

Guided Notes – 8.3 Estimating a Population Mean CI

1. Inference about population proportions (____) based on _____ variables.
 - Proportions are _____.
2. Inference about population means (____) based on _____ variables.
 - Means are _____.
3. In most real world problems, we do **NOT** know the population _____ (μ) or _____ (σ), therefore we **cannot use** the **Z-statistic** for **inference for means**.
 - We will learn a new test statistic in this chapter that will always be used for inference tests with means called the **t-Statistic**
 - You will **NEVER** be asked to do a “1 Sample Z-interval for a population mean”. We never know the population standard deviation (σ), so this is a useless test.

Estimating Sample Sizes for Means

4. What is the formula to **calculate the sample size for means**?
 - a) What statistic will be used to calculate **the sample size for means**? _____
 - b) What critical value will be used to calculate **the sample size for means**? _____
 - c) What conditions are required?
 1. R_____
 2. I_____
 3. N_____
 4. Plus **you must know** the population _____ (σ)

5. Describe the three steps for choosing a sample size for a desired margin of error when estimating μ .

6. Complete the Check Your Understanding “Monkeys” -- page 501-502.

1) Define population parameter	$\mu =$
2) Get information to estimate the sample size	CL= _____ $z^* =$ _____ $\sigma =$ _____ ME= _____
3) Use formula used to determine the sample size n for a population mean:	$z^* \frac{\sigma}{\sqrt{n}} \leq ME$. Solve for n .
4) Substitute numbers and clearly show all steps to calculate the sample size n	
5) Always round _____ whole number to ensure ME is met.	We need to sample _____

7. It is the size of the _____ that determines the margin of error. The size of the _____ does not influence the sample size we need. This is true as long as the population _____.

8.3 Estimating a Population Mean when “σ KNOWN”

8. What is the standardized value of the z-statistic?

- a) See Figure 8.11 to understand this new z-statistic

Sketch the sampling distribution of \bar{x} when the normal condition is met and σ is known.	Compare the distributions	Sketch the standard normal distribution .
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- b) When we don't know " σ ," we estimate it using the _____; creating a **new statistic** called the "**t-statistic**."

- ## 9. SKIP “Bingo” Activity

10. What is the fomula for the “t-statistic”?

- a) How do you calculate the degrees of freedom for a t distribution?

See Figure 8.13 to understand the t-statistic

<p>b) Sketch normal distribution; t-distrib. with $df=9$; and t-distrib. with $df=2$.</p>	<p>c) Describe the similarities between a standard normal distribution and a t distribution.</p> <p>d) Describe the differences between a standard normal distribution and a t distribution.</p> <p>e) What happens to the t distribution as the degrees of freedom increase?</p>
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11. How do you find the critical value t^* using TI84? You only need to know how to use Table B if you have a TI83.

12. Check Your Understanding -- page 507 (use TI84, sketch the graph, answers in back of book)

a)	b)	c)
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13) What is the formula for the <u>standard deviation of the sampling distribution</u> of the sample mean \bar{x} ?	14) What is the <u>standard error</u> of the sample mean \bar{x} ?
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General form to calculate a confidence interval is on the Green Sheet:
 $\text{statistic} \pm (\text{critical value}) \bullet (\text{standard deviation of the statistic})$

15. What is the formula for a 1-sample t- interval for a population mean?

- a) What statistic will be used to calculate this confidence interval? _____
- b) What is the critical value? _____ with df= _____
- c) What part of this formula is the margin of error (ME)? _____

16. What conditions are required for a 1-sample t- interval for a population mean?

- R _____
 ○ _____
 ○ _____
- N _____
 ○ _____
 ○ _____
- I _____

17. Walk through example “Video Screen Tension.”

- You do not need to write the problem.
- Enter the data and use your calculator to replicate all steps. See “Technology Corner” page 514.
- **Your Notes:**

18. “Auto Pollution” example is optional. **Your Notes:**

19. What is a “Robust” procedure? And, when are t-procedures NOT robust?

20. Describe the 2 different normal conditions when using t-procedures:

- _____ ($n < 15$ and $n < 30$)

- _____ ($n \geq 30$)

21. Walk through example “People, Trees, and Flowers.” **Your Notes:**