

# Algebra 2 Unit Plan

## Unit 3: Polynomials and Polynomial Functions



ORANGE PUBLIC SCHOOLS 2014 - 2015  
OFFICE OF CURRICULUM AND INSTRUCTION  
OFFICE OF MATHEMATICS

Algebra 2 Unit 3

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## Algebra 2 Unit 3

### Unit Overview

| Unit 3: Polynomials and Polynomial Functions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |                               |
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| Essential Questions                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |                               |                               |
| <ul style="list-style-type: none"> <li>➤ What does the degree of a polynomial tell you about its related polynomial function?</li> <li>➤ For a polynomial function, how are factors, zeros, and x-intercepts related?</li> <li>➤ For a polynomial equation, how are factors and roots related?</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                               |                               |
| Enduring Understandings                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                               |                               |
| <ul style="list-style-type: none"> <li>➤ A polynomial function has distinguishing “behaviors.” You can look at its algebraic form and know something about its graph. You can look at its graph and know something about its algebraic form.</li> <li>➤ Knowing the zeros of a polynomial function can help you understand the behavior of its graph.</li> <li>➤ If <math>(x - a)</math> is a factor of a polynomial, then the polynomial has value 0 when <math>x = a</math>. If <math>a</math> is a real number, then the graph of the polynomial has <math>(a, 0)</math> as an x-intercept.</li> <li>➤ You can divide polynomials using steps that are similar to the long-division steps that you use to divide whole numbers.</li> <li>➤ The degree of a polynomial equation tells you how many roots the equation has.</li> </ul>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                               |                               |
| Common Core State Standards                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                               |                               |
| <ul style="list-style-type: none"> <li>➤ <b>N.CN.7:</b> Solve quadratic equations with real coefficients that have complex solutions.</li> <li>➤ <b>A.CED.1:</b> Create equations and inequalities in one variable and use them to solve problems.</li> <li>➤ <b>A.SSE.1a:</b> Interpret parts of an expression such as terms, factors, and coefficients.</li> <li>➤ <b>A.SSE.2:</b> Use the structure of an expression to identify ways to rewrite it.</li> <li>➤ <b>A.APR.2:</b> Know and apply the Remainder Theorem: For a polynomial <math>p(x)</math> and a number <math>a</math>, the remainder on division by <math>x - a</math> is <math>p(a)</math>, so <math>p(a) = 0</math> if and only if <math>(x - a)</math> is a factor of <math>p(x)</math>.</li> <li>➤ <b>A.APR.3:</b> Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.</li> <li>➤ <b>A.REI.11:</b> Explain why the x-coordinates of the points where the graphs of the equations <math>y = f(x)</math> and <math>y = g(x)</math> intersect are the solutions of the equation <math>f(x) = g(x)</math></li> <li>➤ <b>F.IF.4:</b> For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity</li> <li>➤ <b>F.IF.5:</b> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes</li> <li>➤ <b>F.IF.6:</b> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph</li> <li>➤ <b>F.IF.7.c:</b> Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior.</li> <li>➤ <b>A.APR.1:</b> Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.</li> <li>➤ <b>A.APR.6:</b> Rewrite simple rational expressions in different forms; write <math>a(x)/b(x)</math> in the form <math>q(x) + r(x)/b(x)</math>, where <math>a(x)</math>, <math>b(x)</math>, <math>q(x)</math>, and <math>r(x)</math> are polynomials with the degree of <math>r(x)</math> less than the degree of <math>b(x)</math>, using inspection, long division, or, for the more complicated examples, a computer algebra system.</li> <li>➤ .</li> </ul> |                               |                               |
| <b>M</b> : Major Content                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | <b>S</b> : Supporting Content | <b>A</b> : Additional Content |

Algebra 2 Unit 3  
Calendar (Honors)

| November 2014 |                                                               |                                                                |                                                                |                                                              |                                                                     |       |
|---------------|---------------------------------------------------------------|----------------------------------------------------------------|----------------------------------------------------------------|--------------------------------------------------------------|---------------------------------------------------------------------|-------|
| Sun           | Mon                                                           | Tue                                                            | Wed                                                            | Thu                                                          | Fri                                                                 | Sat   |
| 11/16         | 11/17                                                         | 11/18                                                          | 11/19                                                          | 11/20<br>Unit 3<br>Diagnostic                                | 11/21<br>Lesson 1<br>Polynomial functions                           | 11/22 |
| 11/23         | 11/24<br>Lesson 1<br>Polynomial functions                     | 11/25<br>Lesson 2<br>Polynomials, Linear<br>factors, and zeros | 11/26<br>Lesson 2<br>Polynomials, Linear<br>factors, and zeros | 11/27<br>No School                                           | 11/28<br>No School                                                  | 11/29 |
| December 2014 |                                                               |                                                                |                                                                |                                                              |                                                                     |       |
| Sun           | Mon                                                           | Tue                                                            | Wed                                                            | Thu                                                          | Fri                                                                 | Sat   |
| 11/30         | 12/1<br>Lesson 2<br>Polynomials, Linear<br>factors, and zeros | 12/2<br>Lesson 3<br>Solving Polynomial<br>Equations            | 12/3<br>Lesson 3<br>Solving Polynomial<br>Equations            | 12/4<br>Lesson 3<br>Solving Polynomial<br>Equations          | 12/5<br>Check up 1<br>(re-teaching flexible<br>day)                 | 12/6  |
| 12/7          | 12/8<br>Lesson 4<br>Dividing Polynomials                      | 12/9<br>Lesson 4<br>Dividing Polynomial                        | 12/10<br>Lesson 4<br>Dividing<br>Polynomials                   | 12/11<br>Performance<br>Assessment<br>(Critical Area Task 1) | 12/12<br>Lesson 5<br>Polynomial Models<br>in the Real World         | 12/13 |
| 12/14         | 12/15<br>Lesson 5<br>Polynomial Models in<br>the Real World   | 12/16<br>Lesson 5<br>Polynomial Models<br>in the Real World    | 12/17<br>Check up 2<br>(re-teaching flexible<br>day)           | 12/18<br>Review                                              | 12/19<br>Performance<br>Assessment<br>(Modeling & Function<br>Task) | 12/20 |
| 12/21         | 12/22<br>Unit Assessment                                      | 12/23<br>Re-teaching                                           | 12/24<br>No school                                             | 12/25<br>No School                                           | 12/26<br>No School                                                  | 12/27 |
| 12/28         | 12/29<br>No school                                            | 12/30<br>No school                                             | 12/31<br>No school                                             | 1/1<br>No school                                             | 1/2<br>No school                                                    | 1/3   |

