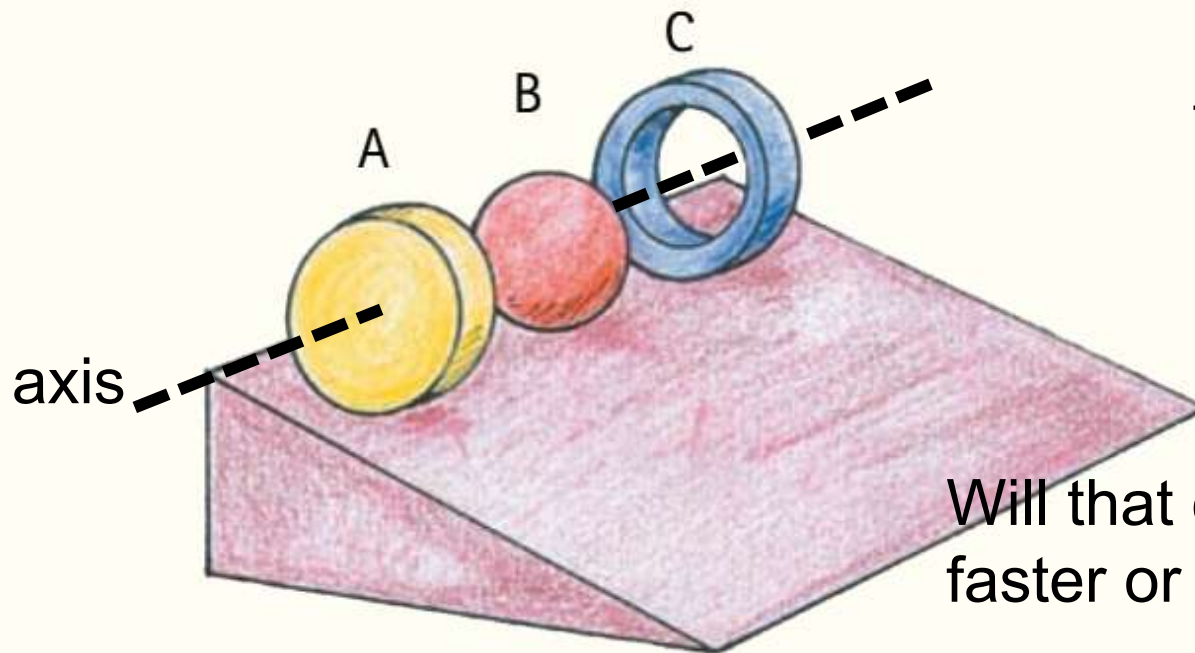


Review:

53. Beginning from a rest position, a solid disk A, a solid ball B, and a hoop C race down an inclined plane. Rank them in reaching the bottom: winner, second place, and third place.



Which has its mass furthest from the axis? C

Does that one have more or less rotational inertia?

