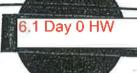
NAME: KEY

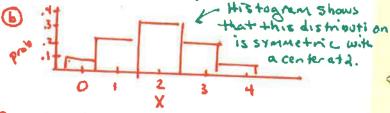
(A)



# Exercises

- Toss 4 times Suppose you toss a fair coin 4 times. Let X = the number of heads you get.
  - (a) Find the probability distribution of X.
  - (b) Make a histogram of the probability distribution. Describe what you see.

(c) Find  $P(X \le 3)$  and interpret the result.



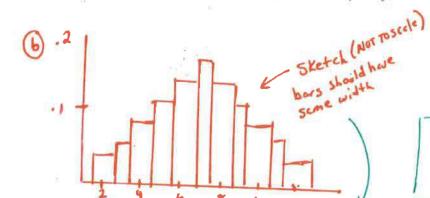
## @ P(X < 3) = 1 -. 0625 = .9375

There is a 93.75% chance that you will get 3 or fewer heads on 4 tosses of a fair coin

- Pair-a-dice Suppose you roll a pair of fair, six-sided dice. Let T = the sum of the spots showing on the up-faces.
  - (a) Find the probability distribution of T.
  - (b) Make a histogram of the probability distribution. Describe what you see.
  - (c) Find  $P(T \ge 5)$  and interpret the result.

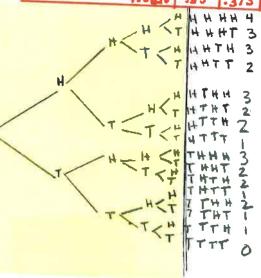
#### 1 T= The SUM of the spots on 2 dice

Value	2	3	4	5	6	7	8	9	01	11	12
Arlas Arlas	130	元	3/2	4	まれ	25	5/30	9 36	3-	랖	1 70



### X= # of heeds (4times)

Value (x)	0	-1	2	3	4		
Proportify (pi)	% .0L25	*//-	-375	4116	914		
	11 4	HHH	H H 4	-			



1 1 = 2 2 : 3 3 = 4 9 = 5 5 = 6 6 : 7 2 1 : 3 3 : 5 9 : 6 5 : 7 6 : 7	31= 4 2 · S 3 · 7 6 · 9 4 · 5 5 · 7 4 · 8 5 · 9	S1=6   2:7   3:4   4:9   5=10   6=11   61:7   7:8   3:4   9:10   5:11   V(=12
		0 4 - 12

# @P(T>5)=1-4/36=5/6 or =.83

HOOST 83% OF THE TIME, WHEN YOU ROLL A PAIR OF Sice, YOU WILL HAVE A SUM OF 5 GIR MORE

Source: TPS (CHG)

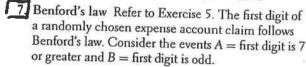
The histogram shows a symmetric distribution about a center of 7

PGI OF4

Benford's law Faked numbers in tax returns, invoices, or expense account claims often display patterns that aren't present in legitimate records. Some patterns, like too many round numbers, are obvious and easily avoided by a clever crook. Others are more subtle. It is a striking fact that the first digits of numbers in legitimate records often follow a model known as Benford's law. Call the first digit of a randomly chosen record X for short. Benford's law gives this probability model for X (note that a first digit can't be 0):

First digit X: 1 2 3 4 5 6 7 8 9 Probability: 0.301 0.176 0.125 0.097 0.079 0.067 0.058 0.051 0.046

- (a) Show that this is a legitimate probability distribution.
- (b) Make a histogram of the probability distribution. Describe what you see.
- (c) Describe the event  $X \ge 6$  in words. What is  $P(X \ge 6)$ ?
- (d) Express the event "first digit is at most 5" in terms of X. What is the probability of this event?
- © The 18t digit is a rendamly chosen record is a 6 or higher P(X > 6) = .067 + .058 + .051 + .046 P(X > 6) = .222



- (a) What outcomes make up the event A? What is P(A)?
- (b) What outcomes make up the event B? What is P(B)?
- (c) What outcomes make up the event "A or B"? What is P(A or B)? Why is this probability not equal to P(A) + P(B)?

