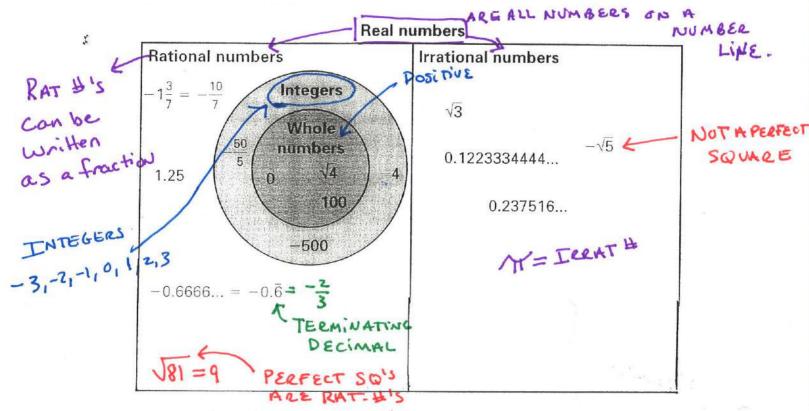
1.1 Lesson Opener

DATE:

REAL NUMBERS AND NUMBER OPERATIONS

The Venn diagram below shows subsets of the real numbers, the numbers used most often in algebra.



- Simplify $\frac{6}{3}$. Is $\frac{6}{3}$ an integer? Is it a whole number?
- 2 All terminating decimals (such as 1.25) and all repeating decimals (such as $0.\overline{6}$) can be written as the ratio of two integers. How can you write 1.25 and $0.\overline{6}$ as ratios?
- 3 Place each number in the correct region of the diagram.

For use with pages 3-10

田山山島

Use a number line to graph and order real numbers and identify properties of and use operations with real numbers

VOCABULARY

The graph of a real number is the point on a real number line that corresponds to the number. On a number line, the numbers increase from left to right, and the point labeled 0 is the origin.

The number that corresponds to a point on a number line is the coordinate of the point.

The opposite, or additive inverse, of any number a is -a.

The reciprocal, or multiplicative inverse, of any nonzero number a is $\frac{1}{a}$.

EXAMPLE 1

Graphing and Ordering Real Numbers

Graph and write the numbers in increasing order: $-\sqrt{7}$, 0, $\frac{3}{2}$, 2, $\frac{3}{8}$.

$$-\sqrt{7} \approx -2.6, \frac{3}{2} = 1.5, \frac{3}{8} \approx 0.4$$

$$-\sqrt{7}$$

$$\frac{3}{8}$$

$$\frac{3}{2}$$

SOLUTION $-\sqrt{7} \approx -2.6, \frac{3}{2} = 1.5, \frac{3}{8} \approx 0.4$ Rewrite each number in decimal form. $-\sqrt{7}$ $\frac{3}{8}$ $\frac{3}{2}$ $\frac{1}{-3}$ Plot the points on the real number line.

Write the numbers from least to greatest.

Exercises for Example 1

Write the numbers in increasing order.

1. $1, \frac{1}{3}, \sqrt{2}$ 2. $\frac{3}{5}, -1, 1$ 3. $\sqrt{5}, \frac{2}{3}, 3.25$ 4. -4, 1, -13. $\sqrt{5}, \frac{2}{3}, 3.25$ 4. -4, 1, -1Write the numbers in increasing order.

1.
$$1, \frac{1}{2}, \sqrt{2}$$

2.
$$\frac{3}{5}$$
, -1 , 1

3.
$$\sqrt{5}$$
 $\frac{2}{5}$ 3 25

5.
$$0, -2, \frac{1}{3}$$

6.
$$-\sqrt{2}$$
, -15 , 5.7

7.
$$\frac{5}{2}$$
, -5 , -10

For use with pages 3-10

Identifying Properties of Real Numbers

PROPERTIES

Identify the property shown.

a.
$$5(10 + 2) = 5 \cdot 10 + 5 \cdot 2$$

b.
$$(6 \cdot 4)5 = 6(4 \cdot 5)$$

SOLUTION

a. Distributive property

b. Associative property of multiplication

Exercises for Example 2

Identify the property shown.

