

Name: Key

Date: _____

Block: _____

PART 1: SHORT ANSWERS (points)

- 1) What is the standard equation of the circle with center (2, 3) passing through (0, -1). (points)

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$r = \sqrt{(0 - 2)^2 + (-1 - 3)^2} = \sqrt{20}$$

$$(x - h)^2 + (y - k)^2 = r^2$$

$$(x - 2)^2 + (y - 3)^2 = 20$$

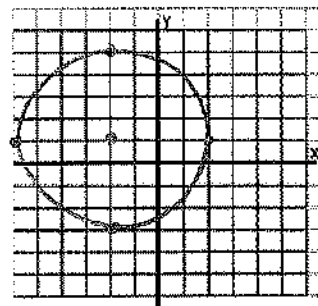
$$r^2 = \sqrt{20^2} = 20$$

- 2) Graph the circle. Label the center and radius. (points)

$$(x + 2)^2 + (y - 1)^2 = 16$$

$$C(-2, 1)$$

$$r = \sqrt{16} = 4$$



- 3) Use $\odot A$ at the right. (points)

- a) What is $m\widehat{BC}$?

$$38^\circ$$

- b) What is $m\widehat{BED}$?

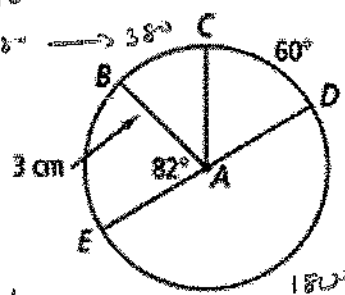
$$82 + 180 = 262^\circ$$

- c) What is the length of $\widehat{CED}$? Leave your answer in terms of π .

$$l = \frac{m}{360} \cdot \pi d = \frac{300}{360} \cdot \pi (6) = 15\pi \text{ cm}$$

$$82 + 60 = 142$$

$$180 - 142 = 38^\circ$$



- 4) Use $\odot C$ at the right. $\overline{DE}$ is tangent to $\odot C$. (points)

- a) If $DE = 8$ and $EF = 4$, what is the radius?

$$a^2 + b^2 = c^2$$

$$r^2 + 8^2 = (r + 4)^2$$

$$r^2 + 64 = r^2 + 8r + 16$$

$$-r^2 - 64 - r^2 - 8r - 16$$

$$0 = 8r - 48 \quad (r + 4)(r + 4)$$

$$+48 \quad +48 \quad r^2 + 4r + 4r + 16$$

$$48 = 8r \quad r^2 + 8r + 16$$

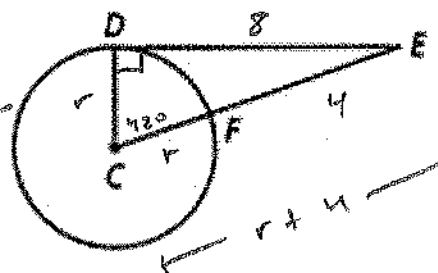
$$\frac{48}{8} = \frac{8r}{8}$$

$$6 = r$$

- b) If $m\angle C = 42^\circ$, what is the $m\angle E$?

$$90 + 42 = 132$$

$$180 - 132 = 48^\circ$$



- 5) Use $\odot P$ at the right. $m\widehat{QR} = 100^\circ$. (points)

- a) What is $m\widehat{ST}$? How do you know?

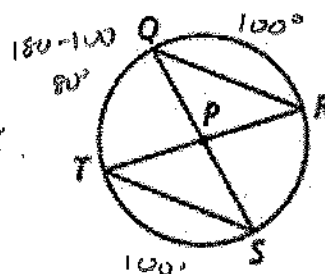
$$m\widehat{ST} = 100^\circ \quad \angle QPR \cong \angle TPS \text{ by Vertical } \angle's.$$

They are central $\angle$'s, so their intercepted arcs are $\cong$.

- b) What is $m\angle QPT$? How do you know?

$$\angle QPT = 80^\circ \quad \widehat{QRS} \text{ is a semicircle, so}$$

$$m\widehat{QT} = 180 - 100 = 80^\circ \quad \text{Since } \angle QPT \text{ is a central } \angle, \text{ it is } \cong \text{ to its intercepted arc.}$$



6) Lines that appear tangent are tangent. Find x , y , and z . (points)

$$x \cdot 8 = 12 \cdot 4$$

$$\frac{8x}{8} = \frac{48}{8}$$

$$x = 6$$

2 Chords

$$y = \frac{1}{2}(80 + 100)$$

$$y = \frac{1}{2}(180)$$

$$y = 90$$

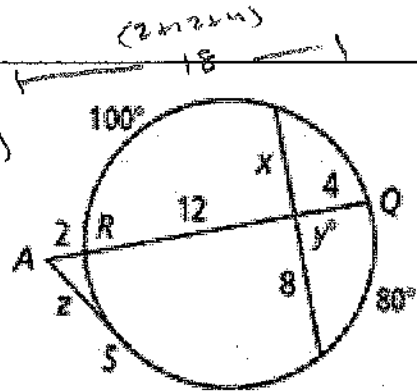
$\angle$ In

$$z \cdot z = (18)(2)$$

$$z^2 = 36$$

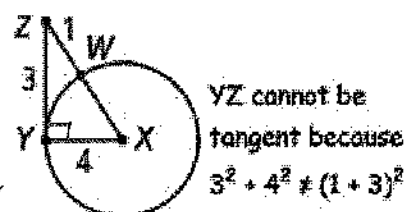
$$z = 6$$

tangent / secant



7) A classmate insists that $\overline{YZ}$ is not tangent to $\odot X$. Explain your classmate's error. (points)

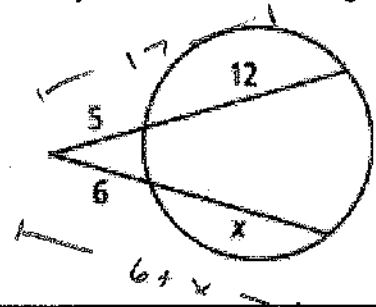
$(1+3)$ is not the hypotenuse. The radius is 4, so the hypotenuse should be $(1+4)$.



Explain your classmate's error

8) A classmate insists that the value of x is 10. Write and solve an equation to show that your classmate is wrong. (points)

My classmate did not use the entire length of each secant. He created the equation $6 \cdot x = 5 \cdot 12$. However, he should have used $6(6+x) = 5(17)$.



PART 2: EXTENDED RESPONSE (points)

$\square ABCD$ is inscribed in $\odot O$. (Draw a picture)

a) Explain why $\angle A$ and $\angle B$ are right angles.

$\angle A \cong \angle C$ and $\angle B \cong \angle D$ (Opp $\angle$ s of $\square$ are $\cong$)

$\angle A$ is supp. to $\angle C$ and $\angle B$ is supp. to $\angle D$ (Opp $\angle$ s of Inscribed Quad are $\cong$)

$\angle A, \angle B, \angle C, \angle D$ are right $\angle$ s ($\angle$ s $\cong$ and supp are rt. $\angle$ s)

b) Explain why $\overline{AC} \cong \overline{BD}$.

$ABCD$ is a rectangle ($\square$ with 4 rt. $\angle$ s)

Therefore, $\overline{AC} \cong \overline{BD}$ (Diags of a rectangle are $\cong$).

