## **Chapter Problems**

## Period and Frequency:

### Classwork

- 1. An object is spun around in circular motion such that it completes 100 cycles in 25 s.
  - a. What is the period of its rotation?
  - b. What is the frequency of its rotation?
- 2. An object completes 2500 cycles in 25 s.
  - a. What is the period of its rotation?
  - b. What is the frequency of its rotation?
- 3. An object is spun around in circular motion such that its period is 12s.
  - a. What is the frequency of its rotation?
  - b. How much time will be required to complete 86 rotations?

## Homework

- 4. An object completes 10 cycles in 50 s.
  - a. What is the period of its rotation?
  - b. What is the frequency of its rotation?
- 5. An object is spun around in circular motion such that its frequency is 12 Hz.
  - a. What is the period of its rotation?
  - b. How much time will be required to complete 86 rotations?
- 6. An object is spun around in circular motion such that its frequency is 500 Hz.
  - a. What is the period of its rotation?
  - b. How much time will be required to complete 7 rotations?

# **Velocity and Acceleration**

### Classwork

- 7. A 5.0 kg object is spun around in a circle of radius 1.0 m with a period of 4.0s.
  - a. What is the frequency of its rotation?
  - b. \*What is its velocity?
  - c. \*What is its acceleration?
- 8. A 15.0 kg mass is spun in a circle of radius 5.0 m with a frequency of 25 Hz.
  - a. What is the period of its rotation?
  - b. \*What is its velocity?
  - c. \*What is its acceleration?

- 9. A 0.5 kg object is spun around in a circle of radius 2.0 m with a period of 10.0s.
  - a. What is the frequency of its rotation?
  - b. \*What is its velocity?
  - c. \*What is its acceleration?

- 10. A 500 kg mass is spun in a circle of radius 25 m with a velocity of 250 m/s.
  - a. \*What is the period of its rotation?
  - b. \*What is its frequency?
  - c. What is its acceleration?

## **Dynamics of UCM**

### Classwork

- 11. What is the acceleration of an object that has a velocity of 25 m/s and is moving in a circle of radius 10m?
- 12. An object is experiencing an acceleration of 12 m/s<sup>2</sup> while traveling in a circle at a velocity of 3.1 m/s. What is the radius of its motion?
- 13. A 61 kg object is experiencing a net force of 25 N while traveling in a circle of radius 35 m. What is its velocity?
- 14. A 0.25 kg object is experiencing a net force of 15 N while traveling in a circle at a velocity of 21 m/s. What is the radius of its motion?
- 15. An object is experiencing a centripetal acceleration of 36 m/s<sup>2</sup> while traveling in a circle of radius 15 m. What is its velocity?
- 16. A 61 kg object is experiencing a net force of 250 N while traveling in a circle of radius 1.5 m. What is its velocity?

- 17. An object is experiencing an acceleration of 12 m/s<sup>2</sup> while traveling in a circle of radius 5.0 m. What is its velocity?
- 18. What is the net force acting on a 5.0 kg object that has a velocity of 15 m/s and is moving in a circle of radius 1.6m?
- 19. What is the acceleration of an object that has a velocity of 37 m/s and is moving in a circle of radius 45m?
- 20. An object is experiencing a centripetal acceleration of 2.0 m/s<sup>2</sup> while traveling in a circle at a velocity of 0.35 m/s. What is the radius of its motion?
- 21. What is the net force acting on a 52 kg object that has a velocity of 17 m/s and is moving in a circle of radius 1.6m?
- 22. A 6.8 kg object is experiencing a net force of 135 N while traveling in a circle at a velocity of 45 m/s. What is the radius of its motion?

### **General Problems**

#### **Class Work**

- 23. A 0.65 kg ball is attached to the end of a string. It is swung in a vertical circle of radius 0.50 m. At the top of the circle its velocity is 2.8 m/s.
  - a. Draw a free body diagram for the ball when it is at the top of the circle. Next to that diagram indicate the direction of its acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the Tension in the string.
  - c. Solve those equations for the Tension in the string.
- 24. A 0.65 kg ball is attached to the end of a string. It is swung in a vertical circle of radius 0.50 m. At the bottom of the circle its velocity is 2.8 m/s.
  - a. Draw a free body diagram for the ball when it is at the bottom of the circle. Next to that diagram indicate the direction of its acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the Tension in the string.
  - c. Solve those equations for the Tension in the string.

- 25. A 0.25 kg ball is attached to the end of a string. It is swung in a vertical circle of radius 0.6 m. At the top of the circle its velocity is 3 m/s.
  - a. Draw a free body diagram for the ball when it is at the top of the circle. Next to that diagram indicate the direction of its acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the Tension in the string.
  - c. Solve those equations for the Tension in the string.
- 26. A 0.25 kg ball is attached to the end of a string. It is swung in a vertical circle of radius 0.6 m. At the bottom of the circle its velocity is 3 m/s.
  - a. Draw a free body diagram for the ball when it is at the bottom of the circle. Next to that diagram indicate the direction of its acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the Tension in the string.
  - c. Solve those equations for the Tension in the string.