Will that one roll faster or slower? more slower

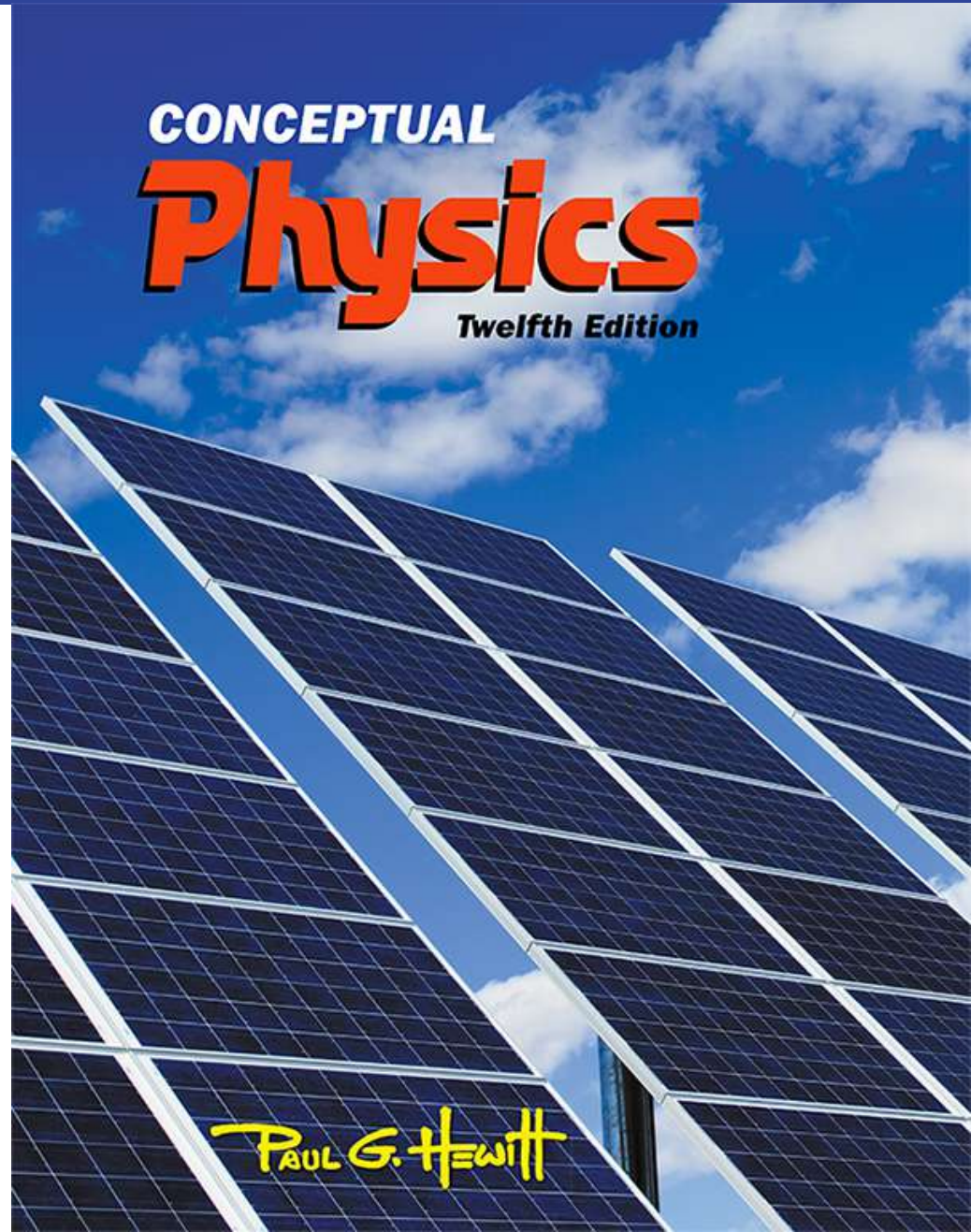
Which will roll the fastest? B

Why? mass closest to axis less rotational inertia

Lecture Outline

Chapter 8: Rotational Motion

Section 8.3 Torque

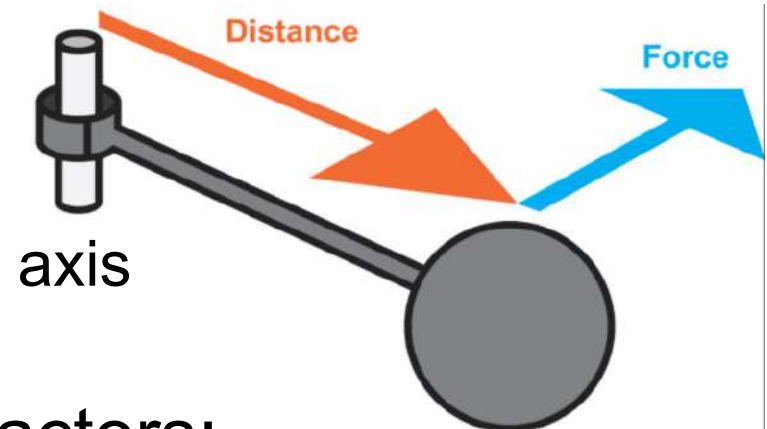


This lecture will help you understand:

- How a torque wrench works
- Why doorknobs are not in the center
- How to pedal a bike better
- How a clock turns
- How to balance on a teeter totter