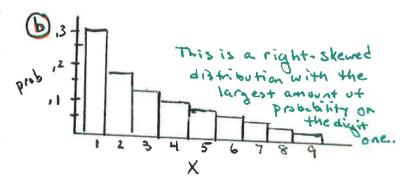
P(AOB) + P(A)+P(B) because

event A and B are NOT mutually exclusive.

This is a legit i mete probability distribution because

O all the probabilities are between

@ the probabilities sum to 1.



- 9 Keno Keno is a favorite game in casinos, and similar games are popular with the states that operate lotteries. Balls numbered 1 to 80 are tumbled in a machine as the bets are placed, then 20 of the balls are chosen at random. Players select numbers by marking a card. The simplest of the many wagers available is "Mark 1 Number." Your payoff is \$3 on a \$1 bet if the number you select is one of those chosen. Because 20 of 80 numbers are chosen, your probability of winning is 20/80, or 0.25. Let X = the amount you gain on a single play of the game.
  - (a) Make a table that shows the probability distribution of X.
  - (b) Compute the expected value of X. Explain what this result means for the player.

X = amount you gain on a single play of Keno

VALUE	<b>\$0</b>	\$3
Probability	.75	.25

[II] To 9	ind exped	ed volv	7	15 To	find std	dev.
Work	3 4	Pi .1 .2 .3 .3 .1	Xi pi 0 .2 .6 .9 .4	xi-lex -2.1 -1.1 -0.1 0.9	(xi-lex) <sup>2</sup> 4.41 1.21 1.01 1.81 3.61	(xi-lex) pi .441 .242 .003 .243 .361 Z=1.290
On a und	verage. leng reduce nonwi	ites mak 250 -Woo	(e	ON hi ei re	= 1,135  average, Imber of rors in a ndonly se say will om the me y about 1	the nonword lected ldiffer en (2.1)

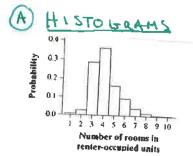
19. Housing in San Jose How do rented housing units differ from units occupied by their owners? Here are the distributions of the number of rooms for owneroccupied units and renter-occupied units in San Jose, California:7

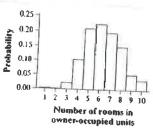
#### Number of Rooms

10 Owned 0.003 0.002 0.023 0.104 0.210 0.224 0.197 0.149 0.053 0.035 Rented 0.008 0.027 0.287 0.363 0.164 0.093 0.039 0.013 0.003 0.003

Let X = the number of rooms in a randomly selected owner-occupied unit and Y = the number of rooms in a randomly chosen renter-occupied unit.

- (a) Make histograms suitable for comparing the probability distributions of X and Y. Describe any differences that you observe.
- (b) Find the mean number of rooms for both types of housing unit. Explain why this difference makes
- (c) Find the standard deviations of both X and Y. Explain why this difference makes sense.





DESCRIBE: THE DISTRIBUTION OF THE NUMBER OF ROOMS IS ROUGHLY SYMMETRIC FOR OWNERS AND SKEWED TO THE RICHT FOR RENTERS. OVERALL, RENTER - OCCUPIED UNITS TEND TO FEWER ROOMS THAN OWNER OCCUPIED UNITS

Mo= 6. 284 MR = 4.187

USE CALC

L1 = 4 RODAS 1-10

La = P(owned)

L3 = L1 × L2

STAT CALC (1) L3 2x=6.284

14= P(rent)

L5 = L1 \* L4

STAT CALC () L5 ZX=4,187

The men for renters is about 4.2 rooms, Compared to the mean for owners is about 6.3 woms; which metches our observations from the histograms

BELOW 60 = 1.64 rooms

6R = 1.31 ROOMS

on how to colculate We would expect

the owner distribution to have a slightly wider spread than the renter distribution. Even though the distribution of renter-occupied units is skewed to the right, it is more concentrated (contains less variability) about the "peak" than the symmetric distribution for owner-occupied units.

