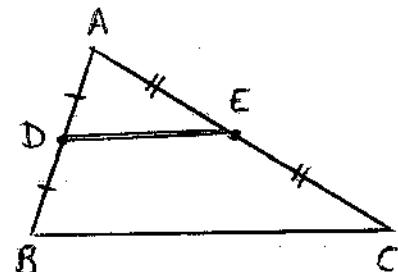
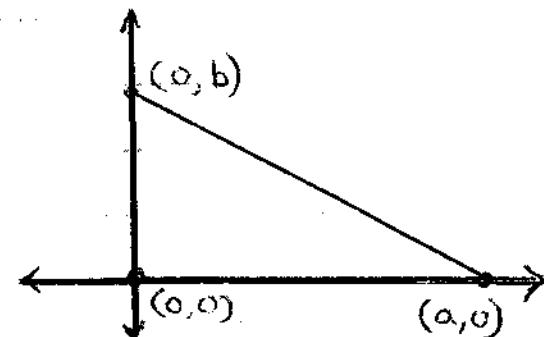


Geometry Ch 5-1 Exer, pg 300 #1-11, 12-18 (even), 21-26

1. In $\triangle ABC$, D is the midpoint of \overline{AB} , and E is the midpoint of \overline{AC} .
 \overline{DE} is a midsegment of $\triangle ABC$.



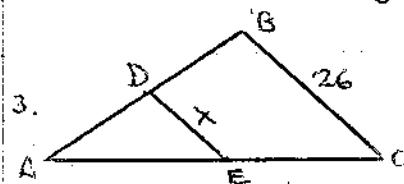
2. Explain why it is convenient to place a right triangle as shown when writing a coord. proof. How might you want to re-label the vertices if the proof involves mid-points?



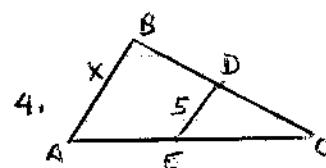
Try to get as many points on x- and y-axis so coordinate values are zero. This makes for easier calculations.

When working with midpoints proofs consider setting vertices at $(0, 2b)$ and $(2a, 0)$. This way your mid-point coordinates won't be fractions.

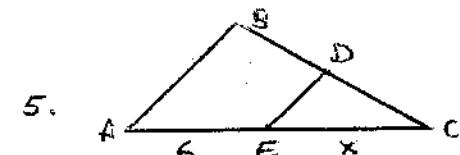
- If \overline{DE} is a midsegment of $\triangle ABC$, find the value of x.



$$x = 13, \text{ half of } \overline{BC}$$



$$x = 10, \text{ twice midsegment } \overline{DE}$$

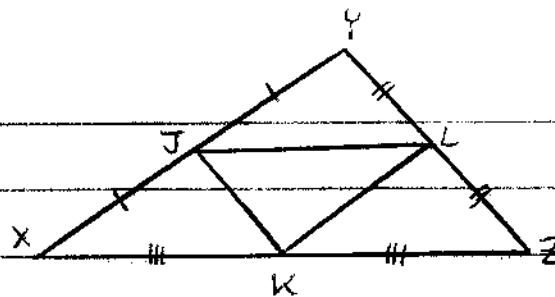


$$x = 6, E \text{ must be a midpt of } \overline{AC}$$

In $\triangle XYZ$, $\overline{XJ} \cong \overline{JY}$,

$$\overline{YL} \cong \overline{LZ},$$

$$\overline{XK} \cong \overline{KZ}$$



6. $\overline{JK} \parallel \overline{YZ}$ [Also \overline{YL} and \overline{LZ}]

7. $\overline{JL} \parallel \overline{XZ}$ [also \overline{XK} and \overline{KZ}]

