is standing on the balcony of their home. The height, h (in feet), of the orange above the ground t seconds after Karen throws the orange is given by the function $h(t) = -16t^2 + 32t + 3$. If Jim's outstretched arms are 16 feet above the ground, will the orange ever be high enough so that he can catch it? Explain your answer.

enough so that he can catch it? Explain your answer.

Jest I The wax height of the crange is 19 ft, or the
y coordinate of the vertex,
I'm can grab it either on the way yo or the way down.

9. On wet concrete, the stopping distance, s (in feet), of a car traveling v miles per hour is given by $s(v) = 0.055v^2 + 1.1v$. At what speed could a car be traveling and still stop at a stop sign 30 feet away?

(V, 30) Use Calc retersect V= 15,41 mph, so 2/5 mph

- 10. The Buckingham Fountain in Chicago shoots water from a nozzle at the base of the fountain. The height, in feet, of the water above the ground t seconds after it leaves the nozzle is given by $h(t) = -16t^2 + 90t + 15$.
 - a) What is the maximum height of the water spout to the nearest tenth of a foot?
 - b) How long does it take for the water to hit the ground?

5,79 Secs

Section 5.1B

5.2A Factoring Review

#1 - 12: Factor out the greatest common factor (GCF) for each polynomial and write in factored form.

1.
$$2x+6$$

3.
$$7a + 28$$

$$2x + 6$$
Ans: $2(x+3)$

$$\begin{array}{c|c} 3y & -9 \\ \hline Ans: 3(9-3) \end{array}$$

$$7a + 28$$
Ans: $7(a+4)$

$$\begin{bmatrix} 36z & -12 \\ -12 & 12 \end{bmatrix}$$
Ans: $32 + 12 = 1$

5.
$$b^2 + b$$

6.
$$2r-r^2$$

7.
$$9t^2 + t$$

8.
$$4n^2 - 5n$$

$$b^2 + b$$

$$2r - r^2$$

Ans:
$$+(9++1)$$

$$\begin{vmatrix} 4n^2 & -5n \\ Ans: & n/4n-5 \end{vmatrix}$$

9.
$$4h^2 + 12h$$

10.
$$9x - 27x^2$$

11.
$$2a^2 + 4a$$

12.
$$20d^2 - 24d$$

$$4h^2 + 12h$$
Ans: $9h(h+3)$

$$9x - 27x^2$$

$$\begin{array}{c|cccc}
9x & -37x^2 & 2a^2 & +4a \\
Ans: 9x(1-3x) & Ans: 2a(a+2)
\end{array}$$

#13 - 27: Factor each polynomial.

13.
$$x^2 + 13x + 42$$

14.
$$x^2 + 6x + 9$$

15.
$$x^2 + 12x + 32$$

Ans:
$$(x+7)(x+6)$$
 Ans: $(x+3)(x+3)$ Ans: $(x+8)(x+4)$

16.
$$x^2 + 3x - 10$$

$$Ans(X+3)(x+3)$$

17.
$$x^2 - 10x + 25$$

18.
$$x^2 - x - 12$$

$$Ans: (X+5)(x-2)$$

19.
$$3x^2 + x - 4$$

Ans:
$$(x-5)(x-5)$$

20.
$$2x^2 + 5x - 12$$

Ans:
$$(X+5)(x-2)$$
 Ans: $(X-5)(x-5)$ Ans: $(X-4)(x+3)$

21.
$$4x^2 - 12x + 9$$

$$Ans(3x+4)(x-1)$$

$$Ans(3x+4)(x-1) \qquad Ans(2x-3)(x+4) \qquad Ans(2x-3)(2x-3)$$

Ans:
$$(2x-3)(2x-3)$$

5.2A Factoring Review

#13 – 27 (continued): Factor each polynomial.

22.
$$12x^2 - 8x + 1$$

23.
$$2x^2 - 8x - 10$$

 $2(x^2 - 4/x - 5)$

24.
$$3x^2 + 21x + 18$$

 $3(x^2 + 7x + 6)$

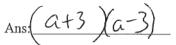
Ans.
$$(6x-1)(2x-1)$$
 Ans. $(2x+1)(x-5)$ Ans. $(3(x+1)(x+6))$
25. a^2-9 26. x^2-16 27. $25x^2-36$

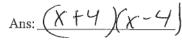
Ans:
$$3(x+1)(x+6)$$

25.
$$a^2 - 9$$

26.
$$x^2 - 16$$

27.
$$25x^2 - 36$$







#28-29: The following quadratic functions are written in standard form. Convert them to factored form.

28.
$$y = x^2 + 3x + 2$$

29.
$$y = x^2 - 49$$

X-intercepts have a y-coordinate of O. Setting y=0 and easily solving for x gives the solution(s), which are the x-intercept(s),

#31 – 32: Convert the following quadratic functions to factored form and identify the x-intercepts.

31.
$$y = x^2 - 24x + 80$$

$$(x - 4)(x - 20)$$

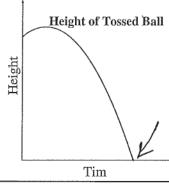
32.
$$y = x^2 + 9x - 10$$

 $0 = (x - 1)(x + 10)$

x-intercepts: 4 and 20

x-intercents: / and 70

33. The parabola graphed below shows the height of a ball tossed into the air.



- a) Draw an arrow to the location of the graph that would represent when the ball hits the ground?
- b) Explain why you placed the arrow at that location.

y=0 means the grand level.

Section 5.2A

5.2B Solve Quadratic Equations by Factoring: Part I

#1 - 3: Solve for x.

1.
$$(x-4)(x+9)=0$$

2.
$$(x-2)(3x-6)=0$$

2.
$$(x-2)(3x-6)=0$$
 3. $(4x+3)(2x-5)=0$

#4 – 17: Factor the quadratic expression then solve the equation by factoring. Verify your solution(s).

4.
$$4x^2 - 36 = 0$$

$$4. \frac{4x^{2}-36=0}{4(x^{2}-9)} = 0$$

$$4(x^{2}-9) = 0$$

$$4(x+3(x-3)=0$$

$$(x=3 \text{ a. }3)$$

$$4(-3)^{2}-36=0$$

$$4(3)^{2}-36=0$$

$$4(3)^{2}-36=0$$

$$4(3)^{2}-36=0$$

✓ Verify your solution(s):

5.
$$5x^2 - 20 = 0$$

√ Verify your solution(s):

6.
$$3x^2 - 9x = 0$$

✓ Verify your solution(s):

7.
$$7x^2 - 28x = 0$$

8.
$$x^2 + 8x - 9 = 0$$

$$\begin{pmatrix} (x+q)(x-1) \\ x=-9 & n & x=1 \end{pmatrix}$$

9.
$$x^2 + 7x + 12 = 0$$

$$(x+4)(x+3)=0$$

Verify your solution(s):

$$7(0)^{2}-38(0)=0$$
 \sim
 $7(4)^{2}-38(4)$
 $7(16)-38(4)$
 $112-112=0$

$$(-4)+7(-4)+12=02$$

 $(-3)^2+7(-3)+12=02$

5.2B Solve Quadratic Equations by Factoring: Part I

#4 - 17 (continued): Factor the quadratic expression then solve the equation by factoring. Verify your solution(s).

10.
$$x^2 - 10x + 25 = 0$$

$$(x-5)(x-5) = 0$$

$$(x-5)(x-5) = 0$$

11.
$$x^2 - 3x = 4$$

 $x^3 - 3x - 4 = 0$
 $(x+1)(x-4) = 0$
 $(x-1)(x-4) = 0$

12.
$$x^{2}-4x=5$$
 $x^{3}-4x-5=0$
 $(x+1)(x-5)=0$
 $(x=-1)5$

✓ Verify your solution(s): (5)2-10(5)+25

Verify your solution(s):

$$(-1)^{3}-3(-1)$$

 $1+3=4\nu$
 $(4)^{3}-3(4)$
 $16-12=4\nu$

13.
$$x^2 - 13x = -40$$

$$(x - 8)(x - 5) = 0$$

$$(x - 8)(x - 5) = 0$$

14.
$$3x^2 + 10x + 8 = 0$$

 $(3x+4)(x+2)$
 $x = -43, -2$

15.
$$8x^2 + 6x - 5 = 0$$

$$(4x + 5)(2x - 1) = 0$$

$$(4x + 5)(2x - 1) = 0$$

√Verify your solution(s): (8)2-13(8) 64-104 = -40~ (5) 2-13(5) 16. $5x^2 + 11x = -2$ 5x2+11x+2=0 (5x+1)(x+2)=0 K=-1/x,-2

Verify your solution(s):

$$3(-\frac{4}{3})^3 + 10(-\frac{4}{3}) + 18$$

 $\frac{3}{3}$, $\frac{16}{9}$
 $\frac{16}{3} - \frac{40}{3} + \frac{24}{3} = 0$
 $3(-2)^2 + 10(-2) + 18 = 0$
 $17. 2x^2 - 15x = 8$
 $2x^2 - 15x - 8 = 0$
 $(2x + 1)(x - 8) = 0$
 $(2x + 1)(x - 8) = 0$

✓ Verify your solution(s): $3(-\frac{4}{3})^{3} + 10(-\frac{4}{3})^{4} + 1$ $3(-2)^{2} + 10(-2) + 3 = 0$ $17. 2x^{2} - 15x = 8$ $17. 2x^{2} - 15x = 8$

Verify your solution(s):
$$5\left(-\frac{1}{5}\right)^{2} + 11\left(-\frac{1}{5}\right) + 2$$

$$2\left(-\frac{1}{5}\right)^{2} - 15\left(-\frac{1}{5}\right)$$

$$3\left(\frac{1}{4}\right)^{2} + \frac{1}{5} = \frac{16}{5}$$

$$5\left(-\frac{1}{5}\right)^{2} + 11\left(-\frac{1}{5}\right)$$

$$3\left(\frac{1}{5}\right)^{2} - 15\left(\frac{1}{5}\right)$$

$$3\left(\frac{$$

Verify your solution(s):

$$2(-\frac{1}{3})^{2} - 15(-\frac{1}{3})$$

 $3(\frac{1}{4})^{2} + \frac{1}{3} = \frac{16}{3}$
 $2(8)^{2} - 15(8)$
 $138 - 120 = 8$

Section 5.2B

Solve Quadratic Equations by Factoring: Part II

#1-9: Solve the following application problems.

1. One leg of a right triangle is 1 foot longer than the other leg. The hypotenuse is 5 feet. Find the dimensions



of the right triangle.

$$x = \begin{cases} x^2 + (x+1)^2 = 25 \\ x^2 + x^2 + 2x + 1 = 35 \\ 2x^2 + 2x - 24 = 0 \\ 2(x^2 + x - 12) = 0 \end{cases}$$

- Verify your solution(s): $2(x^{2} + x 12) = 0$ $2(x^{2} + x 12) = 0$ 2(



2. One leg of a right triangle is 7 f
the right triangle.

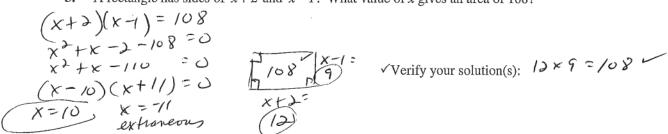
$$x^2 + (x+7)^2 = 13$$
 $x^2 + (x+7)^2 = 13$
 $x^2 + x^2 + 14x + 449 = 169$
 $x + 14x - 130 = 0$
 $x + 14x - 130 = 0$

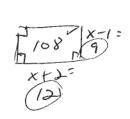
Verify your solution(s):

$$5^{2} + 12^{2} = 13^{2}$$

$$35^{2} + 144^{2} = 169^{2}$$

3. A rectangle has sides of x+2 and x-1. What value of x gives an area of 108?





4. A rectangle has sides of x-1 and x+1. What value of x gives an area of 120?

$$(x-1)(x+1)=120$$

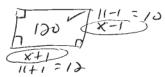
$$x^{2}-1-120=0$$

$$x^{3}-121=0$$

$$(x+11)(x+1)=0$$

$$x=-14-121$$

✓ Verify your solution(s):



The product of two positive numbers is 120. Find the two numbers if one numbers is 7 more than the other.

$$(x+7)=120$$

 $(x+8)(x+15)=0$
 $(x+8)(x+15)=0$

Verify your solution(s): $\frac{1}{8}(15) = 130$

5.2C Solve Quadratic Equations by Factoring, Part II

A rectangle has a 50-foot diagonal. What are the dimensions of the rectangle if it is 34 feet longer than it is



wide? $\chi^2 + (x+34)^2 = 50^2$ X x2+x2+68+1156=2500 2x2+68x-1344=0 2 (x2+ 34x-672) = 0 2 (x-14) (x#48) =0

Two positive numbers have a sum of 8, and their product is equal to the larger number plus 10. What are the

Let X = 15T # X(8-X) = X+10 8-X=2nc # $8X-X^2 = X+10$ $0 = X^2-7X+10$

Product 5(3) = 5+10 V So 2#s are 5+3

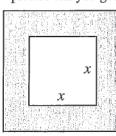
0=(x-5)(x-2) x=5 for x=2 Verify your solution(s): x=5 for x=2 Verify Each So the 2-positive the are 5 and 3

The product of two negative integers is 24. The difference between the integers is 2. Find the integers.

Let X+2 = and integer neg Then x(x+2)=24

(x-4)(x+6) = 0 Verify your solution(s): x = 4 or x = -6 = 2 = 2 = -6 are the 2 negative ints. (-6)(-4) = 2L

Framing Warehouse offers a picture framing service. The cost for framing a picture is made up of two parts: glass costs \$1 per square foot and the frame costs \$2 per linear foot. If the frame has to be a square, what size picture can you get framed for \$20?



Operations with Radical Expressions 5.2D

1. Simplify each expression.

a)
$$\sqrt{20}$$
 $\sqrt{4.5}$
 $2\sqrt{5}$

b)
$$\sqrt{48}$$

$$\sqrt{\cancel{6} \cdot \cancel{3}}$$

$$4 \sqrt{\cancel{3}}$$

c)
$$\sqrt{200}$$

e)
$$5\sqrt{24}$$

 $5\sqrt{4.6}$
 $5\cdot7\sqrt{6}$
 $10\sqrt{6}$

f)
$$6\sqrt{98}$$

 $6\sqrt{49\cdot 2}$
 $6\cdot 7\sqrt{2}$
 $42\sqrt{2}$

2. Add or subtract each expression.

a)
$$\left(5 - \sqrt{3}\right) + \left(4 + \sqrt{3}\right)$$

b)
$$(4+5\sqrt{2})+(2+6\sqrt{2})$$

b)
$$(4+5\sqrt{2})+(2+6\sqrt{2})$$
 c) $(6-8\sqrt{7})-(4+2\sqrt{7})$
 $(6+1)\sqrt{7}$ $(6-8\sqrt{7})-(4+2\sqrt{7})$

d)
$$8 - (3 + 5\sqrt{2})$$

e)
$$-2\sqrt{5} + (3 + \sqrt{5})$$

 $3 - \sqrt{5}$

f)
$$(6+5\sqrt{12})+(5-\sqrt{12})$$

 $11+4\sqrt{12}$
 $11+4\sqrt{4\sqrt{3}}$
 $11+4\sqrt{2}\sqrt{3}$
 $11+8\sqrt{3}$

5.2D Operations with Radical Expressions

- 3. Simplify each using two different methods.
 - a) $\sqrt{2} \cdot \sqrt{18}$

1 st method	2 nd method
√2·√18	√2.√18
√2·18	√2.√9.2
√36	√2.√9.√2
6	3.2=6

b) $\sqrt{8} \cdot \sqrt{2}$

1 st method	2 nd method
$ \sqrt{8} \cdot \sqrt{2} $ $ \sqrt{8} \cdot 7 $ $ \sqrt{6} $ $ 4 $	√8·√2 √4·2·√2 √4 √2·√2 2·2 4

