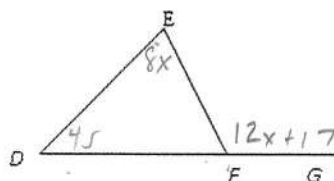


1. In the diagram shown  $m\angle EFG = 12x + 17$ ,  $m\angle FED = 8x$  and  $m\angle EDF = 45$ . Solve for  $x$ : (3 pts)

$$8x + 45 = 12x + 17$$

$$28 = 4x$$

$$7 = x$$



2. Given a regular 14 sided polygon:  
a. Find the sum of the interior angles of the polygon. (2 pts)

$$(12)(180) = 2160$$

- b. Find the measure of one exterior angle of the polygon (2 pts)

$$25.71^\circ$$

3. Write the expression in simplest form: (4 pts)

$$\frac{x^2 - 9x + 18}{9 - x^2} = \frac{(x-6)(x-3)}{(3-x)(3+x)}$$

$$\frac{6-x}{3+x} \text{ or } -\frac{(x-6)}{x+3}$$

4. If the three angles of a triangle measure  $7x - 15$ ,  $2x + 30$  and  $4x + 35$ , solve for the measure of the largest angle. (4 pts)

$$70 - 15 = 55$$

$$20 + 30 = 50$$

$$40 + 35 = 75$$

$$13x + 65 - 15 = 180$$

$$13x + 50 = 180$$

$$13x = 130$$

$$x = 10$$

5. Solve:  $x - \frac{9}{x} = -\frac{9}{2}$

$$\begin{aligned} x^2 - 9 &= -\frac{9x}{2} \\ 2x^2 - 18 &= -9x \\ 2x^2 + 9x - 18 &= 0 \\ (2x - 3)(x + 6) &= 0 \end{aligned}$$

$x = -6$   
 $x = \frac{3}{2}$   
 $-6 + \frac{3}{2} = -\frac{9}{2}$

(5 pts)

6. Each interior angle of a regular polygon measures  $140^\circ$ . How many sides does the polygon have?

$$\frac{360}{40} = 9$$

(3 pts)

7. C is the midpoint of  $\overline{AB}$ . If  $AB = 4x - 12$  and  $CB = x + 2$ , solve for x. (draw a diagram to help you)

$$\begin{aligned} x + 2 &= 2x - 6 \\ 8 &= x \end{aligned}$$



(2 pts)

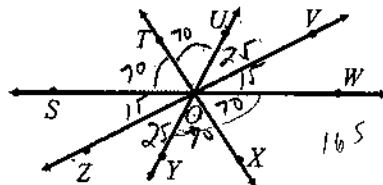
8. The supplement of an angle is 24 less than twice the angle. What is the measure of the angle and its supplement?

$$\begin{aligned} 180 - x &= 2x - 24 \\ 204 &= 3x \\ 68 &= x \\ 180 - 68 &= 112 \end{aligned}$$

(3 pts)

9. In the diagram,  $\overline{OT}$  bisects  $\angle SOU$ ,  $m\angle UOV = 25$ , and  $m\angle YOW = 140$ . Find the measure of each of the following angles.

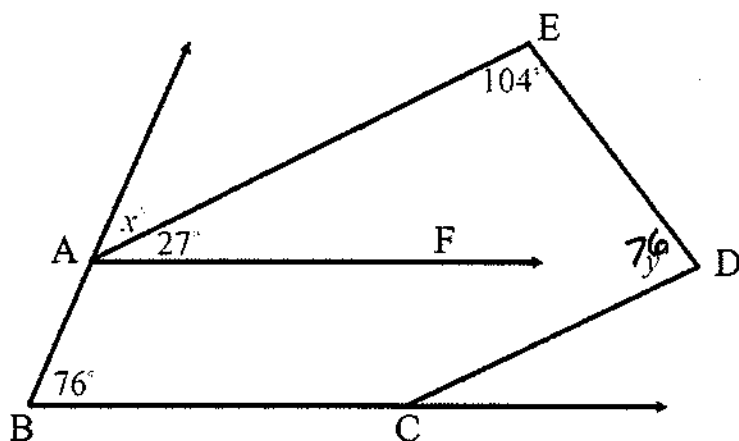
- a.  $m\angle ZOY$  25
- b.  $m\angle SOU$  140
- c.  $m\angle UOT$  70
- d.  $m\angle VOW$  15



(1 pt each)

10. In the diagram shown below,  $\overline{AF} \parallel \overline{BC}$  and  $\overline{AE} \parallel \overline{CD}$ . Solve for  $x$  and  $y$ .