8. $\overline{XY} \parallel \overline{KL}$

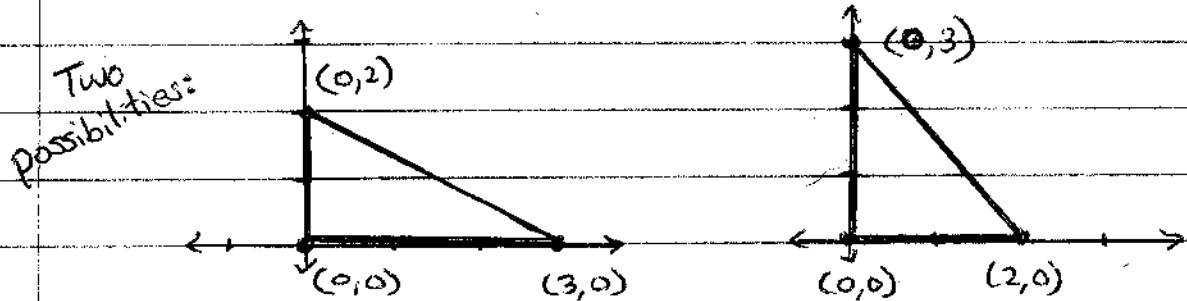
9. $\overline{YJ} \cong \overline{XJ}$ and \overline{KL}

10. $\overline{JL} \cong \overline{XK}$ and \overline{KZ} and \overline{XZ} 11. $\overline{JK} \cong \overline{YL}$ and \overline{LZ} and \overline{YZ}

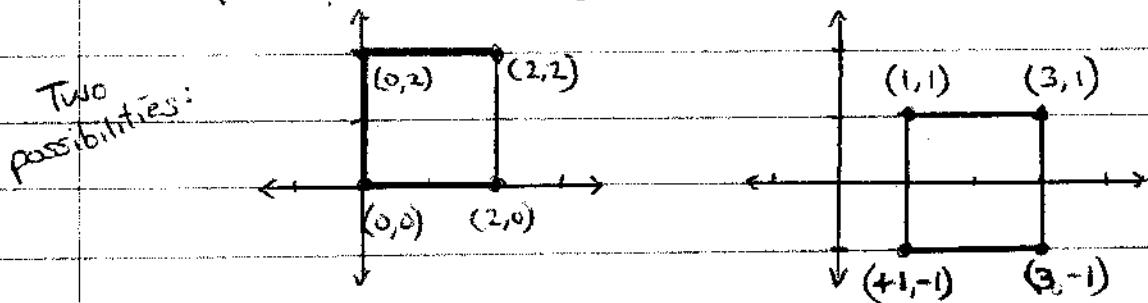
Place the figure in a coordinate plane. Assign coordinates to each vertex.

[There are infinitely many correct answers!
Try to choose a "convenient location."]

12. Right Triangle: leg lengths are 2 and 3.

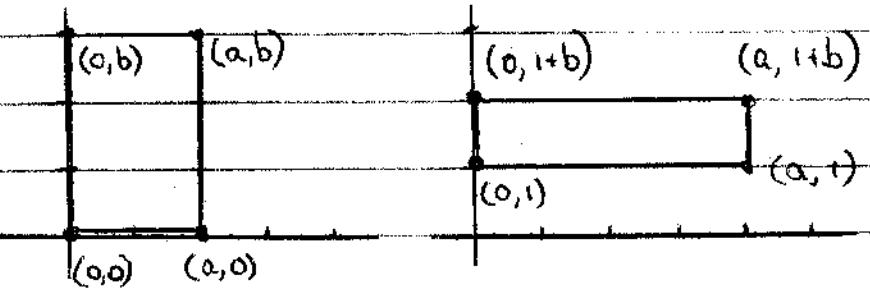


14. Square: side length is 2.



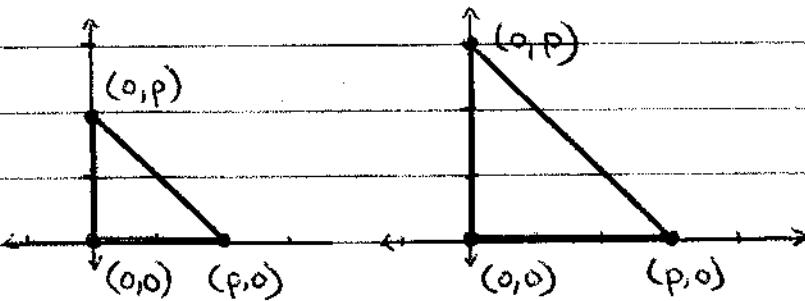
16. Rectangle: length is a , width is b .