4. Simplify each expression.

a)
$$\sqrt{5} \cdot \sqrt{5}$$

d)
$$3\sqrt{20} \cdot 2\sqrt{3}$$

 $6\sqrt{60}$
 $6\sqrt{4\cdot 15}$
 $6\cdot 2\sqrt{15}$
 $12\sqrt{15}$

f)
$$-2\sqrt{6} \cdot 3\sqrt{7}$$

 $-6\sqrt{42}$

5.2D Operations with Radical Expressions

5. Simplify each expression.

a)
$$5(3+\sqrt{7})$$
 $15+5\sqrt{7}$

b)
$$-3(2-\sqrt{3})$$

 $1-6+3\sqrt{3}$

c)
$$2(1+4\sqrt{3})$$

 $\sqrt{2+8\sqrt{3}}$

d)
$$\sqrt{5}(2+3\sqrt{2})$$

$$2\sqrt{5}+3\sqrt{10}$$

e)
$$-\sqrt{2}(3+\sqrt{18})$$

 $-3\sqrt{2}-\sqrt{3}6$
 $-3\sqrt{2}-6$ or $-6-3\sqrt{2}$

f)
$$-\sqrt{3}(5-\sqrt{8})$$

 $-5\sqrt{3}+\sqrt{24}$
 $\sqrt{4\cdot6}$
 $-5\sqrt{3}+2\sqrt{3}$

6. Simplify each expression.

a)
$$(4+\sqrt{3})(4+\sqrt{3})$$

 $/6+8\sqrt{3}+3$
 $19+8\sqrt{3}$

b)
$$2(3-\sqrt{2})^2$$

 $2(3-\sqrt{2})(3-\sqrt{2})$
 $2(9-6\sqrt{2}+2)$
 $2(11-6\sqrt{2})$
 $22-12\sqrt{2}$

b)
$$2(3-\sqrt{2})^2$$
 c) $5(2-\sqrt{3})^2+6(2-\sqrt{3})$
 $2(3-\sqrt{2})(3-\sqrt{2})$ $5(2-\sqrt{3})(2-\sqrt{3})+12-6\sqrt{3}$
 $2(9-6\sqrt{2}+2)$ $5(4-4\sqrt{3}+3)$ 1
 $2(11-6\sqrt{2})$ $5(7-4\sqrt{3})$
 $22-12\sqrt{2}$ $35-20\sqrt{3}+12-6\sqrt{3}$

d)
$$4(1+3\sqrt{2})(1+3\sqrt{2})$$

 $4(1+6\sqrt{2}+18)$
 $4(19+6\sqrt{2})$
 $76+24\sqrt{2}$

e)
$$3(4-2\sqrt{7})^2$$

 $3(4-2\sqrt{7})(4-2\sqrt{7})$
 $3(16-16\sqrt{7}+28)$
 $3(44-16\sqrt{7})$
 $132-48\sqrt{7}$

f)
$$3(2-\sqrt{11})^2-5(2-\sqrt{11})+7$$

 $3(2-\sqrt{11})(2-\sqrt{11})-10+5\sqrt{11}+7$
 $3(4-4\sqrt{11}+11)$
 $3(15-4\sqrt{11})$
 $45-12\sqrt{11}-3+5\sqrt{11}$
 $42-7\sqrt{11}$

5.2DOperations with Radical Expressions

7. Verify that the given answer (value of x) is a solution to the equation.

$$(3\sqrt{2})^{2} + 7 = 25; x = 3\sqrt{2}$$

$$(3\sqrt{2})^{2} + 7 = 25$$

b)
$$x^2 - 14x + 50 = 3$$
; $x = (6 + \sqrt{2})$ c) $(6 + \sqrt{2})(6 + \sqrt{2}) - 14(6 + \sqrt{2}) + 50 = 3$
 $36 + 13\sqrt{2} + 2 - 84 - 14\sqrt{2} + 50$
 $38 + 13\sqrt{2} - 84 - 14\sqrt{2} + 50$

7. Verify that the given answer (value of x) as $x = (6+\sqrt{2})$ c) $2x^2 - 20x = 40$; $x = (5-3\sqrt{5})$ (3\(\frac{1}{2}\)) + 7 = 25(6+\(\frac{1}{2}\))(6+\(\frac{1}{2}\)) $-14(6+\(\frac{1}{2}\)) <math>+50 = 3$ (6+\(\frac{1}{2}\))(6+\(\frac{1}{2}\))(6+\(\frac{1}{2}\)) $-14(6+\(\frac{1}{2}\)) <math>+50 = 3$ (6+\(\frac{1}{2}\))(6+\(\frac{1}{2}\))(6+\(\frac{1}{2}\)) $-14(6+\(\frac{1}{2}\)) <math>+50 = 3$ (8+\(\frac{1}{2}\))(8+\(\frac{1}\))(8+\(\frac{1}\))(8+\(\frac{1}\))(8+\(\frac{1}\))(8+\(\frac{

8. Simplify each expression.

a)
$$\frac{6a+15}{3}$$

2a+5

b)
$$\frac{6+15\sqrt{2}}{3}$$

c)
$$\frac{-14-10\sqrt{6}}{2}$$

d)
$$\frac{-25+15\sqrt{40}}{5}$$

 $-5+3\sqrt{40}$
 $3\sqrt{4.10}$
 $-5+6\sqrt{10}$

9. Verify that the given answer (value of x) is a solution to the equation.

$$2(\frac{3+\sqrt{57}}{4})^{2} - 3(\frac{3+\sqrt{57}}{4})^{2} - 6 = 0$$

$$\frac{9+6\sqrt{57}+57}{16}$$

$$\frac{66+6\sqrt{57}}{16}$$

$$2(\frac{33+3\sqrt{57}}{4})^{2} - \frac{9-3\sqrt{57}}{4}$$

$$\frac{33+3\sqrt{57}}{4} - 6 = 0$$

$$\frac{34-3\sqrt{57}}{4} - 6 = 0$$

Section 5.2D

5.2E Solve Quadratic Equations Using Square Roots to Find Rational Solutions

#1-6: Solve each equation using the square root property and check each answer.

$$\begin{array}{c}
1. \sqrt{x^2} \sqrt{4} \\
|x| = 2 \\
(x = \pm 2)
\end{array}$$

✓ Verify your solution(s):

2.
$$2a^{2} = 32$$
 $\sqrt{a^{3}} = \sqrt{6}$
 $|a| = 4$
 $(a = \pm 4)$
 $2(4) = 2(6) = 32$
 $2(-4)^{2} = 2(6) = 32$

✓ Verify your solution(s):

3.
$$3m^2-8=67$$

$$3m^3=75$$

$$\sqrt{m^2}=\sqrt{25}$$

$$/m/=5$$

$$(m=\pm 5)$$

$$3(5)^2-8$$

$$75-8=67$$

√ Verify your solution(s):

4.
$$\sqrt{(x-1)^2} \neq 36$$

 $|x-1| = 6$
 $|x-1| = 6$
 $|x-1| = 6$
 $|x-1| = 6$
 $|x-1| = 6$

5.
$$(x+3)^2 - 16 = 0$$

$$\sqrt{(x+3)^2} = \sqrt{6}$$

$$|x+3| = 4$$

$$x+3 = 4 \text{ or } x+3 = -4$$

$$x=1 \text{ or } x=-7$$

4.
$$\sqrt{(x-1)^2} \neq 36$$

$$|x-1| = 6$$

$$|x-1| = 6$$

$$|x-1| = 6$$

$$|x+3| = 4$$

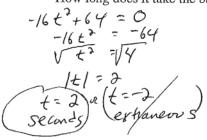
$$|x+3| = 4$$

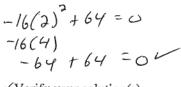
$$|x+3| = 7$$

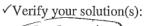
Verify your solution(s): $\sqrt{\text{Verify your solution(s)}}$: $(7-1)^2 = 36$ $(3^2 = 36)$ $(-5-1)^2 = 36$ $(-5-1)^2 = 36$ $(-6)^3 = 36$ $(-6)^3 = 36$ $(-6)^3 = 36$ $(-6)^3 = 36$ $(-6)^3 = 36$ $(-7+3)^2 - 16 = 0$

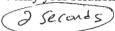
5.2E. Solve Quadratic Equations Using Square Roots to Find Rational Solutions

7. A physics teacher drops an object from an initial height of 64 feet. The height of the ball (in feet) h at time t (in seconds) can be modeled by the equation $h(t) = -16t^2 + 64$. How long does it take the ball to reach the ground?











8. The stopping distance "d" (in meters) that a car needs to come to a complete stop when traveling at speed "x" (in km/h) can be modeled by the equation $d = 0.009(x+15)^2 + 3$. On a certain road, drivers cannot see a stop sign until they are approximately 20 meters away. What is the maximum speed that should be posted in order to allow cars enough room to stop in time? Round your answer to the nearest whole number and verify your solution.



$$20 = 0.009(x+15)^{3} + 3$$

$$17 = 0.009(x+15)^{2}$$

$$0.009 \quad 0.009$$

$$\sqrt{1888.8} = \sqrt{(x+15)^{2}}$$

$$43.4613 = |x+15|$$

$$x+15=43.4613 \text{ or } x+15=-43.4613$$

$$x \approx 58 \text{ exhaneous}$$

9. A missing leg of a right triangle can be found using the Pythagorean Theorem: $a^2 + b^2 = c^2$, where "a" and "b" are the legs of the triangle and "c" is the hypotenuse of the triangle (the side directly across from the right angle). Andy is trying to find the missing leg of the triangle below that represents the distance that the person is from a flagpole. The flag pole is 12 feet tall and he knows that the distance from the person to the top of the flagpole is 15 feet. Andy has started the problem by putting the values into the formula. Help him find the solution.

$$a^{2}+b^{2}=c^{2}$$

$$(12)^{2}+b^{2}=(15)^{2}$$

$$144+b^{2}=225$$

$$151=9$$

$$1211.$$
Then leg in 9 ft

Section 5.2E

5.2F Solve Quadratic Equations Using Square Roots to Find Real Solutions

On a quiz, Omar solved a quadratic equation and got the answer wrong. His work is shown below. Identify 1. his mistake and then solve the equation correctly to find the real solution.

$$\sqrt{(x-3)^2} = 3$$

$$(x-3) = 3$$

$$x-3=3 \text{ or } x-3=3$$

$$x=6 \text{ on } x=0$$

12)
$$2(x-3)^2 = 18$$

$$2 \qquad 2$$

$$(X-3)^2 = 9$$
every $+3 + 3$

$$\sqrt{X^2} = \sqrt{12}$$

$$\chi = 3.464, -3.464$$

#2 - 5: Verify that each of the following values are solutions to the given equation. Show ALL of your work.

2.
$$2x^2+3=21$$
; $x=3, x=-3$
 $2(3)^2+3=21$ $2(-3)^2+3=21$
 $2(9)+3$
 $2(9)+3=21$ $2(9)+3=21$

3.
$$(x-5)^2+1=17$$
; $x=9, x=1$
 $(9-5)^2+1=17$ $(1-5)^2+1=17$
 $(4)^2+1$
 $(6+1)^2+1$
 $(6+1)^2+1$
 $(6+1)^2+1$

4.
$$x^{2}+7=35$$
; $x=2\sqrt{7}, x=-2\sqrt{7}$
 $(2\sqrt{7})^{3}+7=35$ $(-2\sqrt{7})^{3}+7=35$
4.7
 $28+7=35$ 4.7
 $28+7=35$

4.
$$x^{2}+7=35$$
; $x=2\sqrt{7}, x=-2\sqrt{7}$
5. $(x+3)^{2}-5=70$; $x=-3+\sqrt{5}, x=-3-\sqrt{5}$

$$(2\sqrt{7})^{2}+7=35$$

$$(-2\sqrt{7})^{2}+7=35$$

$$(-3+\sqrt{5})+3)^{2}-5=70$$

5.2F Solve Quadratic Equations Using Square Roots to Find Real Solutions

- Samantha solved the following problem on a test and got the right answer. Unfortunately, she doesn't know 6. which answer is the actual solution. Explain to her which solution is correct and why.
 - 5) The height "h" of a water balloon (in feet) at time "x" (in seconds) is given by the equation. $h(x) = -16(x - 0.65)^2 + 10$. If a student throws the balloon and it hits a student who is 6 feet tall in the head, how long was the balloon in the air?

$$6 = -16(\times -0.65)^2 + 10$$

-10

$$-4 = -16 (\times -0.65)^2$$

$$\sqrt{0.25} = \sqrt{(X - 0.65)^2}$$

$$0.5 = X - 0.65$$

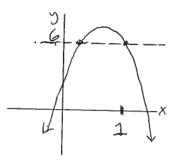
Not sure which is

right???

X = 1.15 seconds or X = 0.15 seconds

HELP!

Both answers are correct. The balloon could have hit a 6 ft tall student on the way up after 0.15 seconds, or it could have hit the student on its descending path after 1-15 seconds. See graph at right.



#7 - 10: Solve each equation for real solutions and simplify your answers. Verify your solutions!

7.
$$\frac{x^2 + 3 = 21}{\sqrt{x^2 = \sqrt{18}}}$$
 $(3\sqrt{2}) + 3$ $(3\sqrt{2}) + 3 = 31$ $(3\sqrt{2})^3 + 3$ $(3\sqrt{2}$

8.
$$\sqrt{(x-1)^2} = 32$$

 $|x-1| = \sqrt{16 \cdot 3}$

√ Verify your so ution(s):

Verify your solution(s)
$$\left(\left(1+4\sqrt{2}\right)-1\right)^{\frac{1}{2}}=32$$

Verify your solution(s):
$$((1-4\sqrt{2})-1)^2 = 32$$

 $((1+4\sqrt{2})^2-1)^2 = 32$
 $(4\sqrt{2})^2 = 32$
 $(-4\sqrt{2})^2 = 32$
 $(6\cdot 2)^2 = 32$

5.2F Solve Quadratic Equations Using Square Roots to Find Real Solutions

#7 - 10 (continued): Solve each equation for real solutions and simplify your answers. Verify your solutions!

9.
$$2x^{2}-8=0$$

$$\sqrt{2x^{3}} = 8$$

$$\sqrt{x} + \sqrt{4}$$

$$\sqrt{x} = 2$$

$$\sqrt{x} = 2$$

10.
$$5(x-1)^2-3=42$$

$$5(x-1)^2=45$$

$$\sqrt{(x-1)^2}=\sqrt{9}$$

$$|x-1|=3$$

$$x-1=3 \text{ or } x-1=-3$$

$$+(-+)$$

$$X=4 \text{ or } x=-2$$

✓ Verify your solution(s):

✓ Verify your solution(s):
$$5(4-1)^3-3$$
 $5(-2-1)^3-3=44$ $5(3)^3-3$ $5(-3)^3-3$ $5(-3)^3-3$ $5(-3)^3-3$

#11 - 14: Find the roots of each function and simplify your answers. Verify your solutions!

11.
$$f(x)=x^2-75$$

 $x^3-75=0$
 $\sqrt{x^3+75}$
 $|x|=\sqrt{35\cdot 3}$
 $|x|=\pm 5\sqrt{3}$

12.
$$f(x) = (x+2)^{2}$$

$$\sqrt{(x+2)^{3}} = \sqrt{0}$$

$$|x+2| = 0$$

$$x+2 = 0$$

$$x = -2$$

$$x = -2$$

Verify your solution(s):

$$(5\sqrt{3})^{2}-75=0$$

$$25.3-75=0$$

$$(-5\sqrt{3})^{2}$$

$$25.3-75=0$$

5.2F Solve Quadratic Equations Using Square Roots to Find Real Solutions

#11 - 14 (continued): Find the roots of each function and simplify your answers. Verify your solutions!