Torque

- The tendency of a force to cause rotation is called **torque**.
- **Torque = turning force**



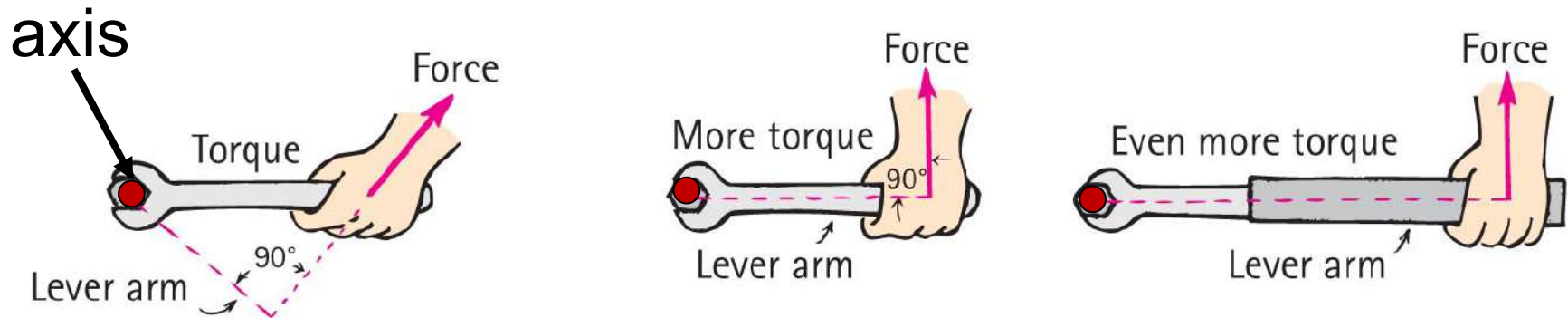
Torque depends upon three factors:

- 1) Magnitude of the force F
- 2) The angle (direction) at which it acts
- 3) The point at which it is applied on the object

The last 2 factors involve the “**lever arm.**”

- The equation for Torque is

$$\text{Torque} = \text{lever arm} \times \text{force}$$

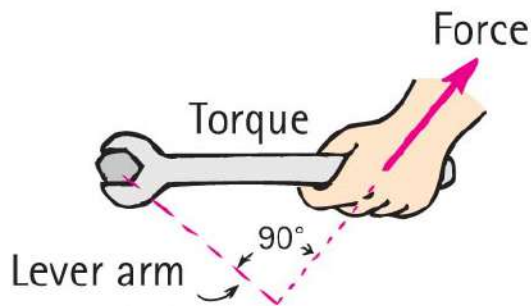


- The lever arm depends upon
 - how far the force is applied from the axis
 - the direction (angle) in which it acts.

The *lever* arm is sometimes called the *moment* arm.

Lever arm: the perpendicular distance from axis of rotation to the “force line”

- 1st picture: Lever arm is *less than* length of handle because of direction of force.
- 2nd picture: Lever arm is equal to length of handle.
- 3rd picture: Lever arm is longer than length of handle.



Most and least torque:

For a given force F ...

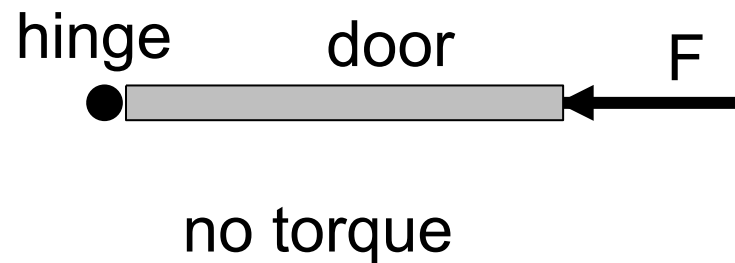
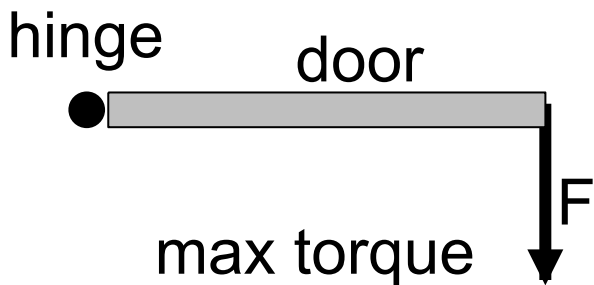
1) **most torque** when:

... F is perpendicular to the lever arm.

2) **least torque (none)** when:

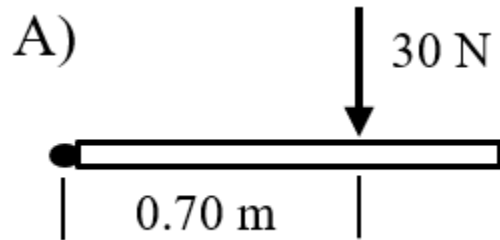
...the lever arm is zero (F points at axis).

Example: Top view of door

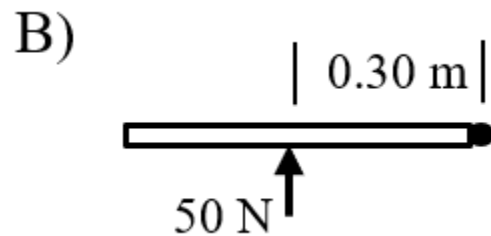


Our calculations will only involve the “most torque” case.

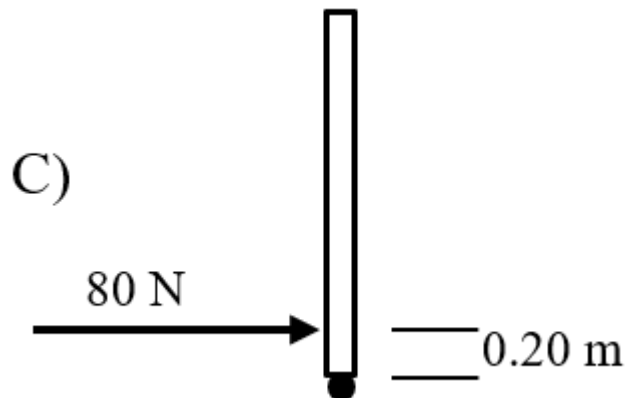
Ex. Calculate torque about the door axis (heavy dot)



$$\begin{aligned}\text{torque} &= \text{lever arm} \times F \\ &= 0.70 \text{ m} \times 30 \text{ N} \\ &= 21 \text{ N}\cdot\text{m}\end{aligned}$$



$$\begin{aligned}\text{torque} &= \text{lever arm} \times F \\ &= 0.30 \text{ m} \times 50 \text{ N} \\ &= 15 \text{ N}\cdot\text{m}\end{aligned}$$



$$\begin{aligned}\text{torque} &= \text{lever arm} \times F \\ &= 0.20 \text{ m} \times 80 \text{ N} \\ &= 16 \text{ N}\cdot\text{m}\end{aligned}$$

Does maximum F mean maximum torque?

