

AP Calculus Exam Prep Assignment #6 page 2 KEY

7) Suppose f is continuous on $1 \leq x \leq 2$, that $f'(x)$ exists on $1 < x < 2$, that $f(1) = 3$, and that $f(2) = 0$. Which of the following is not necessarily true?

C) There exists a number c in $[1,2]$ such that $f'(c) = 3$

8) If $G(2) = 5$ and $G'(x) = \frac{10x}{9-x^2}$ then an estimate of $G(2.2)$ using local linearization is approximately:

C) 5.8 $y = 4x - 3$ is the equation of the tangent at $(2,5)$

9) Let $H(x) = \int_0^x f(t) dt$ where f is the function whose graph appears to the right.

The local linearization of $H(x)$ near $x = 3$ is $H(x) =$

B) $2x - 4$

10) $f(x) = \int_0^{x^2+2} \sqrt{1+\cos t} dt$. Then $f'(t) =$

A) $2x\sqrt{1+\cos(x^2+2)}$

11) $\int_0^6 f(x-1) dx =$

E) $\int_1^7 f(x) dx$

12) The number c satisfying the Mean Value Theorem for $f(x) = \sin x$ on $[1, 1.5]$ is:

$f'(c) = \frac{\sin 1.5 - \sin 1}{1.5 - 1} \approx 0.3120 \quad \cos c \approx 0.3120 \Rightarrow c \approx \cos^{-1}(0.3120) = 1.253$ D)

13) The only function that doesn't satisfy the Mean Value Theorem on the interval specified is:

D) $f(x) = x + \frac{1}{x}$ on $[-1, 1]$