No way to know
which is
greater
 a or b ?



18. Isosceles right triangle: leg length is p .

Two possibilities:



Sketch $\triangle ABC$. Find length/slope of each side; mid point coordinates.

Is $\triangle ABC$ right? Is $\triangle ABC$ isosceles? [variables are positive with $p \neq q, m \neq n$]

21. $A(0,0)$, $B(p,q)$, $C(2p,0)$

Lengths:

$$m\bar{AC} = 2p$$

$$m\bar{AB} = \sqrt{(p-0)^2 + (q-0)^2} = \sqrt{p^2 + q^2}$$

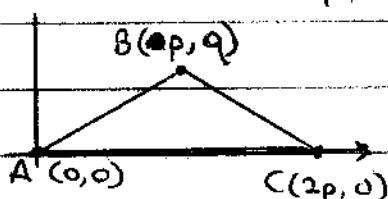
$$m\bar{BC} = \sqrt{(2p-p)^2 + (0-q)^2} = \sqrt{p^2 + q^2}$$

Slopes

$$AC: \frac{0-0}{2p-0} = \frac{0}{2p} = 0$$

$$AB: \frac{q-0}{p-0} = \frac{q}{p}$$

$$BC: \frac{0-q}{2p-p} = \frac{-q}{p}$$



Midpoints:

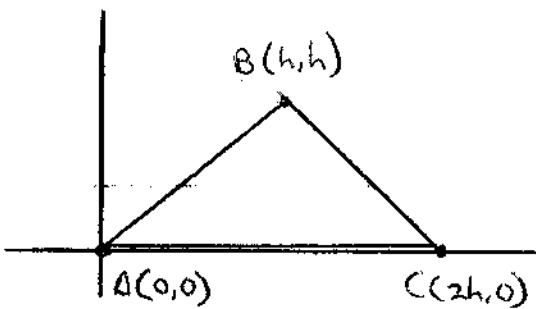
$$AC: \left(\frac{0+2p}{2}, \frac{0+0}{2} \right) = (p, 0)$$

$$AB: \left(\frac{0+p}{2}, \frac{0+q}{2} \right) = \left(\frac{p}{2}, \frac{q}{2} \right)$$

$$BC: \left(\frac{p+2p}{2}, \frac{q+0}{2} \right) = \left(\frac{3p}{2}, \frac{q}{2} \right)$$

Not Right; It is Isosceles

22. $A(0,0)$, $B(h,h)$, $C(2h,0)$



Lengths:

$$AB: \sqrt{(h-0)^2 + (h-0)^2} = \sqrt{2h^2} = h\sqrt{2}$$

$$BC: \sqrt{(2h-h)^2 + (0-h)^2} = \sqrt{h^2 + h^2} = \sqrt{2h^2} = h\sqrt{2}$$

$$AC: 2h$$

Slopes:

$$AB = \frac{h-0}{h-0} = \frac{h}{h} = 1$$

$$BC = \frac{h-0}{h-2h} = \frac{h}{-h} = -1$$

$$AC = \frac{0-0}{2h-0} = \frac{0}{2h} = 0$$

Midpoints:

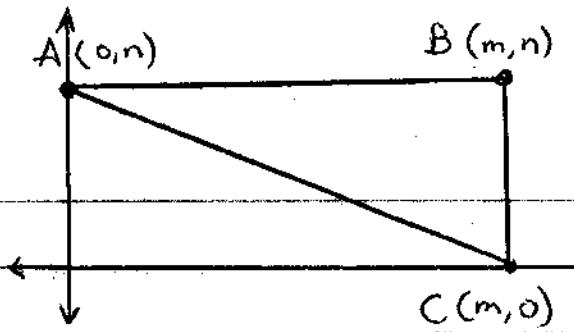
$$AB: \left(\frac{0+h}{2}, \frac{0+h}{2}\right) = \left(\frac{h}{2}, \frac{h}{2}\right)$$

$$BC: \left(\frac{h+2h}{2}, \frac{h+0}{2}\right) = \left(\frac{3h}{2}, \frac{h}{2}\right)$$

$$AC: \left(\frac{0+2h}{2}, \frac{0+0}{2}\right) = (h, 0)$$

$\triangle ABC$ is Right because slope of \overline{AB} and \overline{BC} are negative reciprocals.

$\triangle ABC$ is Isosceles because the measure of \overline{AB} is equal to \overline{BC}



23. $A(0,n)$, $B(m,n)$, $C(m,0)$

Lengths:

$$AB = m$$

$$BC = n$$

$$AC = \sqrt{(0-m)^2 + (n-0)^2} = \sqrt{m^2 + n^2}$$

Slopes:

$$AB = \frac{n-0}{m-0} = \frac{0}{m} = 0$$

$$BC = \frac{n-0}{m-m} = \frac{n}{0} = \text{undefined}$$

$$AC = \frac{n-0}{0-m} = -\frac{n}{m}$$

Midpoints:

$$\overline{AB}: \left(\frac{0+m}{2}, \frac{n+0}{2}\right) = \left(\frac{m}{2}, \frac{2n}{2}\right) = \left(\frac{m}{2}, n\right)$$

$$\overline{BC}: \left(\frac{m+m}{2}, \frac{n+0}{2}\right) = \left(\frac{2m}{2}, \frac{n}{2}\right) = \left(m, \frac{n}{2}\right)$$

$$\overline{AC}: \left(\frac{0+m}{2}, \frac{n+0}{2}\right) = \left(\frac{m}{2}, \frac{n}{2}\right)$$

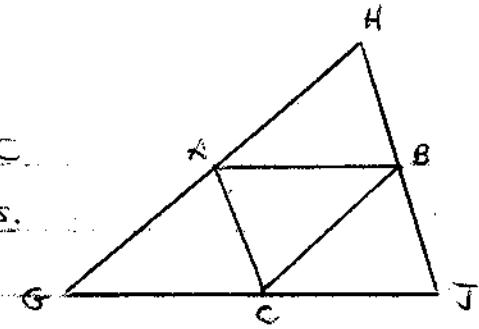
$\triangle ABC$ is right \overline{AB} is a horizontal segment

while \overline{BC} is a vertical segment.

There intersection is at a perpendicular,
creating a right angle.

$\triangle ABC$ is not isosceles; no two sides are
the same length.

ALGEBRA: Use $\triangle GHJ$, where A, B, and C are midpoints of the sides.



24. If $AB = 3x + 8$ and $GJ = 2x + 24$, what is AB ?

$$2AB = GJ$$

$$2(3x + 8) = 2x + 24$$

$$6x + 16 = 2x + 24$$

$$4x = 8$$

$$\boxed{x = 2}$$

$$AB = 3(2) + 8$$

$$= 6 + 8$$

$$\boxed{AB = 14}$$

25. If $AC = 3y - 5$ and $HJ = 4y + 2$, what is HB ?

$$2AC = HJ$$

$$2(3y - 5) = 4y + 2$$

$$6y - 10 = 4y + 2$$

$$2y = 12$$

$$\boxed{y = 6}$$

$$HJ = 4(6) + 2$$

$$HJ = 26$$

$$HB = \frac{1}{2} HJ = \frac{1}{2}(26)$$

$$\boxed{HB = 13}$$

26. If $GH = 7z - 1$ and $BC = 4z - 3$, what is GH ?

$$GH = 2BC$$

$$7z - 1 = 2(4z - 3)$$

$$7z - 1 = 8z - 6$$

$$\boxed{5 = z}$$

$$GH = 7(5) - 1$$

$$= 35 - 1$$

$$\boxed{GH = 34}$$