## Scope and Sequence

| Overview |                                        |                             |
|----------|----------------------------------------|-----------------------------|
| Lesson   | Topic                                  | Suggesting Pacing and Dates |
| 1        | Polynomial Functions                   | 2 days                      |
| 2        | Polynomials, Linear Factors, and Zeros | 3 days                      |
| 3        | Solving Polynomial Equations           | 3days                       |
| 4        | Dividing Polynomials                   | 3 days                      |
| 5        | Polynomial Models in the Real World    | 2 day                       |

## Assessment Framework

## Algebra 2 Unit 3

| Assessment                                                                 | CCSS                                                                                                                                  | Estimated Time | Format     | Graded |
|----------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------|----------------|------------|--------|
| Diagnostic/Readiness Assessment<br>(Beginning of Unit)                     | A.CED.2, F.IF.5, A.CED.1,<br>A.APR.3, A.REI.4.b                                                                                       | ½ Block        | Individual | No     |
| Assessment Check Up 1<br>(After lesson 5.3)                                | F.IF.7.c, A.SSE.1.a, A.APR.3,<br>A.REI.11, A.SSE.2, A.APR.2,<br>A.APR.1, A.APR.6                                                      | ½ Block        | Individual | Yes    |
| Performance (Critical Area) Task<br>Graphing from Roots                    | A.APR.2, A.APR.3                                                                                                                      | ½ Block        | Individual | Yes    |
| Check up 2<br>Pearson Algebra II Chapter 5 quiz<br><i>p 311</i>            | F.IF.7.c, A.SSE.1.a, A.APR.3,<br>A.REI.11, A.SSE.2, A.APR.2,<br>A.APR.1, A.APR.6                                                      | ½ Block        | Individual | Yes    |
| Unit 3 Assessment                                                          | F.IF.7.c, A.REI.11, A.APR.2,<br>N.CN.7, N.CN.8, F.IF.5,<br>A.SSE.1a, A.APR.3, A.SSE.2,<br>A.APR.1, A.APR.6, N.CN.9,<br>F.IF.4, F.IF.6 | 1 Block        | Individual | Yes    |
| Performance (Modeling)Task<br>Introduction to Polynomials:<br>College Fund | A.REI.11, A.CED.1.a                                                                                                                   | 1 Block        | Pair/group | Yes    |
| Others                                                                     |                                                                                                                                       |                |            |        |

## Lesson Analysis

## Lesson 1: Polynomial Functions

### Objective

- Using standard form of a polynomial function, students will work individually/in pair/in group to classify polynomial and describe end behavior of polynomial functions, ASB correctly answering \_\_\_\_ exit slip questions.

### Focused Mathematical Practices

- MP2: Reason abstractly and quantitatively
- MP 5: Use appropriate tools strategically
- MP 7: Look for and make use of structure

Vocabulary: Monomial, degree of a monomial, polynomial, degree of a polynomial, polynomial function, standard form of a polynomial function, roots, zeros, turning point, end behavior

### Common Misconceptions:

- Classifying polynomial by degree – students choose degree based on first term, before putting function in standard form
- Describing end behavior of a polynomial – students may forget the rules of the table, then incorrectly plug values into the polynomial equation (specifically, plugging in a negative number. i.e. incorrectly stating that  $(-1)^2 = -1$ )

| Most relevant CCSS                                                                                                                 | Concepts<br>What students will know                                                                                                                                                                                                                                                                                                                                                                                                                                  | Skills<br>What students will be able to do                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | Material/<br>Resource                  | Suggested<br>Pacing | Assessment<br>Check Point                |
|------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------|---------------------|------------------------------------------|
| <b>F.IF.7.c:</b> Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior | <p><b>Review</b></p> <ul style="list-style-type: none"> <li>Vocabulary (degree, standard form, monomial, polynomial, leading term, increasing / decreasing, end-behavior)</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>Polynomials can be classified by degree or number of terms</li> <li>A function is increasing when the y-values increase as x-values increase, and is decreasing when y-values decrease as x-values increase</li> </ul> | <p><b>Review</b></p> <ul style="list-style-type: none"> <li>Create a table for a pattern / write a pattern rule</li> <li>Identify a pattern using common differences, and find the value of nth term of a pattern</li> <li>Write a polynomial in standard form in order to more easily classify by degree</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>Determine end behavior of a polynomial from leading term</li> <li>Use common differences in y-values to determine degree of a polynomial</li> </ul> | Lesson 5.1 / online textbook resources | 2 days              | Lesson Check: pg. 285 (use as exit slip) |