13.
$$f(x) = 2(x-1)^2 - 18$$

 $2(x-1)^2 - 18 = 0$
 $2(x-1)^3 = 18$
 $(x-1)^3 = 9$
 $(x-1)^3 = \sqrt{9}$
 $(x-1)^3 = \sqrt{9}$
 $(x-1) = 3$
 $(x-1) = 3$

14.
$$f(x) = 3x^{2} - 24$$

$$3x^{2} - 24 = 0$$

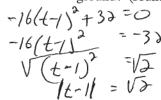
$$3x^{2} = 34$$

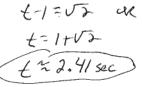
$$\sqrt{x^{2}} = \sqrt{8}$$

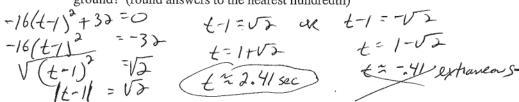
$$1x1 = 2\sqrt{2}$$

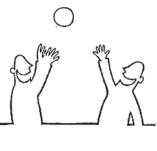
$$x = \pm 2\sqrt{2}$$

15. The height of a ball in the air, h, at time t can be modeled by the equation $h(t) = -16(t-1)^2 + 32$. How long does it take for the ball to reach the ground? (round answers to the nearest hundredth)

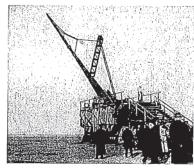








16. Big Bertha, a cannon used in WW1, could fire shells incredibly long distances. The page of a shell could be modeled by $y = -0.0196(x-25)^2 + 12$ where x was the horizontal distance traveled (in miles), and y was the height (in miles). How far could Big Bertha fire a shell? (round answers to the nearest mile)



Big Bertha (Paris Gun), courtesy http://www.militaryimages.net

 $\begin{array}{c} -0.0196(x-25)^{2} + 12 = 0 \\ -0.0196(x-25)^{2} = 72 \\ \sqrt{(x-25)^{2}} = \sqrt{612.245} \end{array}$ -0.0196 (x-25) +12

612.245	
94.74	
x-25 = -24.74 +25 = 0.26 = 0	mles
Section 5.2F) extraneus

5.2G Operations with Complex Expressions

1. Simplify each expression.

a)
$$i^2 = -1$$

b)
$$i^4 = 1$$

c)
$$i^{17} = L$$

d)
$$-i^{10} = (-1) = 1$$

e)
$$i^{101} = \dot{\nu}$$

h)
$$4\sqrt{-9}$$
 $4(3i) = 10i$

i)
$$5\sqrt{-28}$$

 $5i\sqrt{4.7}$
 $5i2.\sqrt{7} = |10i\sqrt{7}|$

1)
$$5\sqrt{-100}$$

 $5L\sqrt{100} = 50L$

2. Add or subtract each expression.

a)
$$(5-3i)+(4+7i)$$
 $(9+4i)$

b)
$$(4-8i)+(9+2i)$$

c)
$$(3-2i)-(5-4i)$$

 $-2+2i$

d)
$$6 - (-5 - \sqrt{-9})$$

e)
$$8i + (9-11i)$$

f)
$$(7-\sqrt{-81})+(5-\sqrt{-100})$$

 $7-9i+5-10i$
 $12-19i$

3. Simplify each expression.

a)
$$3i \cdot 2i$$

 $6(-1) = -6$

c)
$$4\sqrt{-6.2\sqrt{3}}$$

 $4iV6.2\sqrt{3}$
 $8iV18$
 $8iV9.2$
 $8i3.V2$ = $24iV2$

d)
$$-3\sqrt{-20\cdot 2\sqrt{5}}$$

 $-62\sqrt{9\cdot 5}\cdot \sqrt{5}$
 $-62\cdot 2\cdot 5 = -60\dot{c}$

e)
$$8\sqrt{-2} \cdot 3\sqrt{2}$$
 $24i\sqrt{2}\sqrt{2} = \boxed{48i}$

f)
$$-2\sqrt{-6} \cdot 3\sqrt{-3}$$

 $-6i\sqrt{6}i\sqrt{3}$
 $-6i^{2}\sqrt{18}$
 $-6(-1)\sqrt{9} \cdot 2$
 $6\cdot 3\sqrt{2}$

5.2G Operations with Complex Expressions

4. Kasem simplified the expression $\sqrt{-4}$ $\sqrt{-9}$ using various methods.

1 WRONG	2 CORRECT	3 CORRECT
Line 1 $\sqrt{-4} \cdot \sqrt{-9}$	Line 1 $\sqrt{-4} \cdot \sqrt{-9}$	Line 1 $\sqrt{-4} \cdot \sqrt{-9}$
Line 2 $\sqrt{-4 \cdot -9}$	Line 2 $\sqrt{-1\cdot 4}\cdot \sqrt{-1\cdot 9}$	Line 2 $\sqrt{-1\cdot4}\cdot\sqrt{-1\cdot9}$
Line 3 $\sqrt{36}$	Line 3 $\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{-1} \cdot \sqrt{9}$	Line 3 $\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{-1} \cdot \sqrt{9}$
Line 4 6	Line 4 $\sqrt{-1} \cdot \sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{9}$	Line 4 $i \cdot 2 \cdot i \cdot 3$
	Line 5 $i \cdot i \cdot \sqrt{4 \cdot 9}$	Line 5 $2 \cdot 3 \cdot i \cdot i$
	Line 6 $i^2 \cdot \sqrt{36}$	Line 6 $6 \cdot i^2$
	Line 7 (-1)6	Line 7 $6 \cdot (-1)$
	Line 8 –6	Line 8 –6

a) Other than simplifying to the different numeric values, identify 2 or more differences in the process

1) In method 1, Kasem never used the definition of i=V-I to rewrite either vadical

2) Method I used the product property of radicals incorrectly;
only if a and b are BoTH nonnegative with an even index, is VaVb = Vab
method 2 used the product property of radicals correctly.
b) Although the methods have created different numeric values when simplifying, identify 2 or more

similarities in the process shown in methods 1 and 2.

1) Both methods combined $\sqrt{4.9} = \sqrt{36}$ instead of simplifying each separately

2) Both networds used fact that V36 = 6

c) Although the methods have created the same numeric value, identify 2 or more differences in the process

1) From line 3 to line 4, multiplication was done in a different order by commutative property for multiplication.

2) Method 3 simplified the vadicals V4 and V9; method 2 miltiplied them together.

d) Other than simplifying to the same numeric values, identify 2 or more similarities in the process shown in methods 2 and 3.

1) Both used definition of i= V-1 wherever there was a V-1,

2) Both used fact that i = -1

5. Simplify each expression.

a) $\sqrt{-6} \cdot \sqrt{-2}$ 106.212 **b**) $3\sqrt{-5} \cdot 2\sqrt{-8}$ 61V5 LV4.3

Operations with Complex Expressions 5.2G

Simplify each expression.

a)
$$5(1-3i)$$

b)
$$3(3+i)$$
 $9+3c$

c)
$$3(2-4\sqrt{-25})$$

 $6-12\sqrt{-1.25}$
 $6-12\sqrt{-1.25}$
 $6-12\sqrt{-5}$

e)
$$-5i(-8+2i)$$

 $40i - 10(i^{2})$
 $40i - 10(-1)$
 $10 + 40i$

f)
$$\sqrt{-10}(2-\sqrt{-2})$$

 $i\sqrt{10}(2-i\sqrt{2})$
 $2i\sqrt{10}-i^{2}\sqrt{20}$
 $2i\sqrt{10}-(-1)2\sqrt{5}$
 $2i\sqrt{10}+2\sqrt{5}$
 $2\sqrt{5}+2i\sqrt{10}$

7. Simplify each expression.

a)
$$(3+5i)(3+5i)$$
 2
 $9+30i+25i$
 $9+30i-25$
 $-160+30i$

b)
$$3(4-2i)^2$$

 $3(16-16i+4i)^2$
 $3(16-16i-4)$
 $3(12-16i)$
 $36-48i$

c)
$$(5-3i\sqrt{2})^2$$

 $25-30i\sqrt{2}+9.2i^2$
 $25-30i\sqrt{2}-18$
 $7-30i\sqrt{2}$

8. Simplify each expression.

a)
$$4(1+3i\sqrt{2})(1+3i\sqrt{2})$$

 $4(1+6i\sqrt{2}+9i^{3}2)$
 $4(1+6i\sqrt{2}-18)$
 $4(-1)+6i\sqrt{2}$
 $-68+24i\sqrt{2}$

b)
$$3(4-2i\sqrt{7})^2$$
 c) $3(2-i\sqrt{11})^2-5(2-i\sqrt{11})+7$
 $3(16-16i\sqrt{7}+4i^2.7)$ $3(4-4i\sqrt{11}-11)$
 $3(16-16i\sqrt{7}-28)$ $3(4-4i\sqrt{11}-11)$
 $3(-12-16i\sqrt{7})$ $3(-7-4i\sqrt{11})$
 $-36-48i\sqrt{7}$ $-21-12i\sqrt{11}$ $-10+5i\sqrt{11}$

5.2G Operations with Complex Expressions

9. Verify that the given answer (value of x) is a solution to the equation.

a)
$$-2x^{2}+6=56$$
; x
 $-2(52)^{2}+6=56$
 $-2(252)^{2}$
 $-3(-25)^{2}$
 $-3(-25)^{2}$

a)
$$-2x^{2}+6=56$$
; $x=5i$ b) $x^{2}-8x+30=5$; $x=(4+3i)$ c) $x^{2}-2x+48=2$; $x=(1-3i\sqrt{5})$
 $-2(5i)+6=56$ $(4+3i)^{2}-8(4+3i)+30=5$ $(1-3i\sqrt{5})^{2}-2(1-3i\sqrt{5})+48=2$
 $-2(35i^{2})$ $(6+34i+9i^{2})$ $(6+34i-9)$ $(6+34i-9)$

10. Simplify each expression (no decimal values allowed).

a)
$$\frac{6+8i}{2}$$

$$\int 3+4\dot{c}$$

b)
$$\frac{6+10i\sqrt{2}}{2}$$

c)
$$\frac{-15-21i\sqrt{6}}{3}$$

$$\sqrt{-5-7}$$

$$V-1.25.3$$
d)
$$\frac{-30+\sqrt{-75}}{5}$$

$$-30+5i\sqrt{3}$$

$$5$$

$$-6+i\sqrt{3}$$

11. Verify that the given answer (value of x) is a solution to the equation,

$$2x^{2}-6x+8=3; x=\frac{3+i}{2}$$

$$2(\frac{3+i}{2})^{2}-6(\frac{3+i}{2})+8=3$$

$$2(\frac{9+6i+i^{2}}{4})-3(3+i)+8$$

$$2(\frac{8+6i}{4})-9-3i+8$$

$$\frac{8+6i}{4}$$

$$4+3i-1-3i$$

$$3=3$$

Section 5.2G

5.2H Solve Quadratic Equations Using Square Roots to Find Real or Complex Solutions

#1-6: Simplify the following radicals.

1.
$$\sqrt{-9}$$

3.
$$2\sqrt{-3}$$

4.
$$3\sqrt{-100}$$

7. What is the value of i^2 ?

#8-13: Simplify the following complex expressions.

8.
$$(3i)^2$$

$$92^2$$

$$|-9|$$

9.
$$(-5i)^2$$

$$\frac{25i}{1-25}$$

10.
$$(-i)^2$$

$$\downarrow^2 =$$

11.
$$(3-5i)^2$$

$$9-30£ + 25£$$

$$9-30£ -25$$

$$1-16-30£$$

13.
$$(-2-7i)^2+5$$

 $4+28i+49i^2+5$
 $4+38i-49+5$
 $1-40+28i$

#14-17: Verify that each of the following values are solutions to the given equation. Show all of your work.

work.
14.
$$-2x^2 + 3 = 21$$
; $x = 3i, x = -3i$
 $-2(3i)^3 + 3 = 21$
 $-2(9i)^2$
 $-3(9i)^3 + 3 = 21$
 $-2(-3i)^3 + 3 = 21$
 $-2(9i)^3$
 $-18i^3$
 $-18i^3$
 $-18i^3$
 $-18i^3$

15.
$$(x-5)^2 - 1 = -17$$
; $x = 5 + 4i$, $x = 5 - 4i$
 $((5+4i)-5)^2 - 1 = -17$
 $(4i)^3$
 $(6i)^3$
 $-16 - 1 = -17$
 $(-4i)^2 - 1$
 $(6i)^3$
 $-16 - 1 = -17$

5.2H Solve Quadratic Equations Using Square Roots to Find Real or Complex Solutions

#14-17 (continued): Verify that each of the following values are solutions to the given equation. Show all of your work.

16.
$$x^{2}+11=7$$
; $x=2i, x=-2i$
 $(2i)^{3}+11=7$
 $4i^{2}+11$
 $4(-1)^{2}+11=7$
 $(-2i)^{3}+11=7$
 $(-4)^{2}+11=7$

17.
$$(x+2)^2 = -25$$
; $x = -2+5i$, $x = -2-5i$

$$((-2+5i)+2)^2 = -25$$

$$(5i)^2$$

$$25(-1) = -25$$

$$(-2-5i)^2$$

$$25(-1) = -25$$

$$(-5i)^2$$

$$25(-1) = -25$$

#18 – 21: Solve each equation for real or complex solutions. Verify your solutions.

18.
$$x^{2} + 3 = 51$$

$$\sqrt{X^{3} + 48}$$

$$/ \times / = \sqrt{16.3}$$

$$\sqrt{X} = \frac{1}{4} = \sqrt{3}$$

19.
$$\sqrt{(x-1)^2} = \sqrt{-24}$$
 $|x-1| = \sqrt{-1 \cdot 4 \cdot 6}$
 $|x-1| = \sqrt{-1 \cdot 4 \cdot 6}$

Verify your solution(s):

$$(4\sqrt{3})^{2} + 3 = 51$$

 $16.3 + 3 = 51$
 $(-4\sqrt{3})^{2} + 3$
 $16.3 + 3 = 51$

Verify your solution(s):
$$\left(\left(1+\frac{2i\sqrt{6}}{5}\right)^{-1}\right)^{2} = -\frac{34}{54}$$

$$\left(\frac{2i\sqrt{6}}{5}\right)^{2}$$

$$4i^{2}.6$$

$$34(4) = -34$$

$$\left(\left(1-\frac{2i\sqrt{6}}{5}\right)^{-1}\right)^{2} = -34$$

$$\left(-\frac{2i\sqrt{6}}{5}\right)^{2}$$

$$4i^{2}.6$$

$$34(4) = -34$$

Solve Quadratic Equations Using Square Roots to Find Real or Complex Solutions

#18 - 21 (continued): Solve each equation for real or complex solutions. Verify your solutions.

20.
$$3x^{2}-27=0$$

$$3x^{2}=27$$

$$\sqrt{x^{2}}=\sqrt{9}$$

$$/x = 3 \text{ or } x = -3$$

21.
$$5(x+1)^{2} - 3 = -48$$

 $+3$
 $5(x+1)^{2} = -45$
 $(x+1)^{2} = \sqrt{-9}$
 $/x+1/=3i$
 $x+1=\pm 3i$
 $x=-/+3i$, $x=-/-3i$

✓ Verify your solution(s):

$$3(3)^{3}-27=0$$

 $3(-3)^{2}-27$
 $3(-3)^{2}-27$
 $3(-3)^{2}-27=0$

Verify your solution(s):

$$5((-1+3i)+1)^{2}-3=-48$$

 $5(3i)^{2}$
 $5(9i)^{2}$
 $45i^{2}$
 $-45-3=-48$

Verify your solution(s):

$$5((-1+3i)+1)^{2} - 3 = -48$$

$$5((-1-3i)+1)^{2} - 3 = -48$$

$$5(3i)^{2}$$

$$5(-3i)^{2}$$

$$5(-3i)^{2}$$

$$5(-3i)^{2}$$

$$45i^{2}$$

$$-45^{2} - 3 = -48$$

22. The height, h, of a water balloon (in feet) at time t (in seconds) is given by the equation

 $h(t) = -16(t - 0.45)^2 + 32$. If a student throws the balloon and it lands on the ground, how long is the balloon in the air? Verify your solution(s). $= -16(1.86 - .45)^2 + 32 = 0$ Verify your solution(s). $= -16(1.86 - .45)^{2} + 32 = 0$ $(1.41)^{2}$ -16(1.9881) + 32 $(1.41)^{3}$ -16(1.9881) + 32 (1

23.
$$f(x) = x^2 - 125$$

 $x^2 - 125 = 6$
 $\sqrt{x^2 - 1/25}$
 $/x = \sqrt{5} = 5$
 $/x = 5\sqrt{5}$ or $x = -5\sqrt{5}$

24.
$$f(x) = (x+7)^{2}$$

$$\sqrt{(x+7)^{2}} = \sqrt{0}$$

$$/x+7/=0$$

$$x+7=0$$

$$x=-7$$

$$(5\sqrt{5})^{2} - 1 + 5 = 0 \qquad (-5\sqrt{5})^{2} - 1 + 5 = 0$$

$$25.5 = 1 + 5 = 0$$

$$25.5 = 1 + 5 = 0$$

$$25.5 = 0$$

$$25.5 = 0$$

$$0^{2} = 0$$

$$0^{2} = 0$$

Verify your solution(s):
$$(-7 + 7)^2 = 0$$

5.2H Solve Quadratic Equations Using Square Roots to Find Real or Complex Solutions

#23 - 26 (continued): Find the real and/or complex roots of each function. Verify your solutions!

25.
$$f(x) = -2(x-2)^{2} - 18$$

$$-2(x-2)^{2} - 18 = 0$$

$$-2(x-2)^{2} = 18$$

$$\sqrt{(x-2)^{2}} = \sqrt{-9}$$

$$|x-2| = 3i$$

$$x - 2 = \pm 3i$$

$$\sqrt{2}$$

$$\sqrt{2}$$
Verify your solution(s):

26.
$$f(x) = 4x^{2} + 24$$

$$4x^{2} + 34 = 0$$

$$4x^{2} = -34$$

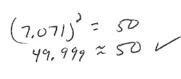
$$1 \times 1 = -2\sqrt{6}$$

$$1 \times 1 = -2\sqrt{6}$$

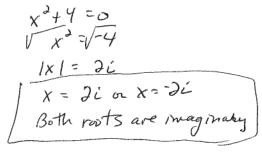
$$1 \times 1 = -2\sqrt{6}$$

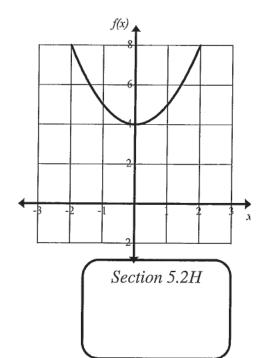
Verify your solution(s): $-2(\frac{3+3(-\lambda)^{2}-18}{2} = 0$ $-2(\frac{3+3(-\lambda)^{2}-18}{2} = 0$

27. The area of a square can be found using the formula $A = s^2$, where "A" is the area and "s" is the length of one side. If the area of a square is 50 square inches, what is the length of one side? Round your answer to the nearest thousandth and verify your solution(s).