Increasing force or lever arm

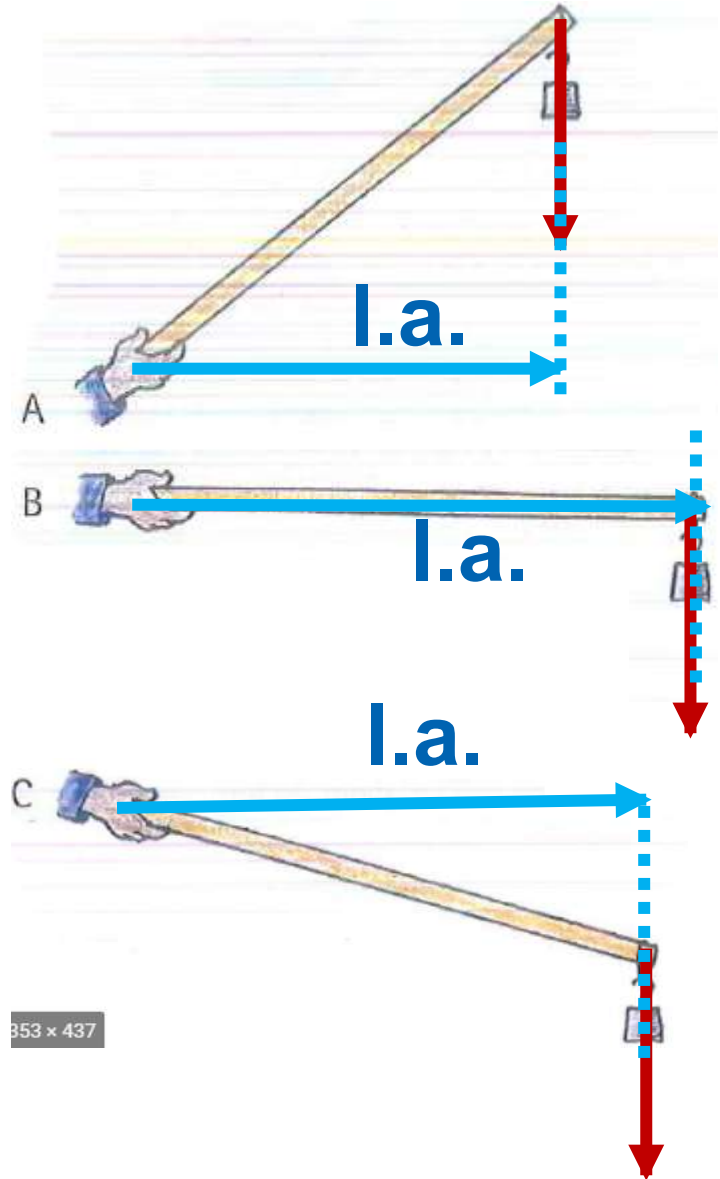
- You hold a meterstick at one end with the same mass at the opposite end. Rank the torque needed to keep the stick steady, from largest to smallest.

same

Torque = lever arm x force

Which has longest lever arm?

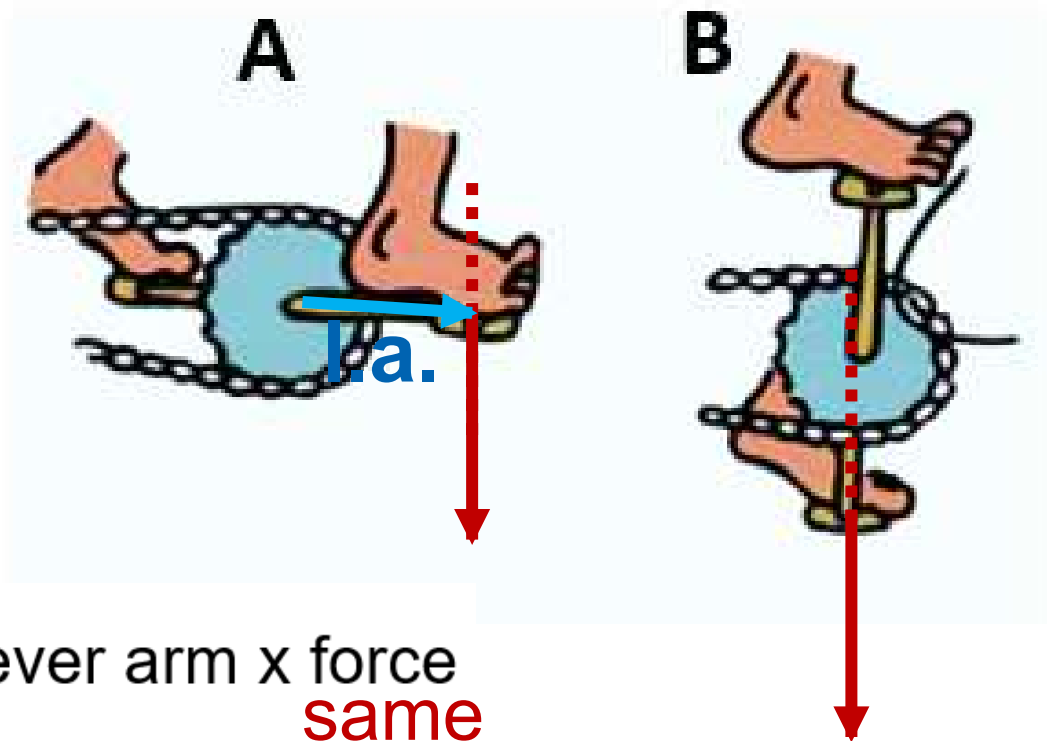
B > C > A



353 x 437

Pedaling a bike:

Why do you get the most torque in A and no torque in B?