(4 pts)



$$\begin{aligned} x + 27 &= 76 \\ x &= 49 \\ y &= 76 \end{aligned}$$

$$104 + y = 180$$

11. a) Write the converse of "If  $x$  is odd, then  $2x$  is even."

If  $2x$  is even then  $x$  is odd

b) Is the sentence you wrote in part a true or false? If it is false, give a counter example?

$$F_{c111} \quad x = 3$$

(4 pts)

Complete each of the following sentences with Always, Sometimes or Never: (1 pt each)

12. Two lines which never intersect are S parallel.
13. The measure of an exterior angle of a triangle is A larger than the measure of each remote interior angle.
14. If two lines are cut by a transversal and same-side interior angles are complementary the lines are N parallel.
15. A triangle N has two obtuse interior angles.
16. If two lines are parallel to the same line, then the two lines are A parallel to each other.
17. If  $p \wedge q$  is false and  $p$  is true than  $(p \wedge q) \rightarrow q$  is N false.

Multiple Choice: Circle the best answer for each question: (1 pts each)

18. If two angles of a triangle measure 56 and 68 degrees, the triangle is:

a. Obtuse    b. isosceles    c. scalene    d. right

$$\begin{array}{r} 56 \\ 68 \\ \hline 124 \end{array} \quad \begin{array}{r} 180 \\ -124 \\ \hline 56 \end{array}$$

19. The measure of an exterior angle of a triangle cannot be:

a. Exactly 90    b. Between 90 and 180    c. less than 90    d. greater than 180

20.  $\angle 1$  and  $\angle 2$  are complementary,  $m\angle 1 = 5x + 15$  and  $m\angle 2 = 10x$ , what is the measure of  $\angle 1$ ?

a. 5    b. 11    c. 40    d. 70

$$\begin{array}{r} 15x + 15 = 90 \\ 15x = 75 \\ x = 5 \end{array}$$

21. Which is not a way to prove two lines cut by a transversal are parallel:

a. Vertical angles being congruent    b. Corresponding angles being congruent  
c. Alternate int. angles being congruent    d. Same-side int. angles being supplementary

In the diagram shown,  $\overline{BG}$  bisects  $\overline{AF}$  and  $\overline{CD}$  bisects  $\angle ADE$ . State the definition, postulate or theorem that justifies each statement. (1 pt each)

22.  $AD + DF = AF$

segment addition

23.  $m\angle ADC = \frac{1}{2}m\angle ADE$

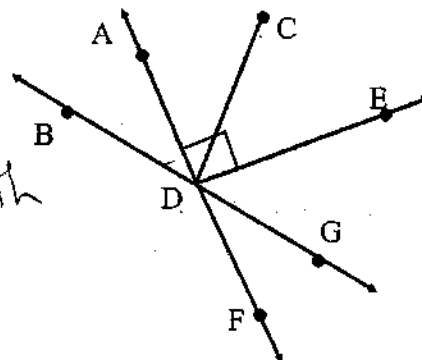
Angle bisector Th

24.  $D$  is the midpoint of  $\overline{AF}$ .

def segment bisector.

25.  $m\angle ADB = m\angle FDG$

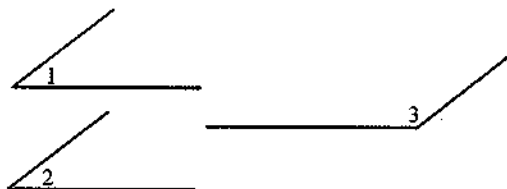
Vertical ~~angles~~



26. Fill in the missing reasons for the following proof. (4 pts)

Given:  $\angle 1$  is supplementary to  $\angle 3$   
 $\angle 2$  is supplementary to  $\angle 3$

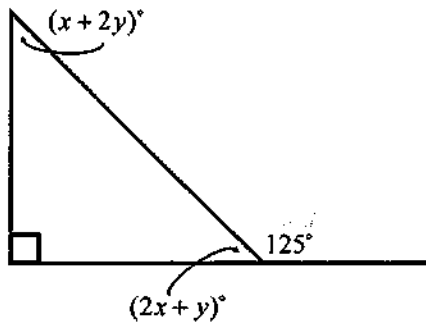
Prove:  $\angle 1 \cong \angle 2$



Statements	Reasons
1. $\angle 1$ is supplementary to $\angle 3$ $\angle 2$ is supplementary to $\angle 3$	1. Given
2. $m\angle 1 + m\angle 3 = 180$ $m\angle 2 + m\angle 3 = 180$	2. def supplementary <del>angles</del>
3. $m\angle 1 + m\angle 3 = m\angle 2 + m\angle 3$	3. transitive prop or substitution
4. $m\angle 1 = m\angle 2$	4. Reflexive Property
5. $\angle 1 \cong \angle 2$	5. Subtraction