The function $f(x) = x^2 + 4$ has no x-intercepts, as shown in the graph to the right. Use algebra to show that no real roots exist for





Solving Quadratic Equations by Completing the Square to Find Rational Solutions

#1 - 3: Solve using square roots.

1.
$$\sqrt{(x-2)^2} \neq 25$$

 $|x-2| = 5$
 $x-2 = 5 \text{ or } x-3 = -5$
 $x = 7 \text{ or } x = -3$

2.
$$\sqrt{(x+4)^2} \neq 16$$

 $|x+4| = 4$
 $x+4 = 4$ $x+4 = -4$
 $|x=0| \propto |x=-8|$

$$|X - 2|^{2} \neq 25$$

$$|X - 2| = 5$$

$$|X + 4| = 4$$

$$|X - 2| = 5 \text{ or } x - 3 = -5$$

$$|X = 7 \text{ or } x = -3|$$

$$|X = 7 \text{ or } x = -3|$$

$$|X = 7 \text{ or } x = -4|$$

$$|X = 7 \text{ or } x = -4|$$

$$|X = 7 \text{ or } x = -4|$$

$$|X = 7 \text{ or } x = -4|$$

$$|X = 7 \text{ or } x = -4|$$

Find and explain the error made when solving the following equation. $x^2 + 10x = 24$

#5 – 6: Fill in the missing value to create a perfect square trinomial. Then solve by Completing the Square.

5.
$$40 + \frac{9}{9} = x^2 + 6x + \frac{9}{9}$$

$$7 = (x+3)$$

$$\frac{x+3-7}{x-4} \text{ or } \frac{x+3-7}{x-2}$$

$$47 - 10: \text{ Solve by } \frac{Completing the Square}{x}. \text{ Then verify your solutions.}$$

6.
$$x^2 - 18x + 81 = 88 + 81$$

 $\sqrt{(x-9)^2}$ $\sqrt{(69)^2}$
 $\sqrt{(x-9)^2}$ $\sqrt{(69)^2}$
 $\sqrt{(x-9)^2}$ $\sqrt{(69)^2}$
 $\sqrt{(79)^2}$ $\sqrt{(79)^2}$
 $\sqrt{(79)^2}$ $\sqrt{(79)^2}$

#7-10: Solve by Completing the Square. Then verify your solutions.

7.
$$29 = x^2 + 28x + 1/96$$
 $(1) + 38(1) = 39$ 8. $x^2 - 10x - 56 = 0$ Checks:

 $1/96 = 1/96 =$

I CAN REPRESENT REAL-WORLD SITUATIONS WITH QUADRATIC EQ APPROPRIATE METHODS. FIND REAL AND NON-REAL COMPLEX ROOTS WHEN THEY EXIST. RECOGNIZE THAT A PARTICULAR SOLUTION MAY NOT BE APPLICABLE IN THE ORIGINAL CONTEXT.

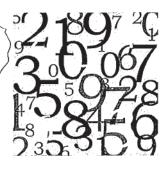
Solving Quadratic Equations by Completing the Square to Find Rational 5.2ISolutions

11. The product of two consecutive positive even integers is 528. What are the numbers?

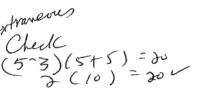
(Solve by Completing the Square)

Let $n = Smaller \ d \ 2 \ pos. ints$ ntd = pext consecutive pos int n(ntd) = 5d8 $n^2 + dn + 1 = 5d8 + 1$ $n^2 + dn + 1 = 5d8 + 1$ $n^2 + dn + 1 = 5d9$ What are the square)

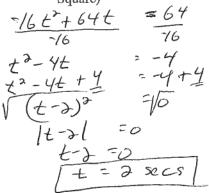
Let $n = Smaller \ d = Smaller \ d$



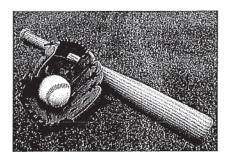
12. A square garden is altered so that one dimension is decreased by 3 yards, while the other dimension is increased by 5 yards. The area of the resulting rectangle is 20 square yards. Find the length of each side of the original garden and its area. (Solve by Completing the Square)



13. A foul ball leaves the end of a baseball bat and travels according to the formula $h(t) = -16t^2 + 64t$ where h is the height of the ball in feet and t is the time in seconds. How long will it take for the ball to reach a height of 64 feet in the air? (Solve by Completing the Square)







Section 5.21

5.2J Solving Quadratic Equations by Completing the Square to Find Real Solutions

#1 - 3: Solve using square roots.

1.
$$\sqrt{(x+7)^2} = \sqrt{15}$$
 $\sqrt{(x+7)^2} = \sqrt{15}$
 $\sqrt{(x+7)^2} = \sqrt{15}$
 $\sqrt{(x+7)^2} = \sqrt{15}$
 $\sqrt{(x-9)^2} = \sqrt{12}$
 $\sqrt{(x-9)^2} = \sqrt{12}$

2.
$$\sqrt{(x-9)^2} \neq \sqrt{12}$$
 $|x-9| = 2\sqrt{3}$
 $|x-9| = \pm 2\sqrt{3}$
 $|x-9| = 2\sqrt{3}$

3.
$$\sqrt{32} \Rightarrow (x-5)^{2}$$

$$/(x-5) = 4\sqrt{2}$$

$$x-5 = \pm 4\sqrt{2}$$

$$x = 5 \pm 4\sqrt{2}$$

#4-5: Fill in the missing value to create a perfect square trinomial. Then solve by <u>Completing the Square</u>.

4.
$$7 + \frac{25}{4} = x^2 + 5x + \frac{25}{4}$$

$$\frac{28}{4} + \frac{25}{4} = (x + 5)^2$$

$$\sqrt{\frac{53}{4}} = \sqrt{(x + 5)^2}$$

$$\sqrt{\frac{53}{4}} = \sqrt{x + 5}$$

$$\pm \sqrt{53} = x + 5$$

$$\sqrt{x - 5 \pm \sqrt{53}}$$

5.
$$x^2 - 7x + \frac{7}{4} = -3 + \frac{7}{4}$$

 $(x - \frac{7}{2})^2 = \frac{17}{4} + \frac{49}{4}$
 $(x - \frac{7}{2})^2 = \sqrt{\frac{37}{4}}$
 $(x - \frac{7}{2})^2 = \pm \frac{\sqrt{37}}{4}$
 $(x - \frac{7}{2})^2 = \pm \frac{\sqrt{37}}{3}$
your solutions

#6-9: Solve by <u>Completing the Square</u>. Then verify your solutions.

[See next page]
7. $2x^2-7x-13=-10$

6.
$$-88 = x^2 + 28x + 196$$

 $\sqrt{108} = \sqrt{(x + 14)^2}$
 $6\sqrt{3} = \sqrt{(x + 14)}$
 $\pm 6\sqrt{3} = x + 14$
 $\sqrt{x} = -14 \pm 6\sqrt{3}$

8.
$$8 = 4x^{2} + 4x - 13$$

$$21 = 4x^{2} + 4x$$

$$\frac{21}{4} = x^{2} + x$$

$$21 = x^{2} + x$$

$$1 = x^{2} + x + 3$$

$$21 = x + 3$$

$$22 = x + 3$$

$$23 = x + 3$$

$$24 = x + 3$$

$$25 = x + 3$$

$$27 =$$

When y 70, there will be a real solutions. when y = 0, there will be I real solution. P-35 Checks

$$| f | = 58 | Cheques$$

$$| f | = 88 = x^{2} + 28x | Verifying x = 74 ± 6V3$$

$$-88 = (74 + 6V3)^{2} + 28(-14 + 6V3)$$

$$= (196 - 168V3 + 108)$$

$$= 304 - 168V3 - 392 + 168V3$$

$$-88 = -88$$
Also
$$-88 = (-14 - 6V3)^{2} + 28(-14 - 6V3)$$

Also $-88 = (-14 - 6\sqrt{3})^{2} + 28(-14 - 6\sqrt{3})$ $= 196 + 168\sqrt{3} + 108$ $= 304 + 168\sqrt{3} - 392 - 168\sqrt{3}$ $-88 = -88 \checkmark$

#7
$$\left[\frac{2x^2-7x-13}{2x^2-7x-13} = 70\right]$$
 Verifying $x = \frac{7\pm\sqrt{73}}{4}$
 $2\left(\frac{7+\sqrt{73}}{4}\right)^3 - 7\left(\frac{7+\sqrt{73}}{4}\right) - 13 = 70$
 $2\left(\frac{49+14\sqrt{73}+73}{16}\right)$
 $\frac{12\lambda+14\sqrt{73}}{8}$
 $\frac{61+7\sqrt{73}}{4} - \frac{49-7\sqrt{73}}{4}$
 $\frac{12}{4}$ $\frac{13}{4}$ $\frac{13}$

$$A(S) = \frac{3}{2(\frac{7-\sqrt{73}}{4})^2 - 7(\frac{7-\sqrt{73}}{4}) - 13} = 70$$

$$2(\frac{49-14\sqrt{73}+73}{16})$$

$$122-14\sqrt{73}$$

$$61-7\sqrt{73} - 49+7\sqrt{73}$$

$$\frac{14}{3}$$
 -13 = 70 ν

P-35 checks

#8
$$[4x^{2} + 4x - 13 = 8]$$
 Verifying $x = \frac{-1 \pm \sqrt{2}x^{2}}{2}$
 $4(\frac{-1 + \sqrt{2}x^{2}}{2})^{2} + 4(\frac{-1 + \sqrt{2}x^{2}}{2}) - 13 = 8$
 $4(\frac{1 - 2\sqrt{2}x + 22}{4})$
 $23 - 2\sqrt{2}x - 2 + 2\sqrt{2}x - 13$
 $21 - 13 = 8$
 $4(\frac{-1 - \sqrt{2}x^{2}}{2})^{2} + 4(\frac{-1 - \sqrt{2}x^{2}}{2}) - 13 = 8$
 $4(1 + 2\sqrt{2}x + 2x^{2})$

Also
$$4(\frac{-1-\sqrt{2}}{2})^{2} + 4(\frac{-1-\sqrt{2}}{2}) - 13 = 8$$

$$4(\frac{1+2\sqrt{2}}{2})^{2} + 24(\frac{-1-\sqrt{2}}{2}) - 13$$

$$21 - 13$$

$$8 = 8$$

$$9\left(\frac{1+\sqrt{2}}{3}\right)^{2} - 1 = 6\left(\frac{1+\sqrt{2}}{3}\right)$$

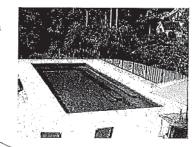
$$9\left(\frac{1+2\sqrt{2}+2}{9}\right) = 2\left(1+\sqrt{2}\right)$$

$$3+2\sqrt{2} - 1 = 1$$

$$2+2\sqrt{2} = 2+2\sqrt{2}$$

Solving Quadratic Equations by Completing the Square to Find Real Solutions

11. A pool measuring 12 meters by 16 meters is to have a sidewalk installed all around it, increasing the total area to 285 square meters. What will be the width of the sidewalk? (Solve by Completing the Square and round



the width of the sidewalk? (Solve by Completing the Square and round your solution to the nearest hundredth.)

$$(1\partial t \partial x)(16t\partial x) = 2.85$$

$$19.2 + 34x + 32x + 44x^2 = 285$$

$$4x^2 + 56x$$

$$y^2 + 14x + 49 = 93 + 49$$

$$(x + 7)^2 = \sqrt{7}, 25$$

$$(x + 7)^2 = \sqrt{7}, 35$$

$$(x + 7)^2 = \sqrt{7}, 5$$

$$($$

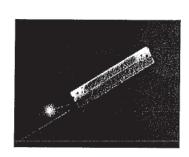
time t = 0 is given by $h(t) = -16t^2 + 80t + 96$. How long will it take the arrow to strike the ground? (Solve by Completing the Square and round your solution to the nearest hundredth.)



-16t2+80t +96 =0 t2-5t-6=0 t2-5t+25=6+25 V(t-5/2) = 199 16-51 = 3



ground is given by $h(t) = -16t^2 + 240t + 8$, where t is the time in seconds.



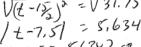
a) What is the height after 2 seconds?

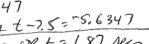
$$h(2) = -16(2)^{3} + 240(3) + 8$$

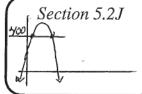
$$h(2) = -46(4)^{4} + 40(3) + 8$$

b) At what times will the rocket be at a height of 400 feet? (Solve by Completing the Square and round your solution to the nearest hundredth.)









 $-\frac{16+340+8}{-16+340+8} = \frac{392}{76} \qquad \sqrt{(t-1)} = \sqrt{31.75}$ $-\frac{16+340+8}{-16} = \frac{392}{76} \qquad |t-7.5| = 5.6347$ $t = \frac{395}{-16} = \frac{392}{76} \qquad |t-7.5| = 5.6347 \text{ of } t-7.5 = 5.6347$ $t = \frac{395}{-16} = \frac{31.75}{4} = \frac{31.7$

P-36

APPROPRIATE METHODS. FIND REAL AND NON-REAL COMPLEX ROOTS WHEN THEY EXIST. RECOGNIZE THAT A PARTICULAR SOLUTION MAY NOT BE APPLICABLE IN THE ORIGINAL CONTEXT.

5.2K Solving Quadratic Equations by Completing the Square to Find Real or Complex Solutions

#1 - 3: Solve using square roots.

1.
$$\sqrt{(x-5)^2} = \sqrt{144}$$

$$\sqrt{x-5} = 12\dot{\iota}$$

$$\sqrt{x} = 5 \pm 12\dot{\iota}$$

2.
$$\sqrt{(x-7)^2} = \sqrt{-24}$$

 $\sqrt{x-7} = 2i\sqrt{6}$
 $\sqrt{x} = 7 \pm 2i\sqrt{6}$

3.
$$\sqrt{-128} = \sqrt{(x+13)^2}$$

 $8i\sqrt{5} = \sqrt{1 + 13}i$
 $x = -13 \pm 8i\sqrt{5}$

#4 – 5: Fill in the missing value to create a perfect square trinomial. Then solve by *Completing the Square*.

4.
$$-40 + 36 = x^2 + 12x + 36$$

$$\sqrt{-4} = \sqrt{(x+6)^2}$$

$$2i = /x+6/$$

$$x = -6 \pm 2i$$

5.
$$x^2 - 24x + 144 = -216 + 144$$

 $\sqrt{(x - 12)^2} = \sqrt{-72}$
 $|x - 12| = 6i\sqrt{2}$
 $|x = 12 \pm 6i\sqrt{2}$

#6-9: Solve by <u>Completing the Square</u>. Then verify your solutions. (See next page)

6.
$$4x = x^2 + 5x + 4$$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4 = x^2 + 5x + 4$
 $4x + 4x + 4x + 4$
 $4x + 4x +$

7.
$$x^{2}-4x+20=0$$

$$x^{2}-4x+4=-20+4$$

$$\sqrt{(x-2)^{2}}=\sqrt{76}$$

$$|x-2|=4i$$

$$x=2\pm4i$$

8.
$$6x+23=10x^2+26$$

$$10x^3-6x = -3$$

$$x^2-3x = -3$$

$$x^2-3x+9x = -3x+9$$

$$\sqrt{(x-3)^2} = \sqrt{-31}$$

$$|x-3| = \sqrt{31}$$

$$|x-3| = \sqrt{31}$$

9.
$$-5 = 8x^{2} + 6x$$

$$x^{2} + \frac{3}{4}x + \frac{9}{64} = -5 + \frac{9}{64}$$

$$\sqrt{(x + \frac{3}{8})^{2}} = \frac{-3!}{64}$$

$$x + \frac{3}{8} = \frac{0.031}{8}$$

$$x = -3 \pm 0.031$$

5.2 I CAN REPRESENT REAL-WORLD SITUATIONS WITH QUADRATIC EQUATIONS AND SOLVE USING
APPROPRIATE METHODS. FIND REAL AND NON-REAL COMPLEX ROOTS WHEN THEY EXIST. RECOGNIZE
THAT A PARTICULAR SOLUTION MAY NOT BE APPLICABLE IN THE ORIGINAL CONTEXT.

p-37 checks

#6)
$$(4x = x^2 + 5x + 4)$$
 Verifying $x = \frac{-1 \pm i V i 5}{2}$
 $4(-1 + i V i 5) = (-1 + i V i 5)^2 + 5(-1 + i V i 5) + 4$
 $2(-1 + i V i 5) = \frac{1 - 2i V i 5 - 15}{2}$
 $= 2 + 2i V i 5 = \frac{-14 - 2i V i 5}{2}$
 $= -4 + 4i V i 5$
 $= -4 + 2i V i 5$
 $= -4 + 2i V i 5$
 $= -2 + 2i V$

