HO FALSE HO TRUE TESTING A CLAIM REJECT CORRECT TYPE FAIL TO REJECT CORRECT TYPE M= mean response time for SECHION 10.18 19 A] Exercises all accidents involving life THREATENING INJORIES IN THE City Ho: M=6.7 min HA: MX6.7 Want to do better Ы refer to the following setting. Slow Exercises 19 MIN esponse times by paramedics, firefighters, and policemen can have serious consequences for accident victims. In 6.7 TYPE I ERROR: false positive d the case of life-threatening injuries, victims generally need medical attention within 8 minutes of the accident. Several 193 The city Council concludes the cities have begun to monitor emergency response times. response time his improved In one such city, the mean response time to all accidents involving life-threatening injuries last year was $\mu = 6.7$ when it has Not. minutes. Emergency personnel arrived within 8 minutes TYPEI ERROR: false negative B after 78% of all calls involving life-threatening injuries last year. The city manager shares this information and encour-The city council Concludes ages these first responders to "do better." At the end of the that the response time has year, the city manager selects an SRS of 400 calls involving life-threatening injuries and examines the response times. not improved when it 19. Awful accidents really has. ERRUR Would be wurse. 19C (a) State hypotheses for a significance test to YPEI The city may stop trying to determine whether the average response time has jacl when in fact they have not. decreased. Be sure to define the parameter of interest. (b) Describe a Type I error and a Type II error in this setting, and explain the consequences of each. (c) Which is more serious in this setting: a Type I MORE PEOPLE QUILD DIE. error or a Type II error? Justify your answer. M= THE MEAN INCOME RESIDENTS OF (a) NEAR THE RESTAURANT. 21) Opening a restaurant You are thinking about open-Ho: M= \$85,000 ing a restaurant and are searching for a good location. From research you have done, you know that HA: 117\$ 85,000 the mean income of those living near the restaurant \$85,000 must be over \$85,000 to support the type of upscale RESTAURANT IN restaurant you wish to open. You decide to take TYPEIEREUR : OPEN THE ALOCATION WHERE THE RESIDENTS WILL NOT a simple random sample of 50 people living near one potential location. Based on the mean income BE ABLE TO SUPPORT IT. of this sample, you will decide whether to open a TYPE IL ERROR: DO NOT OPEN A RESTAURANT restaurant there.8 IN ALOCATION WHERE THE RESIDENTS (a) State appropriate null and alternative hypotheses. COOLD IN FACT SUPPORT IT FINANCIALLY. Be sure to define your parameter. (b) Describe a Type I and a Type II error, and A TYPE I ERROR WOULD BE WORSE IN explain the consequences of each. TO OPEN THE RESTAURANT. (c) If you had to choose one of the "standard" SO IT WUJLD BE BETTER TO CHOSE 2=,01 SELECTING A LUCATION . significance levels for your significance test, would you choose $\alpha = 0.01, 0.05$, or 0.10? Justify your TO MINIMIZE THE RISK OF A TYPE I EREUR choice. POWER = 1-B x =.05 23 Error probabilities You read that a statistical test at sig-.78=1-B POWER = . 78 nificance level $\alpha = 0.05$ has power 0.78. What are the P(TYPEI ERROR) = 2 =,05 probabilities of Type I and Type II errors for this test? P (TYPE II ERROR) = B = .22 (1-.78)

100

M = the mean nicotine content of their cigarettes 3. A certain cigarette brand advertises that the mean nicotine content of their cigarettes is 1.5 mg, but you are suspicious and plan to investigate the advertised claim by testing the hypotheses $H_0: \mu = 1.5$ versus $H_a: \mu > 1.5$ at the $\alpha = 0.05$ significance level. You will do so by measuring the nicotine content of 30 randomly selected cigarettes of this brand.

A PERCON	
Ho	: H= 1.5
HA	· 11 71,5

(a) Describe what a Type I error would be in this context. false positive (a)

Conclude that the mean nicotine content per cigorette is greater than 1.5 mg when it is Equal TO (OR LESS THAN) 1.5 mg. (b) Describe what a Type II error would be in this context. filse negative (B) Not Conclude that the mean nico time level is greater than 1.5 mg per Cigcrette when it is.