Name the theorem that you just proved (2 pts):

If 2 ~~angles~~ are supp ~~to the same line~~  
 then the 2 ~~angles~~ are ~~congruent~~

Bonus: Solve for  $x$  and  $y$ .

$$2x + y = 55$$

$$2x + y + x + 2y = 90$$

$$3x + 3y = 90$$

$$x + y = 30$$

$$x + 55 - 2x = 30$$

$$-x = -25$$

$$x = 25$$

$$y = 5$$

# Math 423 HW #37 key

$$1. \frac{6}{x^2-1} - \frac{3}{x-1} = 2$$

$$\frac{(x+1)(x-1) \cdot 6}{(x+1)(x-1)} - \frac{(x+1)(x-1) \cdot 3}{x-1} = 2(x+1)(x-1)$$

$$6 - 3(x+1) = 2(x+1)(x-1)$$

$$6 - 3x - 3 = 2(x^2 - 1)$$

$$3 - 3x = 2x^2 - 2$$

$$2x^2 + 3x - 5 = 0$$

$$(2x+5)(x-1) = 0$$

$$2x+5=0 \quad \vee \quad x-1=0$$

$$2x = -5 \quad \vee \quad x = 1$$

$$x = \frac{-5}{2}$$

REJECT  
extraneous  
root

2.

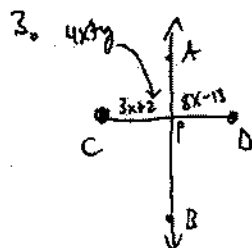
$$\frac{140^\circ}{40^\circ}$$

$$\text{interior } \angle = 140^\circ$$

$$\Rightarrow \text{exterior } \angle = 40^\circ$$

$$\frac{360}{40} = n$$

$$n = 9$$



$$3x+2 = 8x-11$$

$$5x = 15$$

$$x = 3$$

$$4x+y = 90^\circ$$

$$4(3)+y = 90^\circ$$

$$12+y = 90^\circ$$

$$y = 78$$

$$\frac{1.174}{w/12}$$

$$\text{Given: } \overline{BC} \parallel \overline{AD} \\ \overline{AB} \parallel \overline{DC}$$

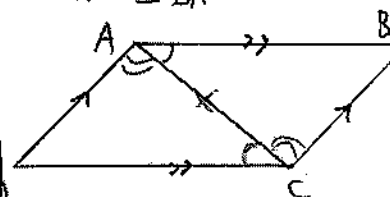
$$\text{Prove: } \triangle ABC \cong \triangle CDA$$

$$1) \overline{BC} \parallel \overline{AD}, \overline{AB} \parallel \overline{DC}$$

$$2) \angle BAC \cong \angle ACD \\ \angle DAC \cong \angle ACB$$

$$3) \overline{AC} \cong \overline{AC}$$

$$4) \triangle ABC \cong \triangle CDA$$



$$1) \text{ Given}$$

$$2) \text{ If 2 } \parallel \text{ lines CB \& AD, then alternate interior } \angle \text{ s are } \cong$$

$$3) \text{ Reflexive}$$

$$4) \text{ ASA Axiom}$$

over

$$4. 81 - x^4$$

$$(9+x^2)(9-x^2)$$

$$(9+x^2)(3+x)(3-x)$$

$$5. \text{ Let } x = \text{measure of the } \angle$$

$$\text{Then } (90-x) = \text{complement}$$

$$(180-x) = \text{supplement}$$

$$\frac{1}{2}(180-x) + (90-x) = 120^\circ$$

$$90 - \frac{1}{2}x + 90 - x = 120$$

$$180 - \frac{3}{2}x = 120$$

$$-\frac{3}{2}x = -60 \quad \cdot \frac{2}{3}$$

$$x = 40$$

$$\Rightarrow \text{complement} = 90 - 40 = 50^\circ$$

6. The inverse is:

If I do remember logic or are not motivated, then I will not look back at my old notes.

$$7. \triangle MOD \cong \triangle ACB$$

$$\Rightarrow \angle M \cong \angle A$$

$$\angle O \cong \angle C$$

$$\angle D \cong \angle B$$

$$\overline{MO} \cong \overline{AC}$$

$$\overline{OD} \cong \overline{CB}$$

$$\overline{DM} \cong \overline{BA}$$