#7)
$$|x^2-4x+20=0|$$
 Verifying $x=2\pm 4i$
 $(2+4i)^2-4(2+4i)+20=0$
 $4+16i-16-8-16i+20$
 $Also$
 $(2-4i)^2-4(2-4i)+20=0$
 $4-16i-16-8+16i+20=0$

#8
$$6x + 23 = 10x^{2} + 36$$
 $Verifying $x = \frac{3 \pm i\sqrt{3}i}{10}$ $6(\frac{3 + i\sqrt{3}i}{10}) + 23 = 10(\frac{3 + i\sqrt{3}i}{10})^{2} + 26$ $3(\frac{3 + i\sqrt{3}i}{5}) - 23 = -23$ $\frac{9 + 3i\sqrt{3}i}{5} = \frac{10(\frac{9 + 6i\sqrt{3}i - 2i}{10})}{5} + 3$ $\frac{-12 + 6i\sqrt{3}i}{5} = \frac{9 + 3i\sqrt{3}i}{5} + \frac{15}{5}$ $\frac{9 + 3i\sqrt{3}i}{5} = \frac{9 + 3i\sqrt{3}i}{5} + \frac{15}{5}$ $\frac{9 - 3i\sqrt{3}i}{5} = \frac{10(\frac{9 - 6i\sqrt{3}i - 2i}{10})}{5} + 36$ $\frac{9 - 3i\sqrt{3}i}{5} = \frac{-12 - 6i\sqrt{3}i}{5} + \frac{15}{5}$ $\frac{9 - 3i\sqrt{3}i}{5} = \frac{-12 - 6i\sqrt{3}i}{5} + \frac{15}{5}$$

= 9-36/21 2

$$\begin{array}{l}
\#g = 8x^{2} + 6x \quad \text{Verifying } x = \frac{-3 \pm i\sqrt{3}i}{8} \\
8\left(\frac{-3 + i\sqrt{3}i}{8}\right)^{2} + 6\left(\frac{-3 + i\sqrt{3}i}{8}\right) = -5 \\
8\left(\frac{9 - 6i\sqrt{3}i - 3i}{64}\right) + \frac{-18 + 6i\sqrt{3}i}{8} = \frac{-32 - 6i\sqrt{3}i}{8} + \frac{-9 + 3i\sqrt{3}i}{4} = \frac{-30}{4} = -5
\end{array}$$

$$\begin{array}{l}
-11 - 3i\sqrt{3}i + \frac{-9 + 3i\sqrt{3}i}{8} = -5 \\
8\left(\frac{9 + 6i\sqrt{3}i - 3i}{8}\right)^{2} + 6\left(\frac{-3 - i\sqrt{3}i}{8}\right) = -5
\end{array}$$

$$\begin{array}{l}
8\left(\frac{9 + 6i\sqrt{3}i - 3i}{8}\right) + \frac{-18 - 6i\sqrt{3}i}{8} = -5
\end{array}$$

$$\begin{array}{l}
-22 + 6i\sqrt{3}i \\
9 \\
-11 + 3i\sqrt{3}i + \frac{-9 - 3i\sqrt{3}i}{4} = -5
\end{array}$$

$$\begin{array}{l}
-30 \\
-31 + 3i\sqrt{3}i \\
-30 + 3i\sqrt{3}i
\end{array}$$

$$\begin{array}{l}
-30 \\
-30 + 3i\sqrt{3}i
\end{array}$$

5.2K Solving Quadratic Equations by Completing the Square to Find Real or Complex Solutions

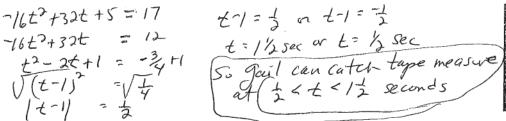
10. Emma hits a golf ball off the tee. The height of the ball is given by $h(x) = -16x^2 + 4000x + 3248$ where h is the height in yards above the ground and x is the horizontal distance from the tee in yards. How far does Emma hit the ball? (Solve by Completing the Square and round your solution to the nearest hundredth.)

-16x + 4000x $x^2 - 250x + 15625 = 203 + 15625$ $\sqrt{(x - 125)^2} = \sqrt{15828}$ /x-1251 = 125,81 $x - 125 = \pm 125.81$ x = 250.81 yds x = 0.81 whanews



11. Gail and Veronica are fixing a leak in a roof. Gail is working on the roof and Veronica is tossing up supplies to Gail. When Gail tosses up a tape measure, the height h, in feet, of the object above the ground t seconds after Veronica tosses it is $h(t) = -16t^2 + 32t + 5$. Gail can catch the object any time it is above 17 feet. How much time does Gail have to try to catch the tape measure? (Solve by Completing the Square and round your solution to the nearest hundredth.)

7/6t3+32t+5=17

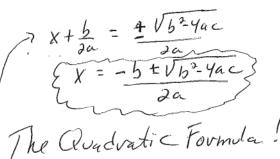




12. For which values of y, given $y = x^2 + bx + \left(\frac{b}{2}\right)^2$, will you find 2 complex solutions? when y < 0

13. Solve the following quadratic for x by Completing the Square.

What is the result?



Section 5.2K

I CAN REPRESENT REAL-WORLD SITUATIONS WITH QUADRATIC EQUATIONS AND SOLVE USING APPROPRIATE METHODS. FIND REAL AND NON-REAL COMPLEX ROOTS WHEN THEY EXIST. RECOGNIZE THAT A PARTICULAR SOLUTION MAY NOT BE APPLICABLE IN THE ORIGINAL CONTEXT.

5.2L Solving Quadratic Equations Using the Quadratic Formula to Find Real Solutions 🗆 🚟 🚟

Describe a situation where you would HAVE to use the quadratic formula to solve a quadratic equation if If the quadratic equation does not factor, the voots are either invational or imaginary

#2-7: Determine a, b, and c and then solve using the quadratic formula. Remember to show ALL work.

2.
$$2x^2 - 5x - 3 = 0$$

$$X = \frac{5 \pm \sqrt{25 - 4(2)(-3)}}{4}$$

$$Y = \frac{5 \pm \sqrt{49}}{4} - \frac{5 + 7}{4} = \frac{3}{\sqrt{x}}$$

$$\frac{5 - 7}{x} = \frac{-1}{3}$$

3.
$$x^2-7x+9=0$$

a:
$$\int b$$
: $\int c$: 4

$$X = 7 \pm \sqrt{(-7)^2 - 4(1)(9)}$$

$$X = 7 \pm \sqrt{13}$$

Could you have solved by factoring? Explain.

Could you have solved by factoring? Explain.

(2x+1)(x-3)=0 (49 is a perfect square #)

$$X = -\frac{1}{2}$$
 or $X = 3$

Could you have solved by factoring? Explain:

4.
$$5x^2 + 3x = 1$$

5.
$$x^2 + x - 1 = 0$$

a: 1 b: | c:
$$-1$$

$$x = \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-1)}}{9^{(1)}}$$

$$x = \frac{-1 \pm \sqrt{5}}{2}$$

Could you have solved by factoring? Explain.

Could you have solved by factoring? Explain:

Not a perfect square #

Not a perfect square # Could you have solved by factoring? Explain:

Solving Quadratic Equations Using the Quadratic Formula to Find Real • Solutions

#2-7 (continued): Determine a, b, and c and then solve using the quadratic formula. Remember to show ALL work.

6.
$$9x^2 + 6x - 1 = 0$$

a: 9 b: 6 c:
$$-\frac{1}{2}$$

 $X = -6 \pm \sqrt{(6)^2 - 4(9)(7)}$
 $X = -6 \pm \sqrt{72} = -6 \pm 6\sqrt{2}$
 $X = -\frac{1 \pm \sqrt{2}}{3}$
8 A cliff diver jumps up and away from

7.
$$2x^2 + 3x + 2 = 3$$

a:
$$\lambda$$
 b: 3 c: -1

$$\chi = -3 \pm \sqrt{(3)^2 - 4(2)(-1)}$$

$$\frac{\lambda(2)}{4}$$

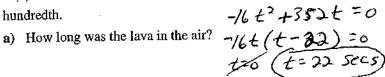
A cliff diver jumps up and away from the cliff as he jumps. His path can be modeled by the equation $h(t) = -16t^2 + 12t + 25$, where h is the height, in feet, of the diver at a specific time, t, in seconds. How long will it take for the diver to reach the water below? Solve using the quadratic formula. Round answers to the nearest hundredth. (Hint: When the diver hits the water, he is at a height of 0 ft.)



$$x = \frac{-12 \pm \sqrt{(12)^2 - 4(16)(25)}}{2(16)}$$

$$x = \frac{-12 \pm \sqrt{1744}}{-32} \times \frac{2 - 0.93}{2 \cdot 0.68} \text{ Seconds}$$
The volcanic cinder cone Puu Puai in Hawaii was formed in 1959 when a massive

The volcanic cinder cone Puu Puai in Hawaii was formed in 1959 when a massive "lava fountain" erupted at Kilauea Iki Crater, shooting lava hundreds of feet into the air. When the eruption was most intense, the height h (in feet) of the lava t seconds after being ejected from the ground could be modeled by $h(t) = -16t^2 + 352t$. Solve using any method you have learned. Round your answers to the nearest





b) How long did it take the lava to reach its maximum height of 1936 feet?

b) How long did it take the lava to reach its maximum height of 1936 test.

$$-16t^{2} + 352t = 1936$$

$$-16t^{3} + 352t - 1936 = 0$$

$$a = -16$$

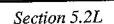
$$b = 352$$

$$c = -1936$$

$$t = -352 \pm \sqrt{0}$$

$$-32$$

$$t = 11 \text{ Seconds}$$



52M Solving Quadratic Equations Using the Quadratic Formula to Find Real or Complex Solutions

#1-3: Review: Simplify the following radicals.

1.
$$\sqrt{-12}$$

$$\sqrt{-1.4\cdot 3}$$

$$2 \cdot \sqrt{3}$$

$$\begin{array}{c|c}
2. & \sqrt{24} \\
\hline
\sqrt{4.6} \\
\hline
206
\end{array}$$

#4-9: The following solutions were found using the quadratic formula but are not simplified all the way. Put the solutions in simplest form. No decimals allowed! $\partial \mathcal{L}$

4.
$$x = \frac{-2 \pm 4}{2} < \frac{3}{5}$$

$$\sqrt{\frac{2}{x^2 + 1}} = \frac{2}{3}$$

$$5. \quad x = \frac{-6 \pm \sqrt{0}}{4}$$

$$\sqrt{x = \frac{3}{2}}$$

6.
$$x = \frac{3 \pm \sqrt{-4}}{2}$$

$$x = \frac{3 \pm 2i}{3}$$

7.
$$x = \frac{-6 \pm \sqrt{-11}}{2(2)}$$

$$x = \frac{-6 \pm i \sqrt{11}}{4}$$

8.
$$x = \frac{-2 \pm \sqrt{-20}^{7}}{2(1)}$$

$$\sqrt{X = -1 \pm i \sqrt{5}}$$

9.
$$x = \frac{-2 \pm \sqrt{64}}{2(1)} < \frac{6}{2}$$

$$\sqrt{\frac{x = 3 \text{ or } x = -5}{2}}$$

10. Carter solved the following quadratic equation using the quadratic formula – his work is shown below. However, he did not simplify his answer correctly. Find his mistake(s) and then simplify the solution correctly.

Even Line 6
$$X = \frac{-6 \pm 3i}{2}i = -3 \pm i$$

$$X = -3 \pm i$$

Line 1
$$x^2+6x+10=0$$

C Line 2 $a=1, b=6, c=10$
C Line 3 $x = \frac{-6\pm\sqrt{(6)^2-4(1)(10)}}{2(1)}$
C Line 4 $x = \frac{-6\pm\sqrt{-4}}{2}$
C Line 5 $x = \frac{-6\pm2i}{2}$
X Line 6 $x = -3\pm2i$

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Name	Fenod

5.2M Solving Quadratic Equations Using the Quadratic Formula to Find Real or Complex Solutions

#11-13: Solve using the quadratic formula. Be sure to simplify your answer, keeping your answers exact (no decimals approximations). Remember to show ALL work.

11.
$$x^{2}+6x=-2$$

12. $2x^{2}-8x=-8$

13. $5x^{2}-13x+9=0$
 $2x^{2}-8x+8=0$
 $2x^{2}-8x+9=0$
 $2x^{2}-8x+9$

- 14. The path of an object thrown straight up in the air with an initial velocity of 40 feet per second and from an initial height of 4 feet can be modeled by the equation $h(t) = -16t^2 + 40t + 4$, where h is the height of the object at time t.
 - a) How long does the object remain in the air before landing (height = 0)? Put your answer in decimal form, rounded to the nearest tenth of a second.

answer to choose? Since t=0 means time when object is initially thrown, positive time means time after the throw was started.

Negative time implies time before the object was thrown, which doesn't make sense here.

c) How long is the object in the air when it reaches a height of 25 feet?

$$-1(t^{2}+40t-21=0)$$

$$a=-16 \quad 5=40 \quad c=-21$$

$$t=-\frac{40 \pm \sqrt{(40)^{2}-4(-16)(-21)}}{2(-16)}$$

c) How long is the object in the air when it reaches a height of 25 feet?

$$-16t^{2} + 40t + 4 = 35$$

$$-16t^{2} + 40t - 21 = 0$$

$$4 = -16 \quad 5 = 40 \quad c = -21$$

$$4 = -40 \pm 16 \quad 0.75 \text{ sec}$$

$$4 = -40 \pm 16 \quad 0.75 \text{ secs}$$

$$4 = -40 \pm 16 \quad 0.75 \text{ secs}$$

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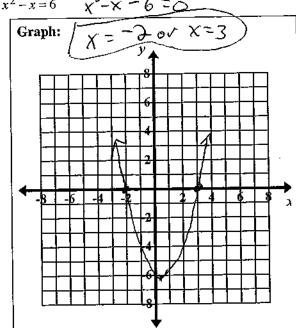
Section 5.2M	•

5.2N Solving Quadratic Equations – Choosing the Best Method: Part L

- List 5 ways to solve a quadratic equation:

 - > Use a graphing utility to find real zeros > Factor and use the zero product property
 - > Use square roots

 - > Complete the Square > Use the Quadratic Formula
- #2-3: Solve the following quadratic equations using the indicated methods.
- $x^2 x = 6$ $x^3 x 6 = 0$



Factor:

$$(x-3)(x+2)=0$$

 $(x-3)(x+2)=0$
 $(x-3)(x+2)=0$

Quadratic Formula:
$$a = 1$$

 $\chi^2 - \chi - 6 = 0$ $b = -1$
 $c = -6$

$$X = \frac{1 \pm \sqrt{(1)^{3} - 4(1)(-6)}}{3(1)}$$

$$X = \frac{1 \pm \sqrt{35}}{3} + \frac{1 + 5}{3} = 3$$

Solution(s):

X = 3	3 65	× =	- - }
<u> </u>			

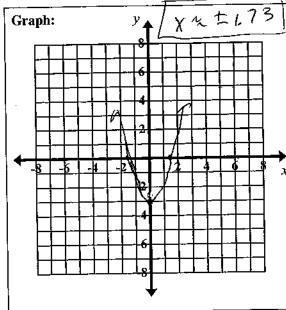
Which method was the most efficient for this problem and why?

Factoring Method is the fastst and yields rational solutions safely.

5.2N Solving Quadratic Equations — Choosing the Best Method: Part I

#2-3 (continued): Solve the following quadratic equations using the indicated methods.

3. $x^2 - 3 = 0$



Square Root:

$$x^{2}-3=0$$

$$\sqrt{x^{2}}=\sqrt{3}$$

$$|x|=\sqrt{3}$$

$$x=\pm\sqrt{3}$$

Quadratic Formula: a=1 b=0 c=3

$$x^{2}-3=0$$

$$x = -0 \pm \sqrt{0^{2}-4(1)(-3)}$$

$$x = 0 \pm \sqrt{12} = \pm 2\sqrt{3} = \sqrt{\pm \sqrt{3}}$$

Solution(s):

$$\sqrt{\chi = \pm \sqrt{3}}$$

Which method was the most efficient for this problem and why?

The SavARE ROOT method
There was no X, term, or b=0

- 4. List the method(s) for solving quadratic equations that:
 - a) You can always use but often it only gives approximate answers.

 graphing calculator (but can't use to find complex / imaginary solns).
 - b) You can always use to solve quadratic equations.
 Completing the Square and Quadratic Formula
 - c) You can only use sometimes to solve quadratic equations.

Factoring or Square Root

5.2N 🖫 Solving Quadratic Equations — Choosing the Best Method: Part I

#5 - 7: For each equation, determine an effective method for solving the quadratic equation and explain why you chose that method. Solve the quadratic equation with the method of your choice, keeping the answer exact (no decimal approximations).

the answer exact (no decimal approximations).
5.
$$2x^2+5x-3=0$$
 It factored easily.

$$\frac{(2x-1)(x+3)}{(x-1)(x+3)}$$

6.
$$-4x^2+4000x=0$$
 It factored easily.

$$\frac{-4x(x-1000)=0}{x=0 \text{ or } x=1000}$$

7.
$$x^2+7x-18=0$$

 $(X+9)(X-2)=0$ It factored easily.
 $X=-9$ or $X=2$

#8 - 11: Determine an answer for each situation. Be sure to clearly record your thinking.

