| AP Statistics – 9.2a | Name: 2020 KEY |
|--|----------------|
| Goal: 1-Sided Significance Tests for a Population Proportion (p) | Date: |

I. Right-Tail Test of Significance for Proportions

Example #1 "Can you be confident of victory?" Jack is a candidate for mayor running against only one other candidate, so he must gain at least 50% of the votes to be elected. Heading into the mayoral election, Jack is feeling fairly confident that he will be elected by obtaining more than 50% of the vote. Suppose that a random sample of 100 voters shows that 56 will vote for Jack. Based on a poll of voters just before the election, can Jack be confident of victory?

Step I: Set up your Test of Hypothesis (TOH).

- Define parameter: P = TRUE PROPORTION WHO VOTE FUR JACK
- Define hypothesis:
- Define your Level of Significance: 2 = 0.5 (Jack wins)

Step II: Check the conditions for carrying out a significance test to determine if Jack should feel confident of victory in the mayoral election.

Step III: Define your choice of significance test: 1 SAMPLE ZTEST FOR P

Step IV: Define Sampling Distribution. Sketch of the sampling distribution of the sample statistic under the null hypothesis, indicating the mean.

- n= 100
- Sketch the graph:

Step V: Calculate the test statistic:

$$Z = \frac{\widehat{P} - P_0}{\sqrt{\frac{P_0(1 - P_0)}{n}}} = \frac{.56 - .50}{\sqrt{(.5)(.5)}} = 1.20$$

CALC: [STAT] [TESTS] [5: I PROP Z TEST]
$$\rho_0 = .5 \times .56 \ n = 100 \ P = 0.1151$$
 $Z = 1.2 \ \hat{\rho} = .56 \ n = 100 \ P = 0.1151$
 $p_0 = .56 \ n = 100 \ P = 0.1151$

Step VI: Calculate the p-value (write as a probability statement):

Step VII: Interpret the P-value. Bocision Rejector Rail to Reject the mail they happens is.

ASSUMING THE PROPORTION OF VOTERS WHO VOTE YES IS. 50, THERE IS A O.1151 Probability OF GETTING A SAMPLE PROPORTION AS FAR AS 0.56 OR FURTHER PURELY BY CHANCE.

Step VIII: Interpret your significance test decision in context. (4 PARTS MUST BE INCLUDED!)

- → SINCE THE PVALUE (O, 1151) IS GREATER THAN HO WE FAIL TO REJECT HO.
- -> WE DO NOT HAVE CONVINCING EVIDENCE JACK WILL WIN THE MAYOR ELECTION.

II. Left-Tail Test of Significance for Proportions

Example #2 Eleven percent of the products produced by an industrial process over the past several months have failed to conform to specifications. The company modifies the process in an attempt to reduce the rate of nonconformities. In a random sample of 300 items from a trial run, the modified process producess 16 nonconforming item. Do these results provide convincing evidence that the modification is effective? Support your conclusion with a test of significance.

- Use the "Test of Significance Template" to work through these steps:
 - 1. Parameter of Interest
 - 2. Level of Significance
 - 3. Choice of Test
 - 4. Null Hypothesis (symbols and words)
 - 5. Alternative Hypothesis (symbols and words)
 - 6. Conditions of Test
 - 7. Sampling Distribution (Sketch of the sampling distribution of the sample statistic under the null hypothesis, indicating the mean)
 - 8. Test Statistic (clearly show calculation)
 - 9. P-value (Use correct probability notation.)
 - 10. Meaning of the P-value (Reject or Fail to reject null hypothesis)
 - 11. Conclusions (in context)