B has a
lever arm
= 0
→ no
torque

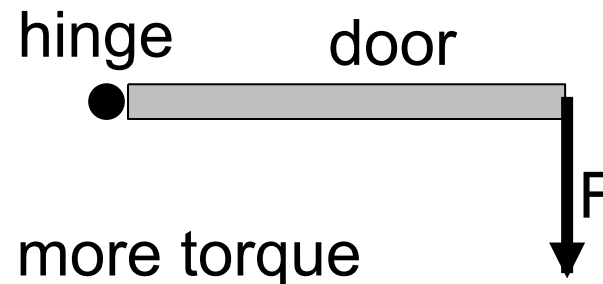
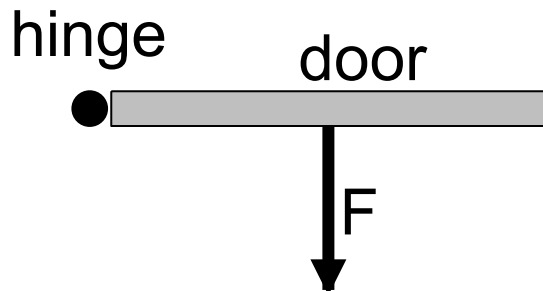
Torque = lever arm x force
same

Which door is easier to turn? Why?

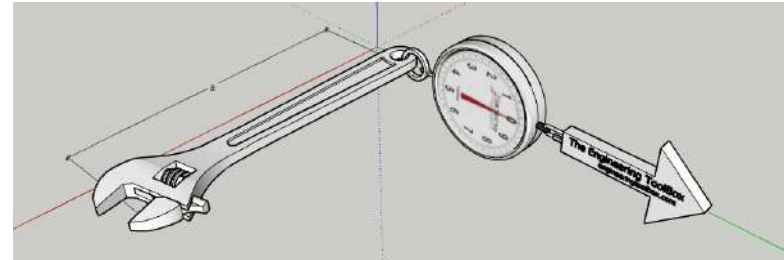


Easier

- Top view:



Torque wrenches allow you to set what the maximum torque will be, so that you don't overtighten:

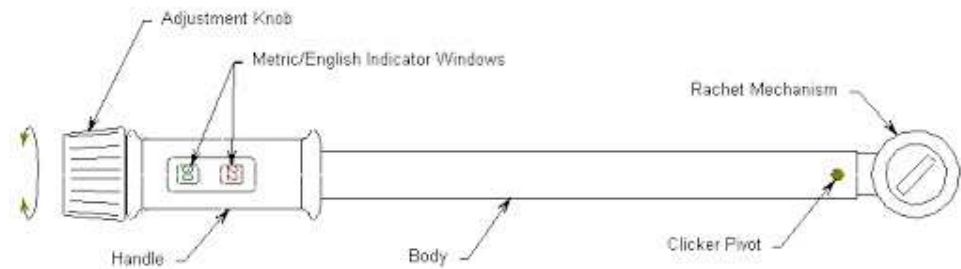
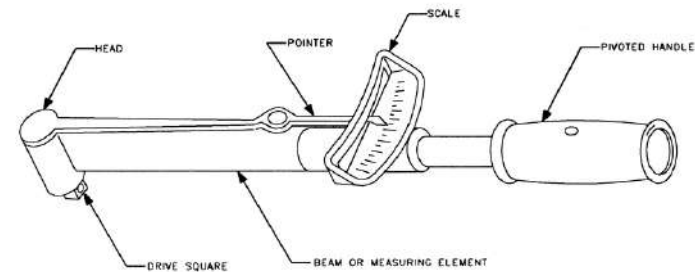


British torque units:

Foot-pounds

Metric units:

Newton-meters

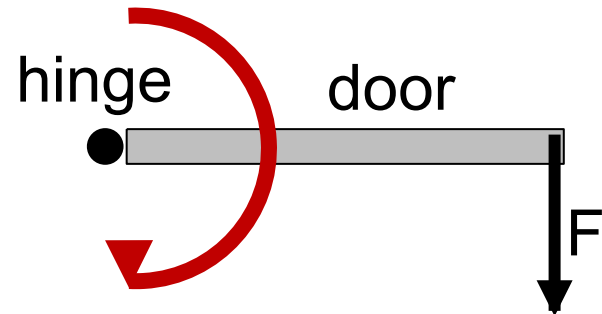
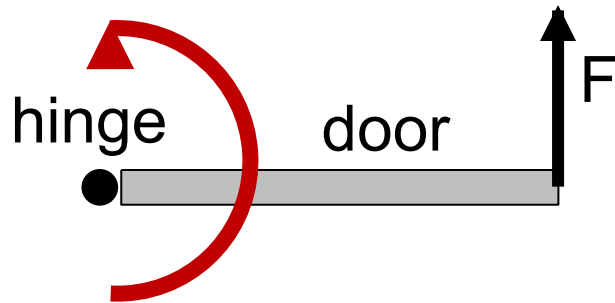


Clockwise (CW) torques vs. Counterclockwise (CCW) torques

CW or CCW?
CCW torque



CW or CCW?
CW torque



Review: Equilibrium

An object is in **equilibrium** if the sum of the forces F that act on it equals 0:

$$\Sigma F = 0$$

The up and down F 's balance.

The right and left F 's balance.

If so, then an object is in **equilibrium**:

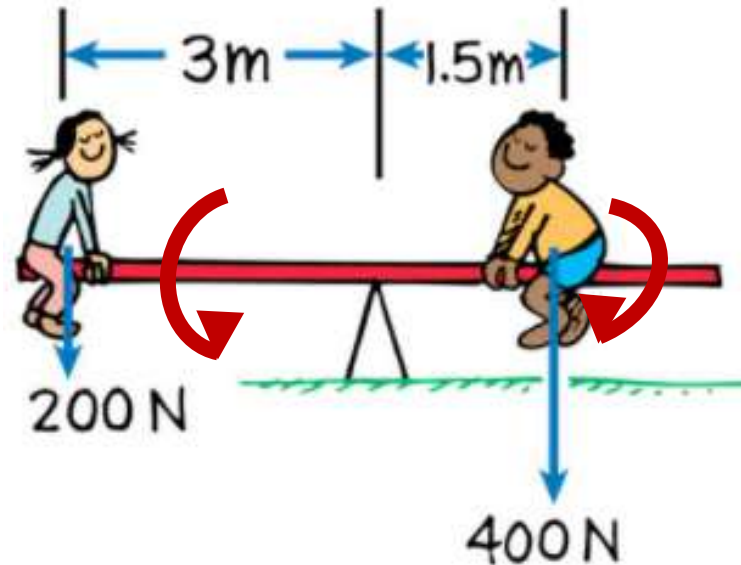
→ it is at rest, or

→ moving with constant velocity.

Rotational equilibrium occurs when **torques** balance:

Counterclockwise torque = clockwise torque

CCW torque = CW torque



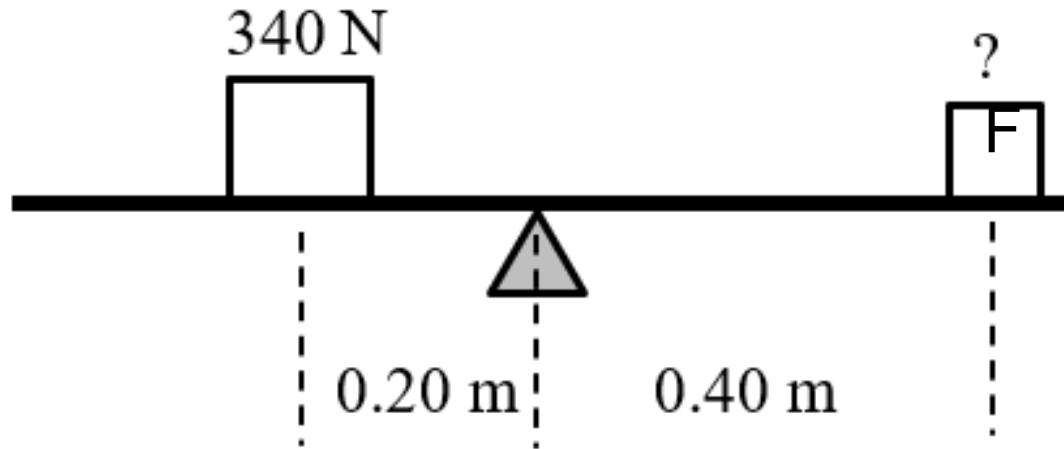
CCW
torque:

$$\begin{aligned}\text{torque} &= \text{lever arm} \times F \\ &= 3 \text{ m} \times 200 \text{ N} \\ &= 600 \text{ N}\cdot\text{m}\end{aligned}$$

CW
torque:

$$\begin{aligned}\text{torque} &= \text{lever arm} \times F \\ &= 1.5 \text{ m} \times 400 \text{ N} \\ &= 600 \text{ N}\cdot\text{m}\end{aligned}$$

Ex. Find the missing weight (F)



CCW torque = CW torque

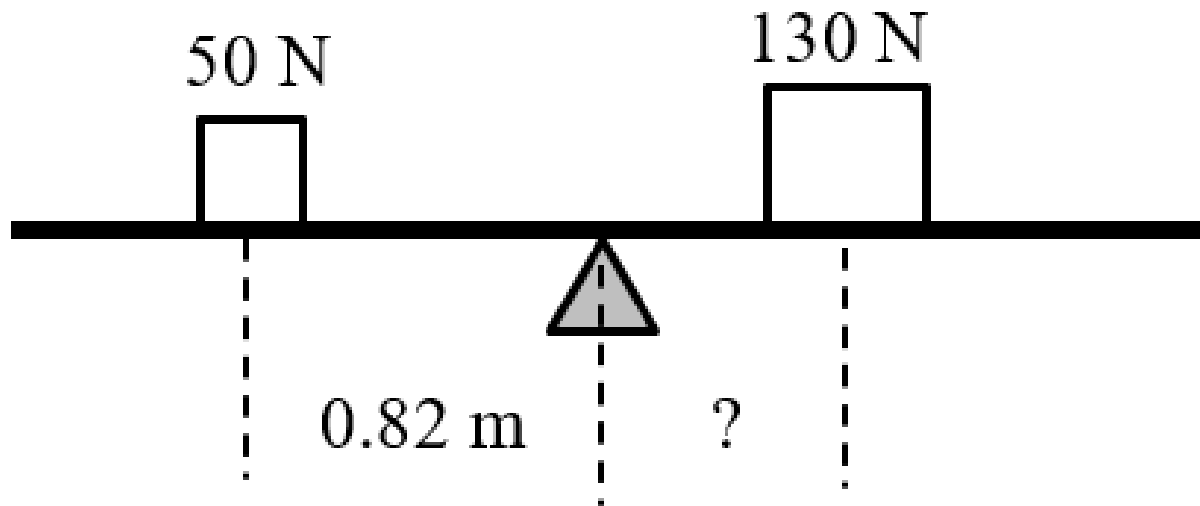
$$0.2 \text{ m} \times 340 \text{ N} = 0.40 \text{ m} \times F$$

$$68 \text{ Nm} = 0.40 \text{ m} \times F$$

$$170 \text{ N} = F$$

How could you have “guessed” the answer?

Ex. Find the missing lever arm (l.a.).



CCW torque = CW torque

$$0.82 \text{ m} \times 50 \text{ N} = \text{l.a.} \times 130 \text{ N}$$

$$41 \text{ Nm} = \text{l.a.} \times 130 \text{ N}$$

$$0.32 \text{ m} = \text{l.a.}$$

Homework: due tonight by 7 pm

- page 153: # 12-14
- page 155: # 38, 39 and 45.
 - Show work (equation used, substitution with units, and answer with units).
- page 156: #54