## Lesson 2: Polynomials, Linear Factors, and Zeros

## Algebra 2 Unit 3

### Objective

- Using factored form of a polynomial, SWBAT analyze and graph the polynomial function showing key features, ASB correctly answering \_\_\_\_ exit slip questions.
- Using zeros of a polynomial, SWBAT create a polynomial function from its zeros, ASB correctly answering \_\_\_\_ exit slip questions.

### Focused Mathematical Practices

- MP 1: Make sense of problems and persevere in solving them
- MP 2: Use appropriate tools strategically
- MP 3: Construct viable arguments and critique the reasoning of others

Vocabulary: Factor theorem, multiple zero, linear factor, multiplicity, relative maximum, relative minimum

### Common Misconceptions:

- Errors with determining zeros from factors (i.e. errors with zero product property: choosing (2,0) as the zero corresponding to a factor of  $(x + 2)$ , also errors with negatives – ex. factor:  $-(x + 4)$ , also forgetting the (0,0) zero corresponding to a factor of “x”)
- Graphing polynomials: forgetting to plot the y-intercept, incorrectly following curve of the polynomial graph (errors with turning points / even-touch odd-cross)
- Errors with distributive property when writing polynomial from zeros

| Most Relevant CCSS                                                                                                                                                                                                                                                                                                          | Concepts<br>What students will know                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Skills<br>What students will be able to do                                                                                                                                                                                                                                                                                                                                                                                                                                           | Material/<br>Resource | Suggested<br>Pacing | Assessment<br>Check Point             |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------|---------------------|---------------------------------------|
| <b>F.IF.7.c:</b> Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior<br><br><b>A.APR.3:</b> Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial. | <b>Review</b> <ul style="list-style-type: none"> <li>Polynomial increasing / decreasing rules learned in Lesson 5.1</li> </ul> <b>New</b> <ul style="list-style-type: none"> <li><math>(x - b)</math> is a linear factor of the polynomial <math>P(x)</math>, <math>b</math> is a zero of the polynomial function <math>y = P(x)</math>, <math>b</math> is a root (or solution) of the polynomial equation <math>P(x) = 0</math>, and <math>b</math> is an x-intercept of the graph of <math>y = P(x)</math></li> </ul> | <b>Review</b> <ul style="list-style-type: none"> <li>Determining end-behavior from the leading term</li> <li>Factor a polynomial – specifically with GCF</li> </ul> <b>New</b> <ul style="list-style-type: none"> <li>Use zero product property to determine zeros of the polynomial</li> <li>Graph a polynomial using zeros, y-intercept, end-behavior, and test points</li> <li>Create a polynomial function from its zeros</li> <li>Finding the multiplicity of a zero</li> </ul> | Lesson 5.2            | 3 days              | Lesson check: pg 22; #'s 1, 3, 5, & 7 |



## Algebra 2 Unit 3

### Objective

- Using factoring and graphing skills, SWBAT solve a polynomial equation, ASB correctly answering 3 / 3 exit slip questions.

### Focused Mathematical Practices

- MP 1: Make sense of problems and persevere in solving them
- MP 3: Construct viable arguments and critique the reasoning of others.
- MP 5: Use appropriate tools
- MP 6: Attend to precision

Vocabulary: Sum of cubes, difference of cubes

### Common Misconceptions:

- Forgetting the "0" solution (ex.  $x(2x + 1)(x - 3)$ )
- Incorrectly writing an x-intercept (ex. (0,4) instead of (4,0))
- Factoring errors (students especially struggle with factoring quadratics with a  $\neq 1$ , sum / difference of cubes, and remembering to check for GCF first)
- Quadratic formula errors (students often incorrectly plug numbers into the formula) – specifically with imaginary solutions (students will simplify  $\sqrt{-9}$  as 3, instead of  $3i$ )

| Most relevant CCSS                                                                                                                                                                                                                                                                                                                                                                                                                  | Concepts<br>What students will know                                                                                                                                                                                                                          | Skills<br>What students will be able to do                                                                                                                                                                                                                                                                                                                                                                           | Material/<br>Resource                                                                                                                                                                                                                                                                                                                                                                                | Suggested<br>Pacing | Assessment<br>Check Point                   |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------|---------------------------------------------|
| <b>A.REI.11:</b> Explain why the x-coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$<br><br><b>A.SSE.2</b> Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$ , thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$ . | <b>Review</b> <ul style="list-style-type: none"> <li>Zero product property</li> </ul> <b>New</b> <ul style="list-style-type: none"> <li>The real solutions to a polynomial equation give the x-intercepts of the graph of the polynomial function</li> </ul> | <b>Review</b> <ul style="list-style-type: none"> <li>Factor methods: factoring out GCF, factoring quadratic trinomials (algebra tiles, x-method, box method, etc.), perfect square trinomials, difference of squares, factor by grouping</li> <li>Determine zeros from factors</li> <li>Quadratic formula</li> </ul> <b>New</b> <ul style="list-style-type: none"> <li>Factor sum and difference of cubes</li> </ul> | *Lesson 5.3,<br>*5.3 Game: Discovering Your Roots (resource online),<br>*Polynomial Factoring BINGO,<br>*"Factor This" game from Lesson 4.4 (resource online),<br>*Factor Stations (see example in Supplemental Materials section),<br>*Solving for Zeros Discovery Activity (see example in Supplemental Material section),<br>*Box Problem Authentic Assessment (see Authentic Assessment section) | 3 days              | Lesson Check pg. 300; #s 1-7, 9 (#8 honors) |

## Lesson 4: Dividing Polynomials

## Objective

- Using long division and synthetic division, SWBAT rewrite polynomials in factor forms or in the form of  $q(x) + r(x)/b(x)$ , ASB correctly answering \_\_\_\_ exit slip questions.

## Focused Mathematical Practices

- MP 3: Construct viable arguments and critique the reasoning of others.
- MP 7: Look for and make use of structure
- MP 6: Attend to precision

Vocabulary: synthetic division, Remainder theorem, divisor, quotient, remainder, dividend, dimensions

## Common Misconceptions:

- Distributing negative sign when subtracting (i.e.  $-(4x^2 + 20x) = -4x^2 - 20x$ )
- Students stop long division process before the remainder is a polynomial with one degree less than the original polynomial

| CCSS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | Concepts<br>What students will know                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | Skills<br>What students will be able to do                                                                                                                                                                                                                                                                                                                                                                                                                                             | Material/<br>Resource                                                                                                                                                                                                      | Suggested<br>Pacing | Assessment<br>Check Point                                                                                                         |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------|-----------------------------------------------------------------------------------------------------------------------------------|
| <p><b>A.APR.2:</b> Know and apply the Remainder Theorem: For a polynomial <math>p(x)</math> and a number <math>a</math>, the remainder on division by <math>x - a</math> is <math>p(a)</math>, so <math>p(a) = 0</math> if and only if <math>(x - a)</math> is a factor of <math>p(x)</math></p> <p><b>A.APR.6:</b> Rewrite simple rational expressions in different forms; write <math>a(x)/b(x)</math> in the form <math>q(x) + r(x)/b(x)</math>, where <math>a(x)</math>, <math>b(x)</math>, <math>q(x)</math>, and <math>r(x)</math> are polynomials with the degree of <math>r(x)</math> less than the degree of <math>b(x)</math>, using inspection, long division, or, for the more complicated examples, a computer algebra system.</p> | <p><b>Review:</b></p> <ul style="list-style-type: none"> <li>* Concepts of long division Algorithm</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>* The Division Algorithm for Polynomials is a generalized version of the technique of long division in arithmetic.</li> <li>• (Divisor)(Quotient) + Remainder = Dividend<br/>OR <math>P(x) = D(x)Q(x) + R(x)</math></li> <li>• If <math>R(x) = 0</math>, then <math>P(x) = D(x)Q(x)</math> and <math>D(x)</math> and <math>Q(x)</math> are factors of <math>P(x)</math></li> </ul> | <p><b>Review</b></p> <ul style="list-style-type: none"> <li>• Numerical long division</li> <li>• Factoring out GCF</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>• Long division – polynomials</li> <li>• Synthetic division – polynomials</li> <li>• Using Remainder Theorem to evaluate a polynomial function</li> <li>• <b>Use division of polynomial to rewrite expressions in different forms:</b><br/><math>a(x)/b(x) = q(x) + r(x)/b(x)</math></li> </ul> | <p>Lesson 5.4</p> <p>Divide using algebra tiles:<br/><a href="http://www.doe.virginia.gov/testing/solsearch/sol/math/A/m_ess_a-2b_1.pdf">http://www.doe.virginia.gov/testing/solsearch/sol/math/A/m_ess_a-2b_1.pdf</a></p> | 3 days              | <p>Lesson Check pg. 308 #s 1 – 5</p> <p>Class discussion on #s 6 &amp; 7</p> <p>#8 challenge</p> <p>Mid-Chapter Quiz: pg. 311</p> |

## Lesson 5: Polynomial Models in the Real World

## Objective

- Using Ti-84 graphing calculator, SWBAT fit data to linear, quadratic, cubic, or quartic models, ASB correctly answering 5 / 6 exit slip questions.

## Focused Mathematical Practices

- MP 1: Make sense of problems and persevere in solving them
- MP 4: Model with mathematics
- MP 5: Use appropriate tools strategically

Vocabulary: regression, the  $(n + 1)$  Point Principle

## Common Misconceptions:

- Only one type of model can fit a given data set
- Choosing a model that doesn't *best* fit a data set

| CCSS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Concepts<br>What students will know                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Skills<br>What students will be able to do                                                                                                                                                                                                                                                                                                   | Material/<br>Resource | Suggested<br>Pacing | Assessment Check<br>Point                       |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------|---------------------|-------------------------------------------------|
| <p><b>F.IF.4:</b> For a function that models a relationship between two quantities, and sketch graphs showing key feature given a verbal description of the relationship.</p> <p><b>F.IF.5:</b> Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes</p> <p><b>F.IF.6:</b> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.</p> <p><b>A.CED.1:</b> Create equations and inequalities in one</p> | <p><b>Review</b></p> <ul style="list-style-type: none"> <li>Domain of a function is all the possible x-values</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>You can use polynomial functions to model many real-world situations. The behavior of the graphs of polynomial functions of different degrees can suggest what type of polynomial will best fit a particular data set.</li> <li>For any set of <math>n + 1</math> points in the coordinate plane that pass the vertical line test, there is a unique polynomial of degree at most <math>n</math> that fits the points perfectly</li> <li>The best model for a data set often depends on the situation.</li> <li>When making predictions based on a regression model, stay within domain of the function for greater confidence</li> </ul> | <p><b>Review</b></p> <ul style="list-style-type: none"> <li>Evaluate a function for a given coordinate pair</li> </ul> <p><b>New</b></p> <ul style="list-style-type: none"> <li>Use LINREG, QUADREG, CUBICREG on Ti-84 to model data set</li> <li>Use RREF() function on Ti-84 to find coefficient values for polynomial function</li> </ul> | Lesson 5.8            | 2 day               | Lesson check pg. 335 #s 1 – 6 (5 & 6 challenge) |

## Algebra 2 Unit 3

variable and use them to solve problems.

### Ideal Math Block

*The following outline is the department approved ideal math block for grades 9-12.*

- 1) Do Now (7-10 min)
  - a. Serves as review from last class' or of prerequisite material
  - b. Provides multiple entry points so that it is accessible by all students and quickly scaffolds up
- 2) Starter/Launch (5 min)
  - a. Designed to introduce the lesson
  - b. Uses concrete or pictorial examples
  - c. Attempts to bridge the gap between grade level deficits and rigorous, on grade level content
  - d. Provides multiple entry points so that it is accessible by all students and quickly scaffolds up
- 3) Mini-Lesson (15-20 min)
  - a. Design varies based on content
  - b. May include an investigative approach, direct instruction approach, whole class discussion led approach, etc.
  - c. Includes CFU's
  - d. Anticipates misconceptions and addresses common mistakes
- 4) Class Activity (25-30 min)
  - a. Design varies based on content
  - b. May include partner work, group work/project, experiments, investigations, game based activities, etc.
- 5) Independent Practice (7-10 min)
  - a. Provides students an opportunity to work/think independently
- 6) Closure (5-10 min)
  - a. Connects lesson/activities to big ideas
  - b. Allows students to reflect and summarize what they have learned
  - c. May occur after the activity or independent practice depending on the content and objective
- 7) DOL (5 min)
  - a. Exit slip

## Sample Lesson Plan

|                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |             |                                                                                                                                    |
|---------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|------------------------------------------------------------------------------------------------------------------------------------|
| <b>Lesson</b>                         | 2: Polynomials, Linear Factors, and Zeros (Day 2 Lesson)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | <b>Days</b> | 1                                                                                                                                  |
| <b>Objective</b>                      | Using factored form of a polynomial, SWBAT analyze and graph the polynomial function, ASB correctly answering 3 / 3 exit slip questions.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | <b>CCSS</b> | <b>F.IF.7.c:</b> Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior |
| <b>Learning activities/strategies</b> | <p>Lesson Material (see</p> <p>Do Now: (8 minutes) -- using graphing calculator</p> <p>*Sketch the graph of <math>f(x) = x^2</math>. What will the graph of <math>g(x)=x^4</math> look like? Sketch it on the same coordinate plane. What will the graph of <math>h(x) = x^6</math> look like?</p> <p>Launch : Discussion: Use the graphs from the Do Now to frame the following discussion about end behavior.</p> <p>* Ask students to compare and describe the behavior of the value <math>f(x)</math> as the absolute value of <math>x</math> increase without bound.</p> <p>Mini Lesson:</p> <p>* Introduce the term “end behavior”<br/>( end behavior is way to describe what happens to the function as <math>x</math> approaches positive and negative infinity without having to draw the graph)</p> <p>* use the picture on material page 166 to help students understand the description of end behavior</p> <p>Investigation: (see material example 1)</p> <p>* Tell students that we are now going to look at a new set of functions:<br/>Sketch the graph of <math>f(x) = x^3</math>. What will the graph of <math>g(x)= x^5</math> look like? Sketch this on the same coordinate plane. What will the graph of <math>h(x) = x^7</math> look like? Sketch this on the same coordinate plane.</p> <p>* Ask students share their finding and take notes about their finding</p> <p>Practice 1: (pair work)</p> <p>* Ask students use the notes that they took from the investigation and work with partners to answer the following questions: (See material page 169)</p> <p>Practice 2: (individual work)</p> <p>* Students will use what they learned today about end behavior to determine whether or not eh polynomial function used to model the data has an even or odd degree.<br/>(See material page 170)</p> <p>Closure:</p> |             |                                                                                                                                    |

## Algebra 2 Unit 3

|                                          |                                                                                                                                                                                                                                                                                                                           |
|------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                          | <p>* Have students summarize the lesson either with a graphic organizer or a written summary. (see material page 171)</p> <p>Exit Ticket: Without using a graphing utility, match each graph with the function . (see material page 172)</p>                                                                              |
| <b>Differentiation</b>                   | <p><b><i>Possible differentiation strategies: (please design your own differentiation based on your students learning styles, academic level, strength and weakness,.....)</i></b></p> <p>* Heterogeneous grouping to allow for peer mentoring throughout investigation activity</p> <p>*Calculators will be provided</p> |
| <b>Assessment</b>                        | <p>Formative: *circulating throughout class during lesson,</p> <p>*observe students when they are answering questions, discussing with their partner, working on class work...etc.</p> <p>*exit slip</p> <p>* homework</p>                                                                                                |
| <b>Common Misconceptions/ Difficulty</b> |                                                                                                                                                                                                                                                                                                                           |

**Supplemental Material**

| CCSS                                   | Dropbox Location and Filename                                                                                                | Link (Original Task)                                                                                                                                                                                                                                    |
|----------------------------------------|------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| A-SSE, A-APR, F-IF, F-BF               | Orange 9-12 Math > Algebra 2 > Unit 3 > Supplemental Material > <b>Presenting Polynomials</b>                                | <a href="http://ecsd-fl.schoolloop.com/file/1298972684338/1298972684200/7226566668305715428.pdf">http://ecsd-fl.schoolloop.com/file/1298972684338/1298972684200/7226566668305715428.pdf</a>                                                             |
| A.SSE2, A.SSE 3, A-APR2, A-APR3, F-IF7 | Orange 9-12 Math > Algebra 2 > Unit 3 > Supplemental Material > Finding roots when degree is three or higher                 | <a href="http://www.atlanta.k12.ga.us/cms/lib/GA01000924/Centricity/Domain/262/CCGPS_Math_III_Unit_2_WEB_TE_August_2010v1.pdf">http://www.atlanta.k12.ga.us/cms/lib/GA01000924/Centricity/Domain/262/CCGPS_Math_III_Unit_2_WEB_TE_August_2010v1.pdf</a> |
| A-APR.2, A-APR.6                       | Orange 9-12 Math > Algebra 2 > Unit 3 > Supplemental Material > <b>Dividing polynomial using alg. tiles</b>                  | <a href="http://www.doe.virginia.gov/testing/solsearch/sol/math/A/m_ess_a-2b_1.pdf">http://www.doe.virginia.gov/testing/solsearch/sol/math/A/m_ess_a-2b_1.pdf</a>                                                                                       |
| A-APR.3, A-APR.6                       | Orange 9-12 Math > Algebra 2 > Unit 3 > Supplemental Material > <b>Graphing Polynomial Functions Activity</b>                |                                                                                                                                                                                                                                                         |
| A-APR.3, A-APR.6                       | Orange 9-12 Math > Algebra 2 > Unit 3 > Supplemental Material > <b>Polynomials, linear factors, &amp; zero sample lesson</b> |                                                                                                                                                                                                                                                         |

## Multiple Representations

| Multiple Representation (Dividing Polynomial)             |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
|-----------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p><b>Concreted Model</b></p>                             | <p>Key:</p> <div style="display: flex; align-items: center; gap: 10px;"> <div style="text-align: center;"> <math>\overset{1}{\underset{1}{\boxed{1}}}</math> </div> <div style="text-align: center;"> <math>\overset{1}{\underset{x}{\boxed{x}}}</math> </div> <div style="text-align: center;"> <math>\overset{x}{\underset{x^2}{\boxed{x^2}}}</math> </div> </div><br><div style="display: flex; align-items: center; justify-content: center;"> </div> <p style="text-align: center;"><math>(x^2 + 7x + 6) \div (x + 1)</math></p><br><p style="text-align: center;"><b>Quotient <math>Q(x) = (x + 6)</math></b></p> <div style="display: flex; align-items: center; justify-content: center;"> <div style="text-align: center; margin-right: 20px;"> <p><b>Divisor</b><br/><math>D(x) = (x + 1)</math></p> </div> <div style="text-align: center; margin-left: 20px;"> <p><b>Divident <math>P(x) = (x^2 + 7x + 6)</math></b></p> </div> </div> |
| <p><b>Symbolic<br/>(Polynomial Long<br/>Division)</b></p> |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |



$$\begin{array}{r}
 \phantom{x^2 + 7x + 6} x + 6 \\
 \hline
 x + 1 \overline{) x^2 + 7x + 6} \\
 \underline{x^2 + \phantom{7}x} \phantom{+ 6} \\
 6x + 6 \\
 \underline{6x + 6} \\
 0
 \end{array}$$

