Horizontal and Slant Asymptotes

Introduction to Calculus

1) Find the equations of the horizontal or slant asymptotes of the following rational functions.

$$f(x) = \frac{2x+1}{x-3}$$

$$f(x) = \frac{x^2 + x}{2x^2 - 5x + 1}$$

$$f(x) = \frac{5x-2}{x^2+x}$$

$$f(x) = \frac{6x^3 - 8x^2 + 5x + 4}{x^2 - x}$$

2) Fill in each sentence below.

A rational function will have a horizontal asymptote when ______.

A rational function will have a slant asymptote when ______.

A rational function will have non-linear end behavior when ______.

3) Sketch the following rational functions:

$$f(x) = \frac{x^2 + 4x + 3}{x + 2}$$

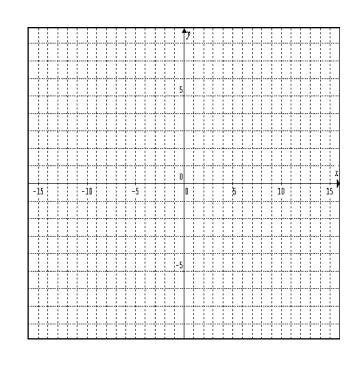
y-intercept:_____ x-intercept:_____

Vertical asymptote(s):_____

$$As x \to \infty$$
, $f(x) \to$

$$A_S x \rightarrow - \alpha, f(x) \rightarrow \underline{\hspace{1cm}}$$

Horizontal or Slant asymptote:



$$f(x) = \frac{2x^2 - x}{x - 1}$$

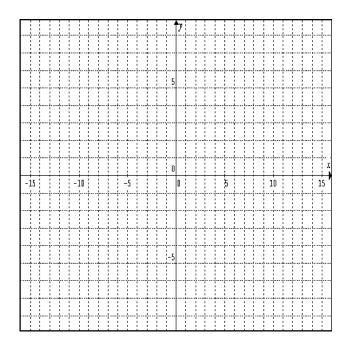
y-intercept:_____ x-intercept:_____

Vertical asymptote(s):_____

$$As x \to \infty$$
, $f(x) \to$

$$As x \to -\alpha, f(x) \to \underline{\hspace{1cm}}$$

Horizontal or Slant asymptote:



$$f(x) = \frac{-x^2 - 2x + 3}{x + 1}$$

y-intercept:_____ x-intercept:_____

Vertical asymptote(s):_____

$$As x \to \infty$$
, $f(x) \to \underline{\hspace{1cm}}$

$$As x \rightarrow - \alpha, f(x) \rightarrow \underline{\hspace{1cm}}$$

Horizontal or Slant asymptote:

