



Unit 1 Equations in One Variable



Expressions, Equations, and Functions

Prerequisite Skills

1.1	Evaluate Expressions	-
1.2	Apply Order of Operations	
1.3	Write Expressions	
1.4	Write Equations and inequalities	
1.5	Use a Problem Solving Plan	
1.6	Represent Functions as Rules and Tables	_
1. 7	Represent Functions as Graphs 4 Investigating Algebra Activity: Scatter Plots and Functions 4 Extension: Determine Whether A Relation is a Function 4 Mixed Review of Problem Solving 5	3

ASSESSMENT

	Quízzes	
	Chapter Summary and Review	
	Chapter Test. Standardized Test Preparation and Practice	52
k	Standardized Test Preparation and Practice	57
	and reparation and riduce	58

Chapter 1 Highlights

PROBLEM SOLVING

- Mixed Review of Problem Solving, 27, 51
- Multiple Representations, 33, 39
- Multi-Step Problems, 6, 11, 19, 27, 40, 51
- Using Alternative Methods, 34
- Real-World Problem Solving Examples, 4, 10, 17, 23, 28, 30, 35, 37, 45

* ASSESSMENT

- Standardized Test Practice Examples, 10, 30
- Multiple Choice, 5, 6, 11, 18, 24, 25, 31, 38, 46
- Short Response/Extended Response, 7, 12, 20, 26, 27, 32, 33, 40, 48, 51, 58
- Writing/Open-Ended, 5, 10, 12, 18, 19, 24, 25, 27, 31, 38, 39, 46, 47, 51, 53

TECHNOLOGY

- At <u>classzone.com</u>:
- *@Home Tutor*, xxii, 6, 11, 13, 19, 25, 32, 39, 41, 47, 53
- Online Quiz, 7, 12, 20, 26, 33, 40, 48
- Electronic Function Library, 52
- State Test Practice, 27, 51, 61

CHAPTER

Unit 1

Equations in **Orie Variable**



Properties of Real Numbers

	Prerequisite Skills
2.1	Use Integers and Rational Numbers
2.2	Add Real Numbers
2.3	Subtract Real Numbers
2.4	Multiply Real Numbers
2.5	Apply the Distributive Property
2.6	Divide Real Numbers
2.7	Find Square Roots and Compare Real Numbers 110 Investigating Algebra Activity: Writing Statements in If-Then Form 109 Extension: Use Logical Reasoning 117 Mixed Review of Problem Solving 119

ASSESSMENT

Qu	lizzes	116
- CN	apter Summary and Review	120
- u	aner lest	172
★ Sta	indardized Test Preparation and Practice	176

Chapter 2 Highlights

PROBLEM SOLVING

- Mixed Review of Problem Solving, 86, 119
- * Multiple Representations, 83, 93, 116 * Multi-Step Problems, 69, 78, 86, 107,
- 115, 119 * Using Alternative Methods, 102
- * Real-World Problem Solving Examples, 65, 76, 81, 90, 98, 104, 111

***** ASSESSMENT

- Standardized Test Practice Examples, 98
- Multiple Choice, 68, 69, 78, 82, 92, 99, 106, 107, 108, 114
- Short Response/Extended Response, . 70, 79, 83, 86, 92, 93, 100, 101, 108, 115, 119, 126
- Writing/Open-Ended, 67, 77, 82, 83, 86, 91, 99, 106, 107, 113, 114, 119

TECHNOLOGY

At dasszone.com:

- **Contractions**, 63, 73, 80, 90, 93, 98
- @Home Tutor, 62, 69, 78, 83, 92, 100, 107, 115, 121
- Online Quiz, 70, 79, 84, 93, 101, 108, 116
- State Test Practice, 86, 119, 129

CHAPTER

Unit 1 Equations in One Variable



Solving Equations, p. 143 8517 = 2117 + 64d

Solving Linear Equations

	Prerequisite Skills 130	
3.1	Solve One-Step Equations	
3.2	Solve Two-Step Equations	
3.3	Solve Multi-Step Equations	
3.4	Solve Equations with Variables on Both Sides	
3.5	Write Ratios and Proportions 162	
3.6	Solve Proportions Using Cross Products	
3.7	Solve Percent Problems	
3.8	Rewrite Equations and Formulas	