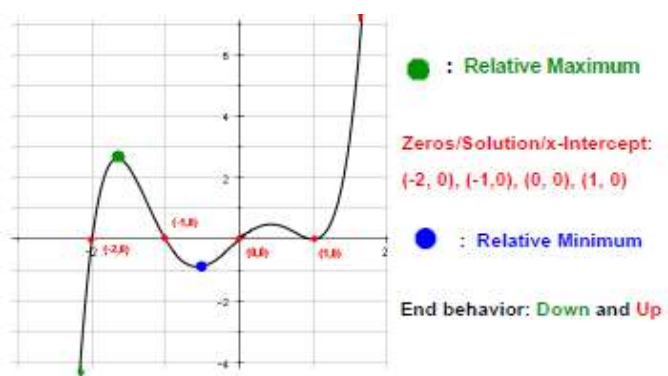
Remainder  $R(x) = 0$ 

$$\begin{aligned}
 \text{Divident} &= (\text{Divisor})(\text{quotient}) + \text{Remainder} \\
 P(x) &= D(x)Q(x) + R(x)
 \end{aligned}$$

### Polynomial Graph

Using graph to  
show  
vocabulary

Key features of polynomial function graph

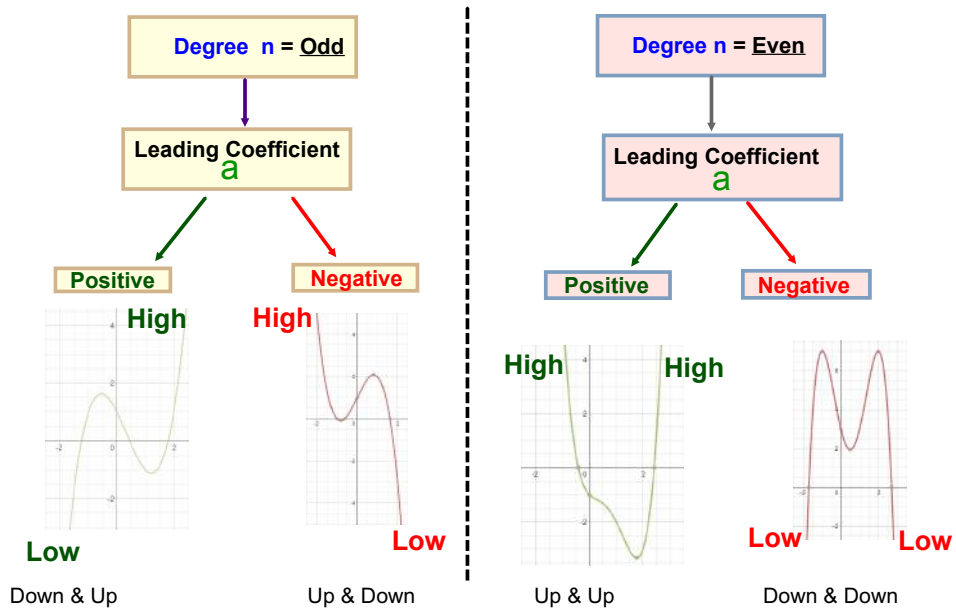


End Behavior of a Polynomial Function With Leading Term  $ax^n$

# Using Graphing Organizer

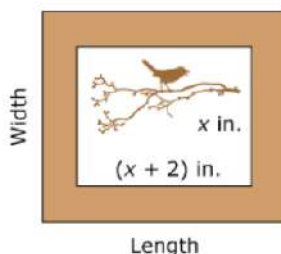
## Leading Coefficient Test (Predicting End Behavior)

$$ax^n + bx^{n-1} + c x^{n-2} \dots$$





Sam uses one-inch frames for pictures for which the length is 2 inches (in.) longer than the width, as shown.



The area of the frame for a picture that is  $x$  inches wide is given by the expression:

$$(x + 4)(x + 2) - (x + 2)x$$

There are four descriptions shown. Drag the correct expression to the appropriate box below the corresponding description.

|            |                  |           |
|------------|------------------|-----------|
| $x$        | $(x + 2)$        | $(x + 4)$ |
| $(x + 2)x$ | $(x + 4)(x + 2)$ |           |

the length of the  
picture alone, in  
inches

the length of the  
frame, in inches

the area of the  
picture alone, in  
square inches

the area of the  
picture and frame  
together, in  
square inches





Click on a choice and drag it to a box.

| HS                                                | Picture Frame                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |
|---------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Type                                              | Type I 2 Points                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
| Evidence Statement                                | <p><b>A-SSE.1-2:</b> Interpret quadratic expressions that represent a quantity in terms of its context.</p> <p>a) Interpret parts of an expression, such as terms, factors, and coefficients.</p> <p>b) Interpret complicated expressions by viewing one or more of their parts as a single entity</p>                                                                                                                                                                                                                                       |
| Most Relevant Standards for Mathematical Content  | <p><b>A-SSE.1:</b> Interpret expressions that represent a quantity in terms of its context.</p> <p>a. Interpret parts of an expression, such as terms, factors, and coefficients.</p> <p>b. Interpret complicated expressions by viewing one or more of their parts as a single entity. <i>For example, interpret <math>P(1+r)^n</math> as the product of <math>P</math> and a factor not depending on <math>P</math>.</i></p> <p>This standard is major content in the course based on the PARCC Model Content Frameworks.</p>              |
| Most Relevant Standards for Mathematical Practice | This task requires students to make use of the structure provided in the diagram and the formula (MP.7). In addition, students must contextualize that structure to address the descriptions (MP.2).                                                                                                                                                                                                                                                                                                                                         |
| Item Description and Assessment Qualities         | <p>This application task requires students to understand a diagram and formula, and then use expressions within that formula to represent a quantity in terms of its context. The situation allows for possible explanations so students have to carefully attend to the meaning of the variable and the context of the situation.</p> <p>The answer space is technology-enhanced so it can be scored immediately. Unlike traditional multiple choice, it is difficult to guess the correct answer or use a choice elimination strategy.</p> |
| Scoring Information                               | <p>The length of the picture alone in inches: <math>(x + 2)</math></p> <p>The length of the frame in inches: <math>(x + 4)</math></p> <p>The area of the picture alone in square inches: <math>(x + 2)x</math></p> <p>The area of the picture and frame together in square inches: <math>(x + 4)(x + 2)</math></p> <p>The student must get all 4 parts correct to earn 2 points and 3 parts correct to earn 1 point.</p>                                                                                                                     |