The product of two consecutive integers is 72. Find the two numbers.

th = any integer

$$h(h+1) = 7$$
 $h^2 + h = 7$
 $h^2 + h = 7$
 $h^2 + h = 7$
 $h^2 + h = 7$

8. The product of two consecutive integers is 72. Find the two numbers.

Let
$$h = any \ rnteger$$
 $h(h+1) = 72$
 $h(h+1) = 72$
 $h^2 + h - 72 = 0$
 $h^2 + h - 72 = 0$

The length of a rectangle exceeds its width by 3 inches. The area of the rectangle is 70 square inches. Find its dimensions.

dimensions.

$$x+3$$
 $x(x+3)=70$
 $x = 70$ $x^3+3x-70=0$
 $(x+10)(x-7)=0$
 $x=-10$ $x=-7$ width = 7 in length = 10 in

5.2N Solving Quadratic Equations – Choosing the Best Method: Part I

#5-7: For each equation, determine an effective method for solving the quadratic equation and explain why you chose that method. Solve the quadratic equation with the method of your choice, keeping the answer exact (no decimal approximations).

5.
$$2x^2 + 5x - 3 = 0$$

 $(2x-1)(x+3)$
 $(2x-1)(x+3)$

5.
$$2x^2+5x-3=0$$
 It factored easily.

$$(2x-1)(x+3)$$

$$X=\frac{1}{2} \text{ or } X=\frac{-3}{2}$$

6.
$$-4x^2+4000x=0$$
 If factored easily.
 $-4x(x-1000)=0$
 $|x=0|$ or $x=1000$

7.
$$x^2+7x-18=0$$

 $(X+9)(X-2)=0$ If factored easily.
 $X=-9$ or $X=2$

#8 - 11: Determine an answer for each situation. Be sure to clearly record your thinking.

8. The product of two consecutive integers is 72. Find the two numbers.

Let
$$h = any \ n + e < r$$
 $h(h+1) = 7 + r$
 $h^2 + h^2 - 7 + r$

$$h(n+1) = 72$$

 $h^{2}+n-72=0$
 $(n-8)(n+9)$

8. The product of two consecutive integers is 72. Find the two numbers.

Let
$$h = any \ n + eger$$
 $h(n+1) = 72$
 $h^2 + h - 72 = 0$
 $h^2 + h -$

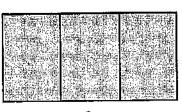
The length of a rectangle exceeds its width by 3 inches. The area of the rectangle is 70 square inches. Find its dimensions.

$$\begin{array}{c|c}
x+3 & x(x+3) = 70 \\
x & 70 & x^3+3x-70 = 0 \\
& (x+10)(x-7) = 0 \\
x = -10 & x=7
\end{array}$$

5,2N Solving Quadratic Equations — Choosing the Best Method: Part I

#8 - 11 (continued): Determine an answer for each situation. Be sure to clearly record your thinking.

10. Suzie wants to build a garden that has three separate rectangular sections. She wants to fence around the whole garden and between each section as shown. The plot is twice as long as it is wide and the total area is 200 square feet. How much fencing does Suzie need?



2x

1x1=10 x= ±10 wieth 10

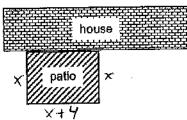
length 20

 $X(2x) = \partial 2$ Fencing = Perimeter + 2x $2x^{2} = 200$ = 2L + 2w + 3x = 2(3x) + 2(x) + 2x

11. Mike wants to fence three sides of a rectangular patio that is adjacent to the back of his house. The area of the patio is 192 ft² and the length is 4 feet longer than the width. Find how much fencing Mike will need.

x(x+4)=191

Fencing = x + (x+4) + x $x^{3}+4x-192=0$ = 3x+4 (x-12)(x+16)=0 = 3(12)+4 x=12 or x=76 extranecys (Fencing=40 feet)



- #12-13: Solve each quadratic equation 2 different ways. Record the method that you are using for each. (Square Roots - Factoring - Completing the Square -Quadratic Formula)
- 12. $2x^2 + 3 = 21$

Method 1: Square Roots

2x3+3=21 Solution(s): [X=±3]
Square Roots because there was no X-term.

Factoring some difference of squares pattern is easy.

Method 2: Factoring $2x^3+3=21$ $2x^{2}-18=0$ $2(x^{2}-9)=0$

Why did you choose the two methods that you did and which do you feel is more SQuare Roots has less chance for a careless sign error.
Also, students have been factoring.
Than they have been factoring.

5.2N. Solving Quadratic Equations—Choosing the Best Method: Part I

- #12 13 (continued): Solve each quadratic equation 2 different ways. Record the method that you are using for each. (Square Roots Factoring Completing the Square Quadratic Formula)
- 13. The length of a rectangular pool is 10 meters more than its width. The area of the pool is 875 square meters. Find the dimensions of the pool.



Method 1: Completing the Square $X(x+10) = 875$ $y^{2}+10x+25 = 875+25$ $\sqrt{(x+5)^{2}} = \sqrt{950}$ $/x+5/ = 30$ $x+5 = \pm 30$ $x = -5\pm 30 < 35$ $x = -5\pm 30$ $x = 35 m$ $x = 35 m$	Method 2: Factoring $x(x+10) = 875$ $x^{2}+10x-875 = 0$ $(x-25)(x+35) = 0$ $x=25 x=-35$ $x+10=35 extransors$ Light = 35m $\text{length} = 35m$
Solution(s): Width = 25 m length = 35 m Complete the Square already had the constant isolated and it was easy to find (b) ² . Factoring was nice since a = 1.	you did and which do you feel is more who were efficien

#14 - 17: Solve the following quadratic equations with the method of your choice. Verify that the answer is correct:

14.
$$3x^{2}+6x=-10$$
 $3x^{3}+6x+10=0$
 $x=-6\pm\sqrt{(6)^{2}-4(3)(5)}$
 $x=-6\pm\sqrt{-34}$
 x

$5.2N \pm S$ őlving Quadrátic Equation \overline{s} — Choosing the Best Method: Part I_{\perp}

#14-17 (continued): Solve the following quadratic equations with the method of your choice. Verify that the answer is correct:

15.
$$-3x^2 + 12x + 1 = 0$$
 $\chi = \frac{-(3 \pm \sqrt{(12)^2 - 4(-3)(1)})}{2(-3)}$
 $x = -3$ $y = -12 \pm \sqrt{156}$
 $x = -12 \pm 2\sqrt{39} \Rightarrow x = \frac{6 \pm \sqrt{39}}{3}$

Verify that your answer(s) are solution(s):

$$-3\left(\frac{6+\sqrt{34}}{3}\right)^{2} + 12\left(\frac{6+\sqrt{3}9}{3}\right) + 1 = 0$$

$$-3\left(\frac{36+12\sqrt{3}9+39}{9}\right) + 4\left(6+\sqrt{3}9\right) + 1$$

$$\frac{75+12\sqrt{3}9}{-3}$$

$$-3\left(\frac{(x+3)(x+3)}{3}\right) = 0$$

$$-3\left(\frac{(x+3)(x+3)}{3}\right) = 0$$

$$-3\left(\frac{6-\sqrt{3}9}{3}\right)^{2} + 12\left(\frac{9}{3}\right)^{2}$$

$$Also -3\left(\frac{6-\sqrt{3}9}{3}\right)^{2} + 12\left(\frac{9}{3}\right)^{2}$$

16.
$$x^2 + 6x + 9 = 0$$

 $(x+3)(x+3) = 0$
 $(x+3)(x+3) = 0$

$$Also -3\left(\frac{6-\sqrt{39}}{3}\right)^{2} + 12\left(\frac{6-\sqrt{39}}{3}\right) + 1 = 0$$

$$-3\left(\frac{6-\sqrt{39}}{3}\right)^{2} + 12\left(\frac{6-\sqrt{39}}{3}\right) + 1$$

$$-3\left(\frac{36-12\sqrt{39}+39}{9}\right) + 4\left(6-\sqrt{39}\right) + 1$$

Verify that your answer(s) are solution(s):

$$(-3)^{3} + 6(-3) + 9 = 0$$

 $9 - (8 + 9)$
 $0 = 0$

17.
$$81x^2 + 1 = 0$$

$$\frac{8/x^{2} = -1}{\sqrt{|x|^{2}}}$$

$$\sqrt{|x|^{2}} = \frac{1}{81}$$

$$\sqrt{|x|^{2}} = \frac{1}{81}$$

$$\sqrt{|x|^{2}} = \frac{1}{81}$$

$$\sqrt{|x|^{2}} = \frac{1}{4}$$

$$\sqrt{|x|^{2}} = \frac{1}{4}$$

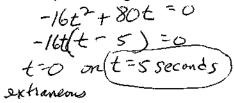
Verity that your answer(s) are solution(s).

$$81\left(\frac{c}{q}\right)^{2} + 1 = 0$$

$$81\left(\frac{-1}{q}\right)^{2} + 1 = 0$$

$52N_{\odot}$ Solving Quadratic Equations \pm Choosing the Best Method: Part I

- 18. The height h (in feet) above the ground of a baseball depends upon the time t (in seconds) it has been in flight. Joe takes a mighty swing and hits a bloop single whose height is described approximately by the equation $h = 80t 16t^2$.
 - a) How long is the ball in the air?





- b) When does the ball reach its maximum height? Use graphing Calc.

 After 2.5 Seconds
- c) What is the maximum height?

100 ft

d) It takes approximately 0.92 seconds for the ball to reach a height of 60 feet. On its way back down, the ball is again 60 feet above the ground. What is the value of t when this happens?

Add the line in y = 60 and use calculate intersect to get

[= 4.08 seconds]

Section 5.2N

Name	Period
52N Solving Quadratic Equations - Choosing the Best Method	d. Part I

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5.20 Solving Quadratic Equations — Choosing the Best Method: Part II

- #1-5: Four equations and one situation are given. Solve one by the square root property, one by factoring, one by completing the square, one using the quadratic formula, and one by graphing. Express your answers in simplest radical form. Verify your answer
- 1. $2x^2 = -7x + 15$
- 2. $x^2 2x 15 = 0$ 3. $x^2 + 12x = 20$ 4. $(x-3)^2 = 8$
- 5. A group of friends hiked to Havasupai Point in Grand Canyon National Park. The Colorado River was 4755 feet below them. A rock was thrown upward at an initial velocity of 24 feet per second. The rock's height t seconds after it was thrown upward is given by the function $h(t) = -16t^2 + 24t + 4755$. How long did it take for the rock to hit the river?

Solve by: Square Root Property

Solve:

1x-31 = 2V2

X=3±2va Solution(s):

Solve by: Factoring

$\frac{\partial}{\partial x}$ equation: $\frac{x^2-2x^2-15}{x^2-2}$

Solve:

(x-5)(x+3)=0

Solution(s): $\int x = 5$ or x = -3

Solve by: Completing the Square

3 equation: $\frac{x^2+12x}{x^2+12x+36} = 30 + 36$

Solve:

V(x+6)2 = 156 1x+61 = 2V14 x = -6 = 2514

Solution(s): $X = -6 \pm 2\sqrt{14}$

Solve by: Using the Quadratic Formula

equation: 2x + 7x - 15 = 0Solve: a = 2 + 5 = 7 + 6 = 7 = 15

X= -7±V72-4(2)(-/5)

 $X = -\frac{7+13}{4}$ or $X = -\frac{7-13}{4}$ Solution(s): $X = \frac{3}{2}$ or $X = -\frac{5}{2}$

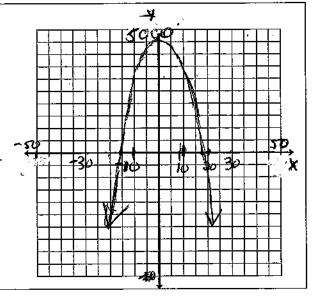
5.20 Solving Quadratic Equations & Choosing the Best Method: Part II

#1 - 5 (continued): Four equations and one situation are given. Solve one by the square root property, one by factoring, one by completing the square, one using the quadratic formula, and one by graphing. Express your answers in simplest radical form. Verify your answer

Solve by: Graphing # 5 equation: $h(\xi) = 76t^3 + 34t + 4755$

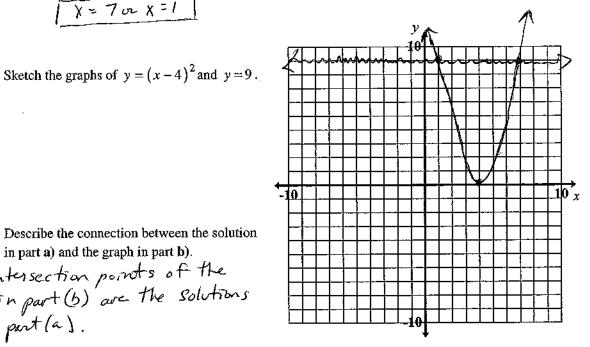
Solution(s): +- 18,005 seconds Verify that your answer(s) are solution(s) $h(18.005) = 76(18.005)^3 + 24(18.005) + 4755$

0 20.2396 x very close, but not exact.



a) Solve $\sqrt{(x-4)^2} = \sqrt{9}$ 1x-41=3 X=4+3 | X=70x X=1

Sketch the graphs of $y = (x-4)^2$ and y=9.

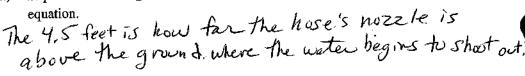


in part a) and the graph in part b). The intersection points of the 2 graphs in part (b) are the solutions for x in part(a).

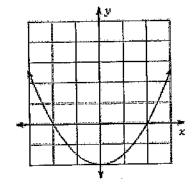
5.2

Solving Quadratic Equations - Choosing the Best Method: Part II

- A hose used by the fire department shoots water out in a parabolic arc. Let x be the horizontal distance from the hose's nozzle, and y be the corresponding height of the stream of water, both in feet. The quadratic function is $y = -0.016x^2 + 0.5x + 4.5$.
 - Explain the meaning in the context of the situation of the 4.5 that appears in the



- What is the horizontal distance from the nozzle to where the stream hits the ground? 38,55 feet
- Will the stream go over a 6-foot high fence that is located 28 feet from the nozzle? Explain your reasoning. No. At 27.89 ft from the nozzle, the stream world hit the top of the 6-foot fence. However, at the 28 ft distance, the water hight is lower, reaching only 5.96 let high.
- The graph of $y = x^2 400$ is shown at right. Notice that no coordinates appear in the diagram. Without using your graphing calculator, figure out the actual window that was used for this graph. Find the high and low values for both the x- and y-axis. After you get your answer check it on your calculator.



{Xmin:} -30

Xmax: 30_

Ymin: -400

Ymax: 1000

Section 5.20

Name	Period
5.20 - Solving Quadratic Fauations - Choosing the Best Me	ethod: PartII

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5.3A Number and Type of Solutions: Part I.

1. What is the discriminant? What does it do?

In the quadratic formula, $x = -b \pm \sqrt{b^2 - 4ac}$ The discriminant is the value of the expression $b^2 - 4ac$ that is under the radical.

This number is used to determine the number and type of solutions of a quadratic equation.

#2-9: Find the discriminant, the number of solutions and the type of solutions for each equation.

2.
$$x^2 + 6x + 10 = 0$$

 $b^2 - 4ac = (6)^2 - 4(1)(10)$
= 36-40

= -4

3.
$$3x^2+2x=1$$

 $3x^2+3x-1=0$
 $6^2-4ac=(2)^2-4(3)(-1)$
 $= 4+12$
 $= 16$

discriminant: _______
number of solutions: ______
type of solutions: imaginary

number of solutions: 2

type of solutions: real, rational

4.
$$0 = x^2 - 4x + 4$$

$$b^2 - 4ac = (4)^2 - 4(1)(4)$$

$$= 16 - 16$$

$$= 0$$

5.
$$12x^2 = 11x + 2$$
 $12x^2 - 11x - 7 = 0$

$$13^2 - 11x - 7 = 0$$

$$13^2 - 4(1)^3 - 4(1)(-7)$$

$$= 131 + 96$$

$$= 217$$

discriminant: 217

number of solutions: 2

type of solutions: real, irrational

5.3A Number and Type of Solutions: Part I

#2 - 9 (continued): Find the discriminant, the number of solutions and the type of solutions for each equation.