ASSESSMENT

Quizzes	153, 173, 189
Chapter Summary and Review	
Chapter Test	
* Standardized Test Preparation and Practice	
Cumulative Review, Chapters 1–3	

Chapter 3 Highlights

PROBLEM SOLVING

- Mixed Review of Problem Solving, 161, 190
- Multiple Representations, 139, 146, 147, 153, 159, 166, 172, 188
- Multi-Step Problems, 140, 146, 161, 167, 190
- Using Alternative Methods, 147
- Real-World Problem Solving Examples, 137, 143, 150, 155, 164, 170, 178, 186

* ASSESSMENT

- Standardized Test Practice Examples, 149, 169
- Multiple Choice, 138, 144, 145, 151, 157, 165, 171, 179, 187, 198
- Short Response/Extended Response, 139, 140, 145, 146, 151, 152, 159, 161, 166, 167, 172, 173, 180, 181, 189, 190
- Writing/Open-Ended, 137, 139, 144, 150, 151, 157, 161, 165, 171, 179, 180, 181, 187, 188, 190

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- @Home Tutor, 130, 139, 145, 152, 158, 160, 166, 172, 180, 188, 192
- Online Quiz, 140, 146, 153, 159, 167, 173, 181, 189
- State Test Practice, 161, 190, 201

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3.1 Solve One-Step Equations



You solved equations using mental math. You will solve one-step equations using algebra. So you can determine a weight limit, as in Ex. 56.

Key Vocabulary

inverse operations

 equivalent equations

reciprocal, p. 915

Inverse operations are two operations that undo each other, such as addition and subtraction. When you perform the same inverse operation on each side of an equation, you produce an *equivalent equation*. Equivalent equations are equations that have the same solution(s).

KEY CONCEPT

For Your Notebook

Addition Property of Equality

Words Adding the same number to each side of an equation produces an equivalent equation.

Algebra If x - a = b, then x - a + a = b + a, or x = b + a.

Subtraction Property of Equality

Words Subtracting the same number from each side of an equation produces an equivalent equation.

Algebra If x + a = b, then x + a - a = b - a, or x = b - a.

EXAMPLE 1 Solve an equation using subtraction

Solve x + 7 = 4.

2	x + 7 = 4	Write original equation.	
🚦 To obtain an equivalent	x + 7 - 7 = 4 - 7	Use subtraction property of equality: Subtract 7 from each side,	
equation, be sure to subtract the same	x = -3	Simplify.	
number from each side.	▶ The solution is -3.		
	CHECK Substitute -3 for .	x in the original equation.	
	x + 7 = 4	Write original equation.	
	$-3+7 \stackrel{?}{=} 4$	Substitute –3 for x.	

$4 = 4 \checkmark$ Simplify. Solution checks.

EXAMPLE 2 Solve an equation using addition

USE HORIZONTAL FORMAT In Example 2, both horizontal and vertical formats are used. In the rest of the book, equations will be solved using the horizontal format. Solve x - 12 = 3.

Horizontal format		Vertical format
x - 12 = 3	Write original equation.	x - 12 = 3
x - 12 + 12 = 3 + 12	Add 12 to each side.	+ 12 + 12
<i>x</i> = 15	Simplify.	x = 15

MULTIPLICATION AND DIVISION EQUATIONS Multiplication and division are inverse operations. So, the multiplication property of equality can be used to solve equations involving division, and the division property of equality can be used to solve equations involving multiplication.

KEY CONCEPT

For Your Notebook

Multiplication Property of Equality

Words Multiplying each side of an equation by the same nonzero number produces an equivalent equation.

Algebra If $\frac{x}{a} = b$ and $a \neq 0$, then $a \cdot \frac{x}{a} = a \cdot b$, or x = ab.

Division Property of Equality

Words Dividing each side of an equation by the same nonzero number produces an equivalent equation.

Algebra If ax = b and $a \neq 0$, then $\frac{ax}{a} = \frac{b}{a}$, or $x = \frac{b}{a}$.

EXAMPLE 3 Solve an equation using division

Solve -6x = 48.

-6x = 48 Write original equation.

 $\frac{-6x}{-6} = \frac{48}{-6}$ Divide each side by -6.

x = -8 Simplify.

GUIDED PRACTICE for Examples 1, 2, and 3

Solve the equation. Check your solution.