VAR (x) = 6 2 = (x, - 1/2) = p1 + (x2-4x)2.p2 ===

CALCULATE

6, = 1.639 rooms

6R = 1.3077 hours

41212

LI = # ROOMS 1-10 (x2's)

LZ = P(OWNED

L3 = L1 \* L2

14 = P(rent)

L5 = L1 + L4

Create 16

16= (11-6.284) = L2

STAT CALC (1) LG

2x = 2.689 = 62

FIND 60

2.689 = (1.6398

Ma = 4.187

Crecke LL L6=(L1-4.187)2, L4

STAT COLC (1) LL

Tx=1.710031=62

1.7/003/ = 1.3077

ITBS scores The Normal distribution with mean ... μ = 6.8 and standard deviation σ = 1.6 is a good description of the Iowa Test of Basic Skills (ITBS) vocabulary scores of seventh-grade students in Gary, Indiana. Call the score of a randomly chosen student X for short. Find P(X ≥ 9) and interpret the result. Follow the four-step process.

STATE: what is the probability

that a randomly chosen student

scores a 9 or better on the ITBS?

(2) PLAN: The Score X of the randomly chosen students has the N (6.8, 1.6) distribution. We want to find the P (x7.9), we will standardize the scores and find the area under the normal conve.

3 Do: The standardized score for the test:

 $Z = \frac{9 - 0.8}{1.6} = 1.38$  P(2 > 1.38) = .0838

= .0838 QUD DIST -- Normaladf (1.38, 9999)=

4 Conclude: there is about an 8% chance that the Chosen student's score is 9 or higher.

Running a mile A study of 12,000 able-bodied male students at the University of Illinois found that their times for the mile run were approximately Normal with mean 7.11 minutes and standard deviation 0.74 minute.8 Choose a student at random from this group and call his time for the mile Y. Find P(Y < 6) and interpret the result. Follow the four-step process. (See last page for steps)

3) DO: SINCE N (7,11,174) AND P(YKG) NORMAL CDF (-EE99, 6, 7.11,74) = 0668 FOUR STEP PROCESS

\*\* That a randomly chosen student runs the mile in under 6 MINUTES.

@ PLAN: • LET Y = the time of a randomly chosen student

· Normal distribution N (7.11, .74)

· We went to find P(YX6)

" Draw the density curve

(A) Concuse.

There is about a 7% chance that a randomly selected student will run the mile in under 6 minutes.

Did you vote? A sample survey contacted an SRS of 663 registered voters in Oregon shortly after an election and asked respondents whether they had voted. Voter records show that 56% of registered voters had actually voted. We will see later that in repeated random samples of size 663, the proportion in the sample who voted (call this proportion V) will vary according to the Normal distribution with mean  $\mu = 0.56$  and standard deviation  $\sigma = 0.019$ .

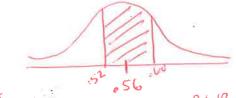
(a) If the respondents answer truthfully, what is  $P(0.52 \le V \le 0.60)$ ? This is the probability that the sample proportion V estimates the population proportion 0.56 within  $\pm 0.04$ .

(b) In fact, 72% of the respondents said they had voted (V = 0.72). If respondents answer truthfully, what is  $P(V \ge 0.72)$ ? This probability is so small that it is good evidence that some people who did not vote claimed that they did vote.

(b)

V= proportion in the sample that workd N(.56,019)

a) P(,52 & V &, 60) = .9647 Normal cdf(,52,060,056,019)



There is about a 96% chance that the population proportion of .56 is within ±,04.

normal alf (.72, EE99, .S6, .019) = 1, BE-17 (essentially 0)

This confirms the probability that 72% of the respondents answered treathfully is zerolos.