6.
$$8x+1=-16x^2$$
 $16x^2+8x+1=0$
 $16^3-4ac=(8)^2-4(16)(1)$
 $=64-64$
 $=0$

7.
$$7x^{2}+16x+11=0$$

 $6^{3}-4ac = (16)^{3}-4(7)(11)$
 $= 256 - 308$
 $= -52$

discriminant: number of solutions: type of solutions: real, rational

number of solutions: 2 type of solutions: imaginary

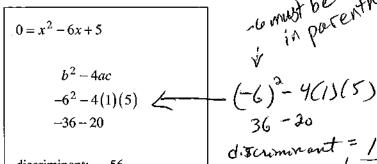
8.
$$5x^2 - 11x + 6 = 0$$

 $h^3 - 4ac = (-11)^2 - 4(5)(6)$
 $= 121 - 120$
 $= 1$

9.
$$0 = 4x^2 + 5x + 2$$

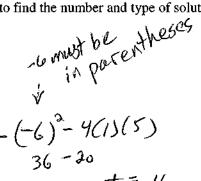
 $b^2 - 4ac = (5)^2 - 4(4)(2)$
 $= 3x^2 - 32$
 $= -7$

discriminant: ______/ number of solutions: type of solutions: <u>real</u> rational 10. On a quiz, Brittani used the discriminant to find the number and type of solutions. Find her mistake and find the correct solution.



discriminant: -56

solutions: 2 imaginary solutions



discriminant = 16 Solutions: /2 real, rational

5.3A Number and Type of Solutions: Part I

- 11. Emma and Brandon own a factory that produces bike helmets. Their accountant says that their profit per year is given by the function $P(x) = 0.003x^2 + 12x + 27760$, where x represents the number of helmets produced. Their goal is to make a profit of \$40,000 this year.
 - Write the equation that would represent a \$40,000 profit.

Write the equation in standard form.

Find the discriminant.
$$6^{9}-4ac = \frac{(12)^{9}-4(0.003)(-12240)}{144+146.88}$$

12. Marty is outside his apartment building. He needs to give Yolanda her cell phone but he does not have time to run upstairs to the third floor to give it to her. He throws it straight up with a vertical velocity of 55 feet/second. Will the phone reach her if she is 36 feet up?

(Hint: The equation for the height is given by $y = -16t^2 + 55t + 4$

$$-16t^{2}+55t+9=36$$

$$-16t^{3}+55t-32=0$$

$$d.3crimvant = (55)^{2}-4(-16)(-32)$$

$$\frac{3025-2048}{d:977/}$$

$$\frac{3025-2048}{d:977/}$$

$$\frac{3025-2048}{d:977/}$$

13. Bryson owns a business that manufactures and sells tires. The revenue from selling the tires in the month of July is given by the function R(x) = x(200 - 4x) where x is the number of tires sold. Can Bryson's No, Since discriminant & O, there are no real solutions

business generate revenue, R, of \$20,000 in the month of July?

Section 5.3A

	70 1 1
Name	Period

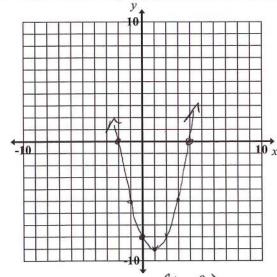
5.3A Number and Type of Solutions: Part I

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5.3B Number and Type of Solutions: Part II

- 1. $y = x^2 2x 8$
 - a) What is the discriminant? $6^{2}-4(a)(c) = (-2)^{2}-4(1)(-8)$ $\frac{4}{36}+32$
 - b) Number of solutions?
 - c) Type of solutions? real, rational
 - d) What are the zeros (roots)? x = -3*Factor or use the graph (x+2)(x-4)=0
 - e) Graph the equation.

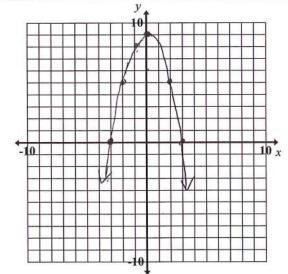
x	-2	-	0	1	2	4
у	0	-5	-8	-9	-8	0



- f) What is the vertex? (1, -9)
- g) Is the vertex a minimum or maximum?
- h) What is the y-intercept (y, y)
- i) What is the domain? all real numbers
- j) What is the range? $y \ge -9$

- 2. $y = 9 x^2$
 - a) What is the discriminant? $-x^3+9=0$ $b^2-4ac=(0)^2-4(-1)(9)$ = 0+36
 - b) Number of solutions? 2
 - c) Type of solutions? real vational
 - d) What are the zeros (roots)? $-1(x^2-9)=0$ *Factor or use the graph $x^2-9=0$ x=-3, x=3 (x+3)(x-3)=0
- e) Graph the equation.

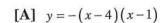
x	-3	-7	-1	0	2	3	
у	0	5	8	9	5	0	



- f) What is the vertex? (0, 9)
- g) Is the vertex a minimum or maximum?
- h) What is the y-intercept? (0, 9)
- i) What is the domain? all reals
- j) What is the range? $9 \le 9$

Number and Type of Solutions: Part II 5.3B

Which equation could model the graph to the right?



[B]
$$y = O(x+4)(x+1)$$

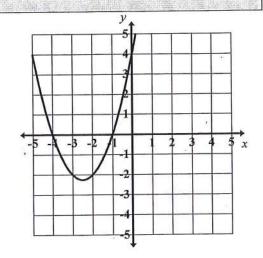
[C]
$$y = (x-4)(x-1)$$

[D]
$$y = (x-4)(x-1)$$

$$y = (x+4)(x+1)$$

$$0 = (x+4)(x+1)$$

$$\chi = -4 \text{ or } x = -1$$

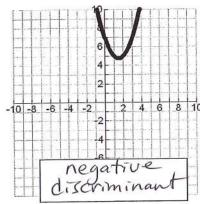


#4 - 6: Find the discriminant of each equation and then

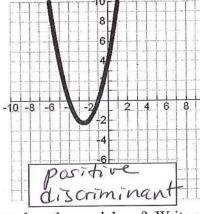
4. $x^2 + 6x = -2$ 36 - 8 5. $2x^2 - 8x = -8$ 16 - 16 6. $5x^2 - 13x + 9 = 0$ 169 - 180 discriminant: 28 number of solutions: 2 number of solutions:

real or imaginary: real or imaginary: real or imaginary: real or imaginary:

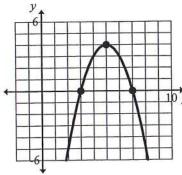
Label each graph below as having a positive, negative, or zero discriminant.



discriminant



What type of discriminant does the graph have? How many solutions does the graph have? Write a possible equation to model the graph pictured to the right.



Discriminant Positive perfect square number

Type and number of solutions

A possible equation y = -(x-3)(x-7)Section 5.3B $y = -(x^2 - 10x + 21)$ $y = -(x^2 + 10x - 21)$

P-60

5.4A Graphing Quadratic Inequalities

#1 - 3: Determine whether each of the given points is a solution to the given quadratic inequality.

1.
$$y \ge x^2 - 3x + 3$$

$$2. \quad y < -\frac{1}{2}x^2 - x + 6$$

3.
$$y > 2x^2 - x + 4$$

b)
$$(3,3)$$

 $34 - \frac{1}{7}(3)^{3} - (3) + 6$
 $4 - \frac{9}{7} - 3 + 6$
 $34 - 1\frac{1}{7}$ False (NOT SOLN)

#4 – 6: For each inequality and graph (the points plotted are points that exist on the boundary)...

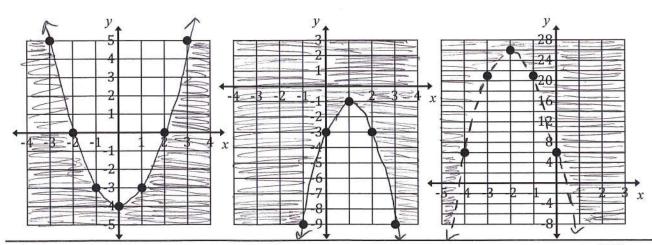
- > determine whether the boundary is included as a solution (solid) or not included as part of the solution (dashed).
- > use a test point to determine the solution region.

Graph the solution to each inequality.

4.
$$y \le x^2 - 4$$

$$5. \quad y \ge -2x^2 + 4x - 3$$

5.
$$y \ge -2x^2 + 4x - 3$$
 6. $y > -5x^2 - 20x + 6$



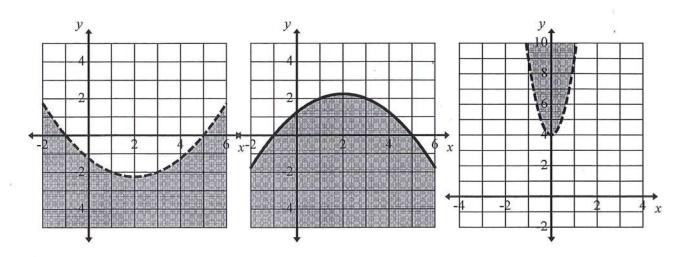
Graphing Quadratic Inequalities 5.4A

#7 - 9: Fill in the blank with the appropriate inequality sign.

7.
$$y = \frac{1}{4}x^2 - 1x - \frac{5}{4}$$

$$y = \frac{1}{4}x^2 - 1x - \frac{5}{4}$$
 8. $y = \frac{1}{4}x^2 - 1x - \frac{5}{4}$ 9. $y = \frac{5}{4}x^2 + 4$

9.
$$y > 5x^2 + 4$$



#10 - 15: Match the inequality with its graph.

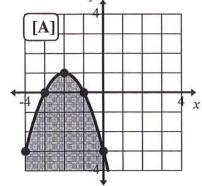
$$C_{10.} y \ge -x^2 + 4x - 3$$

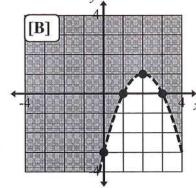
$$A = 11. \quad y \le -x^2 - 4x - 3$$

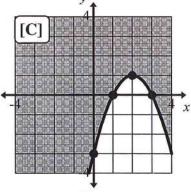
C 10.
$$y \ge -x^2 + 4x - 3$$
 A 11. $y \le -x^2 - 4x - 3$ F 12. $y \le x^2 + 2x - 3$

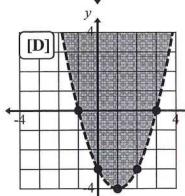
$$\underline{ \mathcal{E}}$$
 13. $y < x^2 - 4x + 3$

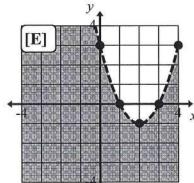
$$\underline{E}$$
 13. $y < x^2 - 4x + 3$ \underline{B} 14. $y > -x^2 + 4x - 3$ \underline{D} 15. $y > x^2 - 2x - 3$

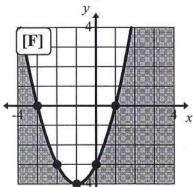








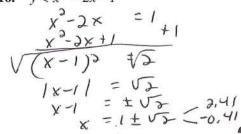


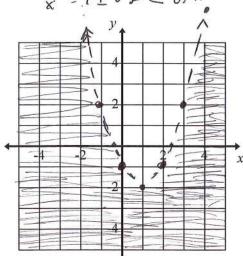


5.4A Graphing Quadratic Inequalities

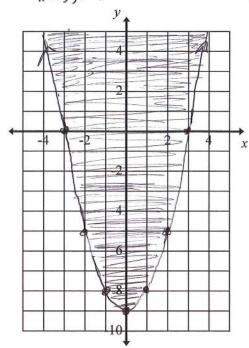
#16 - 23: Draw the graph of each quadratic inequality. When graphing the boundary, consider the various forms of a quadratic and the significant features that are identified from each form.

16. $y < x^2 - 2x - 1$





17.
$$y \ge x^2 - 9$$
 $(x+3)(x-3)$
 $x=3, x=3$

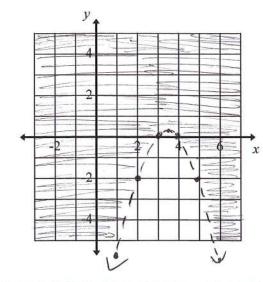


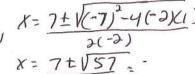
18. $y > -x^2 + 7x - 12$

$$0 = -1(x^2 - 7x + 12)$$

$$0 = -1(x - 3)(x - 4)$$

$$x = 3, x = 4$$

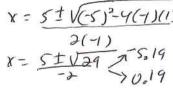




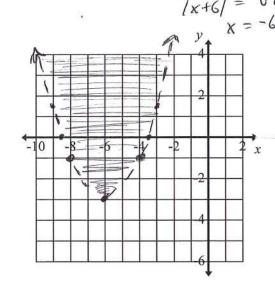
19. $y \le -2x^2 - 7x + 1$ $A = -3 \quad b = -7 \quad c = 1$ $X = \frac{7 \pm \sqrt{(-7)^2 - 4(-3)}(1)}{3(-3)}$ $X = \frac{7 \pm \sqrt{57}}{-4} = \frac{7 \pm \sqrt{57}}{3(-3)} = \frac{7 \pm \sqrt{57}}{3($

5.4A Graphing Quadratic Inequalities

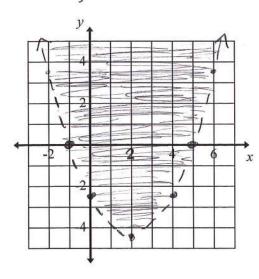
(continued): Draw the graph of each quadratic inequality. When graphing the boundary, #16 - 23consider the various forms of a quadratic and the significant features that are identified from each form.

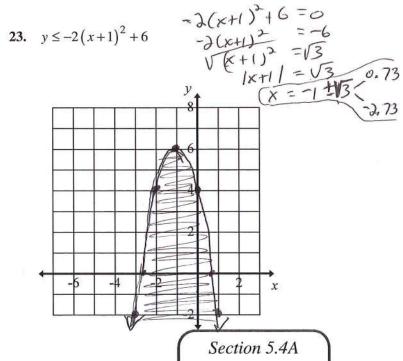


each form. 20. $y \le -x^2 - 5x + 1$ $x = \underbrace{5 \pm \sqrt{(-5)^2 - 4(-1)(1)}}_{2(-1)}$ 21. $y > \frac{1}{2}(x+6)^2 - 3 = 0$ $(x+6)^2 - 3 = 0$ $(x+6)^2 = 3$ $(x+6)^2 = 3$



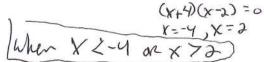
22. $y > \frac{1}{2}(x+1)(x-5)$



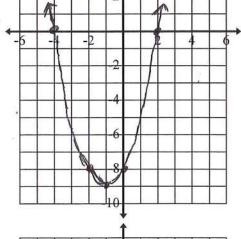


5.4B Solving Quadratic Inequalities

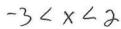
- 1. Graph $f(x) = x^2 + 2x 8$
 - a) On what interval(s) is $x^2 + 2x 8 > 0$?



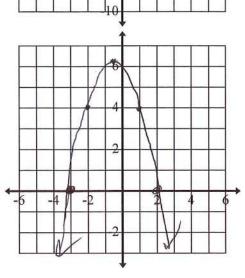
b) On what interval(s) is $x^2 + 2x - 8 < 0$?



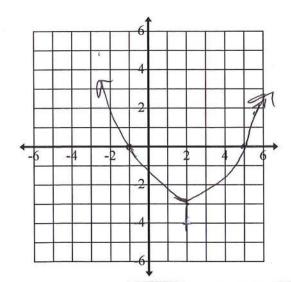
2. Graph $f(x) = -x^2 - x + 6$ $(x^2 + x - 6) = 0$ (x+3) (x-3) = 0(x+3) (x-3) = 0

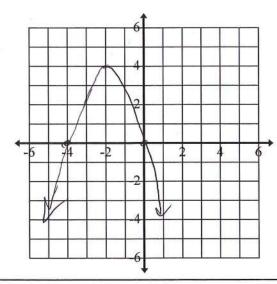


b) On what interval(s) is $-x^2 - x + 6 < 0$?



- 3. Draw a quadratic function that is:
 - \triangleright Positive when x < -1 and x > 5
 - \triangleright Negative when -1 < x < 5
- 4. Draw a quadratic function that is:
 - \triangleright Positive when -4 < x < 0
 - \triangleright Negative when x < -4 and x > 0

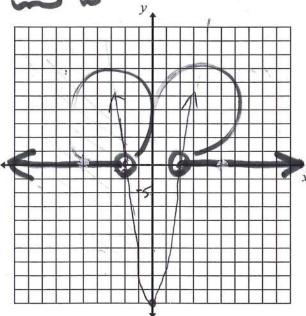


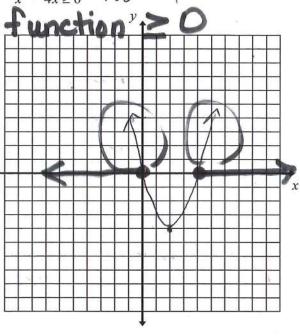


5.4B Solving Quadratic Inequalities

#5 - 12: Use a graph to find the solution for the following inequalities.

