

Show all work for each problem.

①

x	$f(x)$	$g(x)$	$f'(x)$
-4	0	-9	5
-2	4	-7	4
0	6	-4	2
2	7	-3	1
4	10	-2	3

The table above gives values of the differentiable functions f and g , and f' , the derivative of f , at selected values of x . If $g(x) = f^{-1}(x)$, what is the value of $g'(4)$?

- (A) $-\frac{1}{3}$ (B) $-\frac{1}{4}$ (C) $-\frac{3}{100}$ (D) $\frac{1}{4}$ (E) $\frac{1}{3}$

②

Let f be the function defined by $f(x) = x^3 + x$. If $g(x) = f^{-1}(x)$ and $g(2) = 1$, what is the value of $g'(2)$?

- (A) $\frac{1}{13}$ (B) $\frac{1}{4}$ (C) $\frac{7}{4}$ (D) 4 (E) 13

- ③ Let f be a differentiable function such that $f(3) = 15$, $f(6) = 3$, $f'(3) = -8$, and $f'(6) = -2$. The function g is differentiable and $g(x) = f^{-1}(x)$ for all x . What is the value of $g'(3)$?
- (A) $-\frac{1}{2}$
- (B) $-\frac{1}{8}$
- (C) $\frac{1}{6}$
- (D) $\frac{1}{3}$
- (E) The value of $g'(3)$ cannot be determined from the information given.

- ④ The functions f and g are differentiable, and $f(g(x)) = x$ for all x . If $f(3) = 8$ and $f'(3) = 9$, what are the values of $g(8)$ and $g'(8)$?
- (A) $g(8) = \frac{1}{3}$ and $g'(8) = -\frac{1}{9}$
- (B) $g(8) = \frac{1}{3}$ and $g'(8) = \frac{1}{9}$
- (C) $g(8) = 3$ and $g'(8) = -9$
- (D) $g(8) = 3$ and $g'(8) = -\frac{1}{9}$
- (E) $g(8) = 3$ and $g'(8) = \frac{1}{9}$