Test of Significance Template

| TRUE PROPORTION OF NON CONFORMING PRODUCTS 1 SAMPLE Z TEST FOR P (Proportions) 2 = 0.05 USE WHEN NOT GIVEN & Glish: Ho: P=.11 Company Claims 1170 PRODUCTS FAIL TO CONFORM TO STANDARDS MIDDLES MIDDLES MEDICED THE PROPORTIONS REDUCED THE PROPORTIONS Name and The Modern Sample (Stated) Name of the Sample (Stated) Ormal: Po=.11 (.10(300) = 3,000 ITEMS. Ormal: Po=.11 (.10(300) = 337,107 (.89)(300) = 2677,10 Each of the sampling distribution of the sample statistic under the null hypothesis, indicating |
|--|
| glish: Ho: P=.11 	— Company Claims 1170 PRODUCTS FAIL TO CONFORM TO STANDARDS mbols: glish: HA: P < .11 	— HAVE THE MODIFICATIONS REDUCED THE PROPORTIONS mbols: andom: Rendom Sample (stated) independent: We must assume each trial run must have more than 10(300) = 3,000 ITEMS. ormal: Po = .11 	— (.10)(300) = 337,107 (.89)(300) = 2677,10 |
| mbols: glish: HA: P < .11 HAUE THE MODIFICATIONS REDUCED THE PROPORTIONS mbols: andom: Rendom Sample (stated) "Ndependent: We must assume each trial run must have more than 10(300) = 3,000 ITEMS. ormal: Po = .11 (.11)(300) = 337,107 (.89)(300) = 2677,10 |
| mbols: andom: Rendom sample (stated) independent: We must assume each trial run must have more than 10(300) = 3,000 ITEMS. ormal: Po = 11 < (.11)(300) = 337,107 (.89)(300) = 2677,10 |
| independent: We must assume each trial run must have more than $10(300) = 3,000$ ITEMS. ormal: $P_0 = .11 < (.11)(300) = 337,107$ $(.89)(300) = 2677,10$ |
| etch of the sampling distribution of the sample statistic under the null hypothesis, indicating |
| mean: $\frac{16}{300} = 0.053$ $\frac{16}{300} = 0.053$ |
| Plug-ins & Value: $Z = \frac{\hat{P} - P_0}{\sqrt{\frac{P_0(1 - P_0)}{Q}}} = -3.16$ |
| e correct probability notation. Praire = $P(Z = -3.16) = 0.00079$ |
| SSUMING THE TRUE PROPORTION OF NONCONFORMING ITEMS 11%, THERE IS ONLY A 0.00079 Probability of getting sample proportion AS FAR FROM 0.056 OR FURTHER |
| Reject null hypothesis Fail to reject null hypothesis glish: since the pucive (0.00079) is less than d=.05, Je reject tho. |
| R F: |



"FRAPPY" {Free Response AP Problem...Yay!}

The following problem is taken from an actual Advanced Placement Statistics Examination. Your task is to generate a complete, concise statistical response in 15 minutes. You will be graded based on the AP rubric and will earn a score of 0-4. After grading, keep this problem in your binder for your AP Exam preparation.

Some boxes of a certain brand of breakfast cereal include a voucher for a free video rental inside the box. The company that makes the cereal claims that a voucher can be found in 20 percent of the boxes. However, based on their experiences eating this cereal at home, a group of students believes that the proportion of boxes with vouchers is less than 0.2. This group of students purchased 65 boxes of the cereal to investigate the company's claim. The students found a total of 11 vouchers for free video rentals in the 65 boxes.

Suppose it is reasonable to assume that the 65 boxes purchased by the students are a random sample of all boxes of this cereal. Based on this sample, is there support for the students' belief that the proportion of boxes with vouchers is less than 0.2? Provide statistical evidence to support your answer.

4 PARTS TO ANSWER

Scoring:

@ p= proportion of boxes at this brand of break fest Cereal that include a voucher for a free video

> Ho: P=.2 HA: P <.2

(a) E I

(b) Identify current Test (by Nome or by furnula)

* one sample Z-test for p or Z= p-por

<u></u> Б І

*Conditions (as stated in pubric)

(1) npo = 65 (.2) = 13 > 10 and n(1-po) = 65(.8) = 52 > 10

€ E I

1) It is reasonable to assume that the company

Produces more than 65×10 = 650 boxes of this cereal

3) It is recorded to assume that the 65 boxes
are random samples of all boxes of this cereal

Е і

Total: /4

$$P = \frac{1}{65} = .169$$

$$Z = \frac{.169 - .2}{\sqrt{\frac{.2(1-.2)}{65}}} = -.62$$

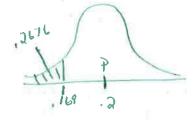
Ocheckwicale STAP (TESTS)

5:1 prop 2 test

Po=. 2 1 Po x=11 n=15

P=, 2676

@ Sketch graph



1 State a correct conclusion, with results of test, in context.

Since the p-value =, 2676 is larger

than any reasonable significance level

(e.g. d=.05), we cannot reject the

Companies claim. That is, we do not

have statistically significant evidence
to support the student's be lied that

the propertion of cereal boxes is

less than 20 percent.



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