5. $x^2 - 25 > 0$ $\chi^2 = 25$ $\chi = \pm 5$





Solution: X2-5 on X>5

7. $x^2 - 7x + 10 < 0$ (x - 5)(x - 3) = 0 (x - 5)(x - 3) = 0

Solution: $X \le 0$ or $X \ge 4$ 8. $x^2 - 5x - 12 \le 0$ $x = 5 \pm \sqrt{(-5)^2 - 4(1)(7)}$ $x = 5 \pm \sqrt{73}$

Solution: 22 X 45

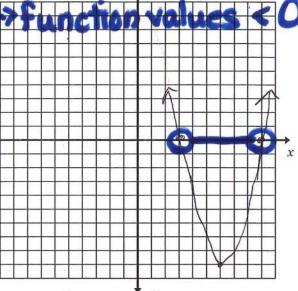
5.4B Solving Quadratic Inequalities

#5-12 (continued): Use a graph to find the solution for the following inequalities.

9. $x^2 > 8x + 20$

X3-8X-30=0

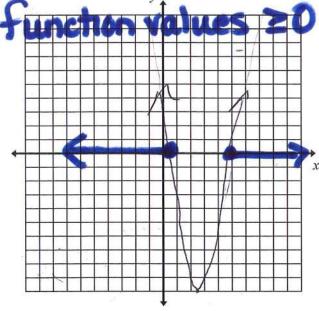
Solution: X < - 2 or X > 10



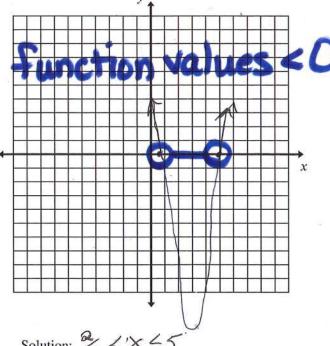
Solution: 3 < x < 9

11. $2x^2 - 11x + 5 \ge 0$ (2x - 1)(x - 5)

12. $3x^2 - 17x + 10 < 0$ (3x - 2)(x - 5) $x = \frac{3}{3}$ or x = 5



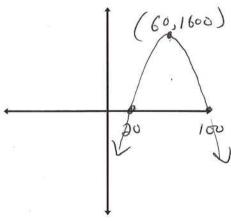
Solution: X= 4 or x 25



Solution: $\frac{2}{3} \angle ' \times \angle 5$

5.4B Solving Quadratic Inequalities

- #13 17: Use your graphing calculator to solve the following problems. Sketch the graph and label the x-intercepts and vertex.
- 13. The profit a coat manufacturer makes each day is modeled by the equation $P = -x^2 + 120x - 2000$, where P is the profit and x is the price for each coat sold. For what values of x does the company make a profit 20 < X < 100



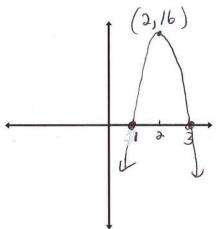
14. When a baseball is hit by a batter, the height of the ball, h, at time t, is determined by the equation $h(t) = -16t^2 + 64t + 4$. For which interval of time is the height of the ball greater than or equal to 52 -16+2+64+ +4 = 52 feet?

$$-16t^{2} + 64t - 48 = 0$$

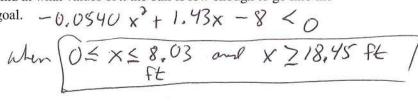
$$-16t^{2} + 64t - 48 = 0$$

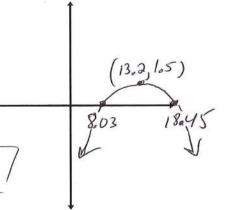
$$t = 1 \text{ or } t = 3$$

$$1 \le t \le 3$$
Seconds



- 15. The path of a soccer ball kicked from the ground can be modeled by $y = -0.0540x^2 + 1.43x$ where x is the horizontal distance (in feet) from where the ball was kicked and y is the corresponding height (in feet).
 - a) A soccer goal is 8 feet high. Write and solve an inequality to find at what values of x the ball is low enough to go into the goal. $-0.0540 \times^{3} + 1.43 \times -8 < 0$





b) A soccer player kicks the ball toward the goal from a distance of 15 feet away. No one is blocking the goal. Will the player score a goal? Explain your reasoning.

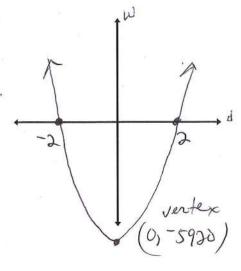
No! From 15 feet away, the height of the ball would be 9.3 ft So the ball would go over the top of the net.
Also, from the graph and algebraic solution inequalities above, 15 is not in the correct ranges.

5.4B Solving Quadratic Inequalities

#13-17 (continued): Use your graphing calculator to solve the following problems. Sketch the graph and label the x-intercepts and vertex.

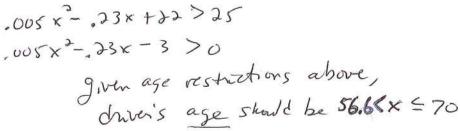
16. A manilla rope used for rappelling down a cliff can safely support a weight W (in pounds) modeled by the inequality $W \le 1480d^2$ where d is the rope's diameter (in inches). What diameter of rope would be needed to support a weight of at least 5920 pounds?

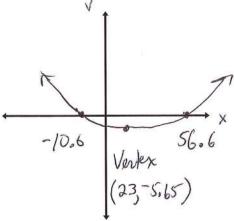
1480 2°-5920 20



17. For a driver aged x years, a study found that the driver's reaction time ν (in milliseconds) to a visual stimulus such as a traffic light can be modeled by $\nu = 0.005x^2 - 0.23x + 22$ when $16 \le x \le 70$.

At what age does a driver's reaction time tend to be greater than 25 milliseconds?





Name	Period

5.4B Solving Quadratic Inequalities

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Section 5.4B

Describe what you look for in determining which method is best to solve a quadratic equation:

a) Square Root: $No \times + kvm \cdot (kx^2 + k^2 + k^2$

b) Completing the Square: If infactorable and a=1 and bis even

c) Factoring: a, b, c are all integers and fairly small

d) Quadratic Formula: If unfactorable and a, b, c are larger numbers and for decimals.

Choose the most efficient method for each equation. You must select 3 equations for each method. *

Place a triangle around the letter of each equation you would solve by factoring.

Place a circle around the letter of each equation you would solve using the square root method.

& one Place a square around the letter of each equation you would solve by completing the square.

> The three equations with no mark would represent the equations you would solve using the quadratic formula.

(A) $2x^2 + 5 = 41$

- $[B] \sqrt{3x^2 + 17x} = -10$
- [C] $x^2 + 20x = -104$

[D] $x^2 - 6x - 15 = 0$

- \mathbf{E} $x^2 + 4x = 12$
- $[\mathbf{F}]$ $8x^2 28x 60 = 0$

- [G] $3x^2 + 6x + 2 = 0$
- [H] $6x^2 8x = -3$
- $|I| 9x^2 + 12x + 4 = 0$

- (J) $-3(x-1)^2 = 36$
- (K) $2(x-6)^2-45=53$
- ILI $5x^2 13x + 6 = 0$
- 3. The letters you placed a circle around represent the equations you would solve using the square root method. Write one equation in each blank below (3 blanks, 3 equations). Solve each equation using the square root method to find the real or imaginary solutions:

to find the real or imaginary solutions: $2x^2 + 5 = 41$ b) $\boxed{J} = 3(x-1)^2 = 36$ c) $\boxed{K} = 2(x-6)^2 = 45 = 53$ $2x^2 = 36$ $\boxed{(x-1)^2 = \sqrt{-12}}$ $\boxed{(x-1)^2 = \sqrt{-12}}$ $\boxed{(x-6)^2} = 98$ $\boxed{(x-6)^2} = 98$

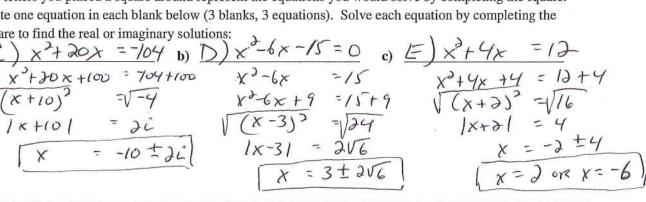
The letters you placed a square around represent the equations you would solve by completing the square 4. Write one equation in each blank below (3 blanks, 3 equations). Solve each equation by completing the square to find the real or imaginary solutions

$$\begin{array}{ccc}
x^{3}+30x+100 & = 704+10 \\
V(x+10)^{2} & = V-4 \\
Ix+10I & = 3c
\end{array}$$

$$\begin{bmatrix}
x & = -10 & = 3c
\end{bmatrix}$$

$$x^{3}-6x = -15$$

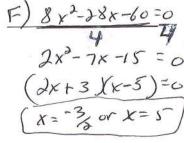
 $x^{3}-6x+9 = 15+9$
 $\sqrt{(x-3)^{2}} = \sqrt{34}$
 $1x-31 = 2\sqrt{6}$
 $x = 3 \pm 2\sqrt{6}$



The letters you placed a triangle around represent the equations you would solve by factoring. Write one 5. equation in each blank below (3 blanks, 3 equations). Solve each equation by factoring to find the real or imaginary solutions:

a) B) $3x^3 + 17x$	=-/
3x2+17x +10	= 0
(3x+2)(x+5)	=0
x=-33 or x=-	5/

7



- The letters you placed a triangle around represent the equations you would solve by factoring. Write one equation in each blank below (3 blanks, 3 equations). Solve each equation using the quadratic formula to find the real or imaginary solutions:

- find the real or imaginary solutions: a) G 3x + 6x + 2 = 0 b) H $6x^2 8x = -3$ c) L $5x^2 13x + 6 = 0$ a = 3, b = 6, c = 2 $6x^2 8x + 3 = 0$ a = 5, b = 73, c = 6 $x = \frac{-6 \pm \sqrt{(6)^2 4(3)(2)}}{2(3)}$ $x = \frac{8 \pm \sqrt{(-8)^2 4(6)(3)}}{2(6)}$ $x = \frac{13 \pm \sqrt{(-13)^2 + 4(5)(6)}}{2(5)}$ $x = \frac{8 \pm \sqrt{-8}}{6}$ $x = \frac{8 \pm 2i\sqrt{2}}{12}$ $x = \frac{13 \pm \sqrt{49}}{10} = \frac{13 \pm 7}{10}$ Simplify. $x = \frac{4 \pm i\sqrt{2}}{6}$

 - a) $-4 \pm \sqrt{50}$ b) $\frac{3 \pm \sqrt{81}}{12}$ c) $\frac{-6 \pm \sqrt{-45}}{3}$ d) $\frac{7 \pm \sqrt{-12}}{14}$ $-4 \pm \sqrt{50}$ $\frac{3 \pm 9}{12} = \frac{13}{13} a^{-\frac{1}{12}}$ $\frac{6 \pm \sqrt{7 \cdot 9 \cdot 5}}{3} = \frac{7 \pm \sqrt{7 \cdot 4 \cdot 3}}{7 \pm \sqrt{14}}$ $\frac{7 \pm \sqrt{2} \cdot \sqrt{3}}{14}$
- A ball is thrown off of a rooftop 200 feet high with an initial velocity of 40 feet per second. The equation 8. $h(t) = -16t^2 + 40t + 200$ represents the height of the ball h after t seconds. Write and solve the equation you would use to determine when the ball would hit the ground. $-16t^2+40++300=0$

$$-16t^{2}+40t+200=0$$

$$2t^{2}-5t-25=0$$

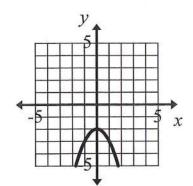
$$(2t+5)(t-5)=0$$

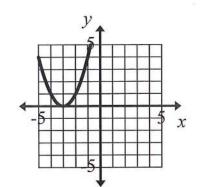
$$t=-52, t=5 second 5 / extraneous$$

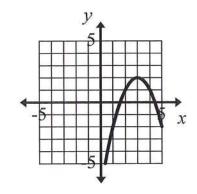
A water balloon is catapulted into the air. The height h of the balloon in meters is represented by the equation $h(t) = -4.9t^2 + 27t + 2.4$ where t represents the time in seconds. Write and solve the equation you would use to determine when the balloon would hit the ground.

and use to determine when the balloon would intuit ground. $-4.9 t^{2} + 27 t + 2.4 = 0 \qquad x = \frac{27}{4} + \sqrt{(-27)^{2} - 4(4.9)(-2.4)} + \sqrt{(4.9)} + \sqrt{(4.9$

10. Use the graph to determine if the discriminant is positive, negative, or zero. State the type of solutions the parabola has and how many solutions there are.







Pos/Neg/Zero: Neg/Zero: Pos/Neg/Zero: Pos/Neg/Zero: Pos/Neg/Zero:

of Solutions:

of Solutions: # of Solutions: 2

Type of solutions: Imaginary Type of solutions: Real, Rational Type of solutions: Real

11. Determine the discriminant of each quadratic function. State how many solutions the equation will have and what type of solutions they will be.

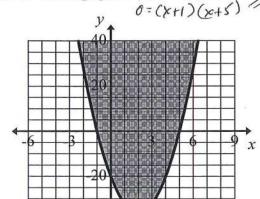
1-4-20 2--16

- a) $a(x) = x^2 + 2x + 5$ b) $b(x) = 5x^2 x 13$ c) $c(x) = 4x^2 4x + 1$ a = 4 + 5 = -1 + 260c) $c(x) = 4x^2 4x + 1$ a = 4 + 5 = -1 + 260c) $c(x) = 4x^2 4x + 1$ a = 4 + 5 = -1 + 260d = $(-1)^2 4(1)(1)$ d = $(-1)^2 4(1)(1)$ e = $(-1)^2 4(1)(1)$

Discriminant: 76 Discriminant: 26 / Discriminant: 0 # of Solutions: 4 # of Solutions: 4 # of Solutions: 1

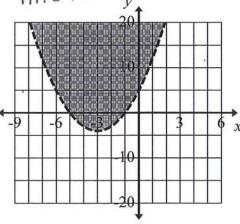
d)

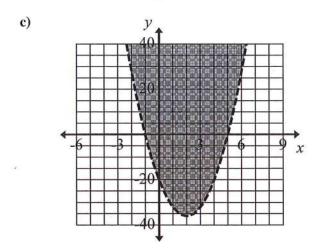
Unit 5 Review Materials

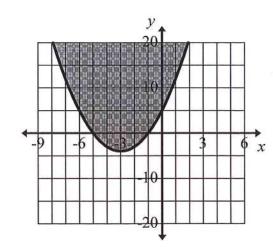


12. Which is the correct graph of $y > x^2 + 6x + 5$?

a) y = (x+1)(x+5)(b) y = (x+1)(x+5) y = (x+1)(x+5)

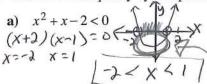






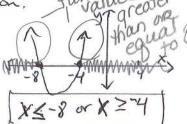
- 13. Use the graph above to write the solution to the inequality: $x^2 + 6x + 5 < 0$.
- 14. List below the 4 steps that you should follow to solve a quadratic inequality.
 - > Algebraically find the x-intercepts
 - > Sketch the graph of a purabola that has those x-intercepts and opens up if a >0 or down if a <0, Also determine dashed or solid line.
 > Identify the x values for which the graph lies below the x-axis (#15a) or above (or an) the x-axis (#15b).

 - > For & or =, include the x-intercepts in the solution.
- 15. Solve each inequality by completing the 4 steps stated above.



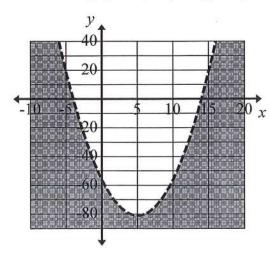


Sunction b) $x^2 + 12x \ge -32$ $x^2 + 12x \ge -32$ $x^2 + 12x \ge -32$ $x + 12x \ge -32$

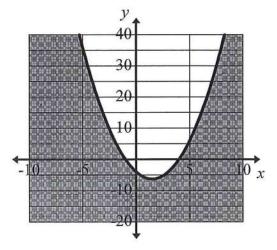


16. Which is the correct graph of $y \le (x-4)(x+1)$? Graph _______

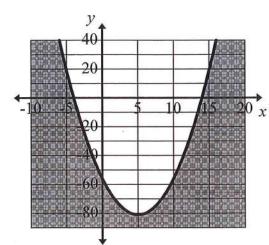
a)



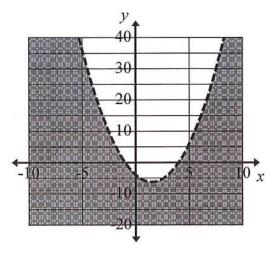
b)



c)



d)



17. Use the graph above to write the solution to the inequality:
$$(x-4)(x+1) \ge 0$$
.

Unit 5 Review

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