9.
$$5 + 3 = 3 + 5$$

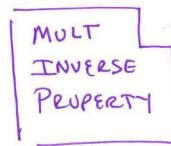
COMMUNATIVE PEOPERTY

11.
$$-2 + \underline{0} = -2$$

ADDITION

IDENTITY PROPERTY

13.
$$8 \cdot \frac{1}{8} = 1$$
 reciproce



10.
$$7 + (-7) = 0$$

ADDITION INVERSE
PERTY

12.
$$2(x+1) = 2 \cdot x + 2 \cdot 1$$

 $5(x-6) = 5 \cdot x + 5(-6)$

DISTRIBUTIVE PROPERTY

14.
$$(5+7)+3=5+(7+3)$$

& NOTICE H'S ARE IN THE SAME OLDER

* ()'S CHANGE

ASSINCIATIVE PROPERTY



For use with pages 3-10

(主任山田里)

Operations with Real Numbers

UNIT ANALYSIS

At rest, the average person's heart beats 65 times per minute. During aerobic exercise, this rate increases by 40%.

- (a) How many times does the average person's heart beat per hour?
- b. How many times will the average person's heart beat per minute during aerobic exercise?

Example

SOLUTION

a.
$$\left(\frac{65 \text{ beats}}{1 \text{ minute}}\right) \left(\frac{60 \text{ minutes}}{1 \text{ hour}}\right)$$

3900 beats per hour

(b) To find 40% of 65, multiply.

Rewrite 40% as 0.4.

Simplify.

91 beat/MIN

During aerobic exercise, the average person's heart would beat 65 + 26 = 91 times per minute.

Exercises for Example 3

In Exercises 15 and 16, use the following information.

At Indianapolis Motor Speedway, one lap is 2.5 miles in length. The average speed of an Indy racing car is 190 miles per hour.

15. Find the length of one lap in yards.

KI: 1 lop = 2. Smiles Rote 190 mph

4.400 Yards

CALC: 2.5 • \$ 280 -3

16. How many seconds would it take to complete one lap?

(ROUND TO Seconds)

47 Seconds

CALC Z.5 .60.60 [enter] - 19

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47. 3

For use with pages 11-17

Evaluate algebraic expressions and simplify algebraic expressions by combining like terms

VOCABULARY "KNOW HIGHLIGHTED WORDS"

A variable is a letter that is used to represent one or more numbers. Ex (x, y...)

An algebraic expression is an expression involving variables. $E \times (x^2 + 4x - 2)$

Like terms are expressions that have the same variable part. Constant terms such as -4 and 2 are also like terms.

The base of an exponent is the number or variable that is used as a factor in repeated multiplication. For example, in the expression 4^b , 4 is the base.

> An exponent is the number or variable that represents the number of times the base is used as a factor. For example, in the expression 4b, b is the exponent.

A power is the result of repeated multiplication. For example, in the expression $4^2 = 16$, 16 is the second power of 4.

Any number used to replace a variable is a value of the variable.

When the variables in an algebraic expression are replaced by numbers, the result is called the value of the expression. EVALUATE

Terms are the parts that are added in an expression, such as 5 and -x in the expression 5 - x. Ex: x2+4x - 2 has 3 terms x2, 4x, -2

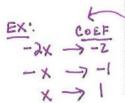
A coefficient is the number multiplied by a variable in a term.

Two algebraic expressions are equivalent if they have the same value for all values of their variable(s).

LIKE TEEMS Same & variables + EXPONENTS EX] 2x2, -2 x2

> THIS IS CALLED SUBSTITUTION"

> > EXPRESSIONS TO FIND THE VALUE OF THE EXPRESSION.