### **Class Work**

- 27. \*A ball is attached to the end of a string. It is swung in a vertical circle of radius 1.5 m. What is the minimum velocity that the ball must have to make it around the circle?
- 28. \*A ball is attached to the end of a string. It is swung in a vertical circle of radius 0.75 m. What is the minimum velocity that the ball must have to make it around the circle?
- 29. \*A car is going over the top of a hill whose curvature approximates a circle of radius 200 m. At what velocity will the occupants of the car appear to weigh 20% less than their normal weight (or their normal weight times 0.8)?
- 30. \*A car is going through a dip in the road whose curvature approximates a circle of radius 200 m. At what velocity will the occupants of the car appear to weigh 20% more than their normal weight (or their normal weight times 1.2)?
- 31. \*The occupants of a car traveling at a speed of 30 m/s note that on a particular part of a road their apparent weight is 15% higher than their weight when driving on a flat road.
  - a. Is that part of the road a hill or a dip?
  - b. What is the vertical curvature of the road?

- 32. \*A ball is attached to the end of a string. It is swung in a vertical circle of radius 0.33 m. What is the minimum velocity that the ball must have to make it around the circle?
- 33. \*A ball is attached to the end of a string. It is swung in a vertical circle of radius 2.5 m. What is the minimum velocity that the ball must have to make it around the circle?
- 34. \*A car is going over the top of a hill whose curvature approximates a circle of radius 350m. At what velocity will the occupants of the car appear to weigh 10% less than their normal weight?
- 35. \*A car is going through a dip in the road whose curvature approximates a circle of radius 150m. At what velocity will the occupants of the car appear to weigh 15% more than their normal weight?
- 36. \*The occupants of a car traveling at a speed of 40 m/s note that on a particular part of a road their apparent weight is 30% lower than their weight when driving on a flat road.
  - c. Is that part of the road a hill or a dip?
  - d. What is the vertical curvature of the road?

## **Class Work**

- 37. \*\*A car, traveling at a speed of 25 m/s, rounds a flat curve whose radius is 125 m.
  - a. Draw a side view free body diagram for the car. Indicate the direction of acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the frictional force acting on the car.
  - c. Solve those equations for the coefficient of friction between the tires and the road.

- 38. \*\*A car, traveling at a speed of 32 m/s, rounds a flat curve whose radius is 250 m.
  - a. Draw a side view free body diagram for the car. Indicate the direction of acceleration.
  - b. Use that free body diagram to set up the equations needed to determine the frictional force acting on the car.
  - c. Solve those equations for the coefficient of friction between the tires and the road.

# **Answers**

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b)4 Hz b)1.59 Hz b) $F_T + mg = mv^2/r$ c) $2.500 \text{ m/s}^2$ c) $3.83 \text{ N}$ 2)  a)0.01 s b)100 Hz 12) $0.8 \text{ m}$ 24) a) $F_T + mg = mv^2/r$ c) $16.57 \text{ N}$	
c)2,500 m/s <sup>2</sup> c) 3.83 N 2) a)0.01 s b)100 Hz 11) 62.5 m/s <sup>2</sup> 24) a) $F_T$ up, mg down, b) $F_T$ -mg=mv <sup>2</sup> /r c) 16.57 N	a up
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12) 0.8 m c) 16.57 N	
C) 10.57 N	
3) 12) 2.9 m/s	
1 ~/ I 3) 3.0 III/S	
a)0.083 Hz 25) a)F <sub>T</sub> , mg, and a do	wn
b)1032 s 14) 7.35 m b) $F_T$ +mg=mv <sup>2</sup> /r	
(c) 1.3 N	
15) 23 m/s	
a) 5s	a up
b) 0.2Hz b) F <sub>T</sub> -mg=mv <sup>2</sup> /r	
17) 7.7 m/s c) 6.2 N	
5) 18) 705 N	
a) 0.083s 27) 3.83 m/s	
b) 7.2s 19) 30.4 m/s <sup>2</sup>	
20) 0.06 m	
6)	
a) 0.002s 21) 9393 N 29) 19.8 m/s	
b) 0.014s	
22) 102 m 30) 19.8 m/s	
7)	
a) 0.25Hz 31) a) dip	
b) 1.6m/s b) 612 m	
c) 2.56 m/s <sup>2</sup>	
32) 1.80 m/s	
8)	
a) 0.04s 33) 4.95 m/s	
b) 785m/s	
c) 123,245m/s <sup>2</sup> 34) 18.52 m/s	
9) 35) 14.85 m/s	
a)0.1 Hz	
b)1.257 m/s 36) a) hill	
c)0.79 m/s2 b) 544 m	
37) 0.51	
38) 0.42	