**Unit 3 Performance Assessment Task (Critical Area)**

Graphing from Roots

CCSS: A.APR.2, A.APR.3 (No calculator allowed)

Mike is trying to sketch a graph of the polynomial

$$F(x) = x^3 + 4x^2 + x - 6$$

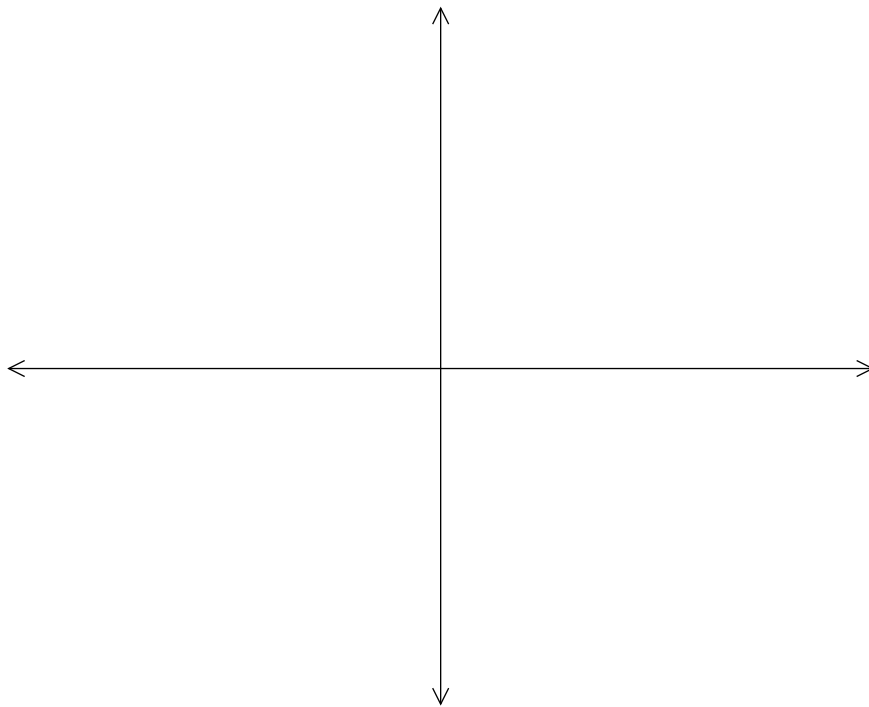
He notices that the coefficients of  $f(x)$  add up to zero (  $1 + 4 + 1 - 6 = 0$  ) and says

“ This means that 1 is a root of  $f(x)$ , and I can use this to help factor  $f(x)$  and produce the graph.”

Part A: Is Mike right that 1 is a root of  $f(x)$ ? Explain your reasoning.

Part B: Find all roots of  $f(x)$ .

Part C: Sketch a graph of the function  $f(x)$  and show key features of the graph (i.e. zeros, y-intercept, end of behaviors)



Part D: Find all inputs  $x$  for which  $f(x) < 0$

**Unit 3 Performance Assessment Task (Modeling)****College Fund**

When Marcus started high school, his grandmother opened a college savings account. On the first day of each school year she deposited money into the account: \$1000 in his freshmen year, \$600 in his sophomore year, \$1100 in his junior year and \$900 in his senior year. The account earns interest of at the end of each year.

Part A: If  $r$  is the annual interest rate of the bank account, at the end of the year the balance in the account is multiplied by a growth factor of  $x = 1 + r$ . Find an expression for the total amount of money Marcus receives by the end of each year in terms of  $x$ . (Simplify your expressions)

End of 1<sup>st</sup> year of high school:

End of 2<sup>nd</sup> year of high school:

End of 3<sup>rd</sup> year of high school:

End of 4<sup>th</sup> year of high school:

Part B: When Marcus starts college after four years of high school, he gets the balance of the savings account plus an extra \$500. Suppose that altogether he receives \$4400 from his grandmother. Use appropriate technology to find the growth factor of  $x$ .

Part C: What is the annual interest rate  $r$  of the bank account?

Part D. How much total interest did the bank account earn over the four years?

## **Additional Resources**

From [pearsonsuccessnet.org](http://pearsonsuccessnet.org)

- Find the errors
- Enrichment
- Re-teaching
- Activities, games, and puzzles
- Performance tasks
- Chapter project

Pearson Algebra 2 Common Core Teacher's Edition

Student Resources

From [pearsonsuccessnet.org](http://pearsonsuccessnet.org);

- Standardized test prep
- Homework tutors
- Think about a plan
- Student companions

Student workbook