EXAMPLE 1)

Using Order of Operations

$$2(3 + 18 \div 3^2 - 7) = 2(3 + 18 \div 9 - 7)$$

= $2(3 + 2 - 7)$

= 2(-2)

Divide.

Evaluate the power.

Add within parentheses.

Multiply.

PEMDAS 02 (D ()'S INSIDE FOUT (D EXPONENTS

(3) X, ÷ L→R

(+, - L -> R

Exercises for Example 1

Evaluate the expression.

4.
$$5 - (-2 + 4)^2$$

$$5 - (2)^2$$

$$5 - 4$$

5.
$$36 \div (-3)^2 - 1$$

5.
$$36 \div (-3)^2 - 1$$
 36. $-6^2 = -25$ 4-1

For use with pages 11-17

EXAMPLE 2)

Evaluating an Algebraic Expression

Evaluate $2t^2 - 3$ when t = 4.

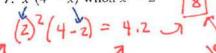
SOLUTION

$$2t^2 - 3 = 2(4)^2 - 3$$
 Substitute 4 for t.
 $= 2(16) - 3$ Evaluate the power.
 $= 32 - 3$ Multiply.
 $= 29$ Subtract.

Exercises for Example 2

Evaluate the expression.

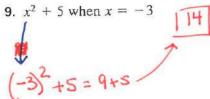
7. $x^2(4-x)$ when x=2



(1) Show

Rememberuse





$$x^2 + 5$$
 when $x = -3$

11.
$$4x - 3y + 2$$
 when $x = 4$ and $y = -3$
12. $9(m - n)^2$ when $m = 4$ and $n = 1$

$$4(4) - 3(-3) + 2 = 9(3)^2 = 9(3)$$

EVALUATING EXPONENTS

$$(-2)^3 = -2 \cdot -2 \cdot -2 = 68$$

ODD EXPONENT-RESULT

> Result is (-)

8.
$$x - (x + 5)$$
 when $x = 20$

10.
$$3x^3 + 4$$
 when $x = -2$

$$3(-2)^3 + 4 = 3(-8) + 4 = 3(-8)$$

12.
$$9(m-n)^2$$
 when $m=4$ and $n=1$

$$9(4-1)^2 = 9(3)^2 = 9.9 = 181$$

For use with pages 11-17

EXAMPLE 3

Simplifying by Combining Like Terms

Simplify 6(x - y) - 4(x - y).

SOLUTION

$$6(x - y) - 4(x - y) = 6x - 6y - 4x + 4y$$

$$= (6x - 4x) + (-6y + 4y)$$

$$= 2x - 2y$$
Distributive property

Group like terms.

Exercises for Example 3

Simplify the expression.

13.
$$7x - (9x + 5)$$

$$7x - 9x - 5 =$$

$$-2x - 5$$

14.
$$2(n^2 + n) - 5(n^2 - 4n)$$

IMPORTANTORDER TERMS: H > L EXPONENTS; CONSTANTICIT

15. $-6x^2 + 4x - x^2 + 15x$ 16. 7x - 2y + 3 - 9y + 4 + 5x

15.
$$-6x^2 + 4x - x^2 + 15x$$

16.
$$7x - 2y + 3 - 9y + 4 + 5x$$

For use with pages 19-24

(GOAL)

Solve linear equations and use linear equations to answer questions about real-life situations

SOLUE Equation

TO FIND THE VALUE OF THE UARIABLE. VOCABULARY

An equation is a statement in which two expressions are equal.

A linear equation in one variable is an expression that can be written in the form ax = b where a and b are constants and $a \ne 0$.

A number is a solution of an equation if the statement is true when the number is substituted for the variable.

Two equations are equivalent if they have the same solutions.

EXAMPLE 1

Variable on One Side

Solve -19 = -2y + 5.