- (c) From the perspective of public health, which error—Type I or Type II—is more serious? Explain.
 - A TYPE I ERROR WOULD MEAN THAT YOU FAIL TO DISCOUR THAT THE CIGARETTES HAVE A HIGHER NICOTINE CONTENT THAT THE COMPANY CLAIMS, WHICH MEANS PEOPLE WILL BE EXPUSED TO MURE NICOTINE THAT THEY EXPECT AND THIS WOULD BE A PUBLIC HEALTH ISSUE! A TYPE I ERLOR MICHT BRINGUNWARRANTED NEGATIVE PUBLICITY TO THE TOBALLO COMPANY BUT NOT A HEALTH ISSUE,

(d) Explain why it might be a good idea to increase the significance level to 0.10 for this test.

YOU WANT TO MINIMIZE THE CHANCE OF MAKING A TYPE II FROZ (NOT FINDING THAT THE NICOTINE LEVEL IS HIGHER THAN 1.5 WHEN IT IS), SO IT WOULD BE A GOUD IDEA TO USE A HIGHER SIGNIFICANCE LEVEL (2) WHICH WILLINCREASE THE POWER OF THE TEST.

(e) You have determined that at the $\alpha = 0.05$ significance level, the power of the test against the alternative $\mu = 1.75$ is 0.88. Explain what the power of the test means in the context of the problem.

Power = . 88 measures the probability of rejecting the null hypothesis and concluding that the true mean hicotine level is above 15 when IT IS IN FACT 1.75 mg.

(f) What impact will reducing the significance level to 0.01 have on the power of the test?

1,75 Reducing & from, 05 to, 01 (the significance level) Shift d will increase the probability of a Type II error, so it reduces the power. You can see this relationship by shifting the red line to the right

15=,22

UD

MA

1.5

12. "Red tide" is a bloom of poison-producing algae-a few different species of a class of plankton called dinoflagellates. When weather and water condition cause these blooms, shellfish such as clams living in the area develop dangerous levels of a paralysis-inducing toxin. In Massachusetts, the Division of Marine Fisheries (DMF) monitors levels of the toxin in shellfish by regular sampling of shellfish along the coastline. If the mean level of toxin in clams exceeds 800µg (micrograms) of toxin per kg of clam meat in any area at a 5% level of significance, clam harvesting is banned there until the bloom is over and levels of toxin in clams subside. During a bloom, the distribution of toxin levels in clams on a single mudflat is distinctly non-Normal. M= mean Concentration of Red Tide toxins in clams (Mg/kg) (a) Define the parameter of interest and state appropriate hypotheses for the DMF to test. Ho: Le = 800 mg/kg HA: Le > 800 mg/kg (b) Because of budget constraints and the large number of coastal areas that must be tested, the DMF would like to sample no more than 10 clams from any single area. Explain why this sample size may lead to problems in carrying out the significance test from (a). The sample size of loclims is too small for a Population that is Known (given in the problem) to be "distinctly non-Normal."

(c) Describe a Type I and a Type II error in this situation and the consequences of each.

TYPEIERROE: Concluding that the mean level of toxin is above 800 kg/kg when it is normal. <u>Consequence</u>: The DMF would close the area to alam havesting which would have a negative economic impact on anyone who depends on the claim business, even though the class are safe to eat. TYPE I ERROR: NOT CONCLUDING THAT THE MEAN LEVEL OF TOXINS IS ABOVE SAFE LEVELS WHEN IT IS. CONSEQUENCE! THIS COULD CAUSE ANYONE WHO EATS CLAMS FROM THIS AREA TO BECOME SICK OR EVEN DIE.

(d) The DMF is considering changing the significance level of the test to 10%. Discuss the impact this might have on error probabilities and the power of the test, and describe the practical consequences of this change.

SIGNIFICANCE LEVEL TO 1000 WOULD INCREASE RAISING THE THE PROBABILITY OF A TYPE I ERROR , BUT DECREASE THE PROBABILITY OF A TYPE I ERROR AND INCREASE THE POWER OF THE TEST. THIS WOULD DECREASE THE LIKELIHOOD OF PEOPLE EATING TOXIC CLAMS, SO IT MICHT BE A GOUD IDEA, BETTER SAFE THAN SURRY.