SOLUTION

$$-19 = -2y + 5$$

Write original equation.

$$-24 = -2y$$

To isolate y, subtract 5 from each side.

$$12 = y$$

Divide each side by -2.

Exercises for Example 1

SOLUE AND CHECK

Solve the equation.

ALWAYS Check IN Original eQ!

 $\frac{+2}{5} = 1$ $\boxed{X = -1}$

2. -18 = y + 6 y = -24

3. 9 - z = 5 -9 -2 = 4 -2 = -4 -1 -1 -1

7 3=3/

use calc to check! 4. 6 + 6x = -12

$$\frac{4x = -18}{6}$$

$$\chi = -3$$

5. 2x - 5 = 1

 $6.\frac{x}{3} = (2)^{-3} \times - -6$

Multiply by the reciprocal

For use with pages 19-24

Variable on Both Sides

STEP1: GET VARIABLE ON THE SAME SIDE

Solve 4x - 2x = 15 - 3x.

STEPZ: UNDO +,

SOLUTION

STEPS: UNDO X, -

4x - 2x = 15 - 3x

2x = 15 - 3x

Write original equation.

STEP4: ALL WAYS CHECK

Combine like terms.

IN ORIGINAL EQ!

5x = 15

To collect the variable terms, add 3x to each side.

USE CALC!

x = 3

Divide each side by 5.

Exercises for Example 2

Solve the equation.

7. 15 - 3a = -4d + 16

C: 6=6V

C: -8=-8V

ALWAYS SIMPLIFT IF POSSIBLE

C: -18=-180

EXAMPLE 3 Using the Distributive Property

Solve 15(4 - y) = 5(10 + 2y).

SOLUTION

$$15(4 - y) = 5(10 + 2y)$$
 Write original equation.

$$60 - 15y = 50 + 10y$$
 Distributive property

$$60 = 50 + 25y$$
 To collect the variable terms, add 15y to each side.

$$10 = 25y$$
 Subtract 50 from each side.

$$\frac{2}{5} = y$$
 Divide each side by 25.

WHEN POSSIBLE, SIMPLIFY BOTH SIDES. (NOTICE PINK IS COMPLETELY SIMPLIFIED)

Then follow some steps in Exemple # 2 (prior page)

Exercises for Example 3

13.
$$5(x-3) + 12 = -2(x-2)$$

$$5x - 3 = -2x + 4$$

15.
$$-2x = 2(x + 1)$$

$$-4K+8+3K+3=7$$
 $-K+1V=7$
 $-1V=-4$

16.
$$3x - 9 = 2(x - 5)$$

Solve
$$\frac{2}{3}x + \frac{3}{5} = \frac{4}{15}$$
.

SOLUTION

$$\frac{2}{3}x + \frac{3}{5} = \frac{4}{15}$$

Write original equation.

$$15\left(\frac{2}{3}x + \frac{3}{5}\right) = 15\left(\frac{4}{15}\right)$$

Multiply each side by the LCD, 15.

$$10x + 9 = 4$$

Distributive property

$$10x = -5$$

To isolate x, subtract 9 from each side.

$$x = -\frac{1}{2}$$

Divide each side by 10.

$$\frac{1}{5}(25x - 10) = 18$$

Exercises for Example 4

Solve the equation.
17.
$$6n = \frac{2}{3}(5n - 2)$$
 $N = -1$

$$18. \frac{3}{4}x + 1 = 4$$

$$5\sqrt{19}. \ \frac{1}{2}x - \frac{2}{3} = 4x$$

$$5^{\frac{1}{2}} 19. \ \frac{1}{2}x - \frac{2}{3} = 4x$$

$$\times \frac{19}{20.} \ \frac{3}{5}x = \frac{2}{3}x + 1$$

$$\times \frac{19}{20.} \ \frac{3}{5}x = \frac{2}{3}x + 1$$

$$5^{1}$$
20. $\frac{3}{5}x = \frac{2}{3}x + 1$