1. $y + 7 = 10$	2. $x - 5 = 3$	3. $q - 11 = -5$	4. $6 = t - 2$
5. $4x = 48$	6. $-65 = -5y$	7. $6w = -54$	8. $24 = -8n$

EXAMPLE 4Solve an equation using multiplicationSolve $\frac{x}{4} = 5$.Solution $\frac{x}{4} = 5$ Write original equation. $4 \cdot \frac{x}{4} = 4 \cdot 5$ Multiply each side by 4.x = 20Simplify.

GUIDED PRACTICE for Example 4

Solve the equation. Check your solution.

9. $\frac{t}{-3} = 9$ 10. $6 = \frac{c}{7}$ 11. $13 = \frac{z}{-2}$ 12. $\frac{a}{5} = -11$

USING RECIPROCALS Recall that the product of a number and its reciprocal is 1. You can isolate a variable with a fractional coefficient by multiplying each side of the equation by the reciprocal of the fraction.

EXAMPLE 5 Solve an equation by multiplying by a reciprocal Solve $-\frac{2}{7}x = 4$. Solution REVIEW RECIPROCALS The coefficient of x is $-\frac{2}{7}$. The reciprocal of $-\frac{2}{7}$ is $-\frac{7}{2}$. For help with finding reciprocals, see p. 915. $-\frac{2}{7}x = 4$ Write original equation. $-\frac{7}{2}\left(-\frac{2}{7}x\right) = -\frac{7}{2}(4)$ Multiply each side by the reciprocal, $-\frac{7}{2}$. x = -14 Simplify. The solution is -14. Check by substituting -14 for x in the original equation. CHECK $-\frac{2}{7}x = 4$ Write original equation. $-\frac{2}{7}(-14) \stackrel{?}{=} 4$ Substitute -14 for x. $4 = 4 \checkmark$ Simplify. Solution checks. **GUIDED PRACTICE** for Example 5 Solve the equation. Check your solution. 13. $\frac{5}{6}w = 10$ 14. $\frac{2}{3}p = 14$ 15. $9 = -\frac{3}{4}m$ 16. $-8 = -\frac{4}{5}v$

EXAMPLE 6 Write and solve an equation

OLYMPICS In the 2004 Olympics, Shawn Crawford won the 200 meter dash. His winning time was 19.79 seconds. Find his average speed to the nearest tenth of a meter per second.

Solution

Let r represent Crawford's speed in meters per second. Write a verbal model. Then write and solve an equation.





Crawford's average speed was about 10.1 meters per second.

GUIDED PRACTICE for Example 6

17. WHAT IF? In Example 6, suppose Shawn Crawford ran 100 meters at the same average speed he ran the 200 meters. How long would it take him to run 100 meters? Round your answer to the nearest tenth of a second.



	•				1		
EXAMPLES	15. * MULTIPLE CHO	CE What is the so	blution of $-8 = d$	- 13?			
1 and 2 on pp. 134–135	▲ -21	B -5	© 5	D 21			
for Exs. 15, 16	16. * MULTIPLE CHO	CE What is the so	olution of $22 + v^2$	= -65?			
		(B) −43	© 43	(D) 87			
	▲ -87	6 -43	•	-			
EXAMPLES	SOLVING MULTIPLICA	TION AND DIVISION	ON EQUATIONS S	olve the equation.			
3 and 4 on pp: 135-136	Check your solution.	18. –4 <i>q</i>	- 52	19. $48 = 8c$			
for Exs. 17-30	17. $5g = 20$			22. 187 = -1	7r		
	20. $-108 = 9j$	21. 15 =	= - <i>n</i>				
	23. $\frac{\gamma}{3} = 5$	24. $\frac{m}{2}$ =	= 14	25. $8 = \frac{x}{6}$			
2	26. $7 = \frac{t}{-7}$	27. –11	$z = \frac{z}{-2}$	28. $-3 = \frac{d}{14}$			
	In Exercises 29 and	30, refer to the m	ethod	Let $x = 0.\overline{63}$. Then	$100x = 63.\overline{63}.$		
	shown, which a stud	ent used to write	8				
	repeating decimal a	s a fraction.		Subtract: 100x =			
	29. Explain the stud	ent's method.			-0.636363		
	30. Write the repeat	ing decimal as a í	fraction.	99x =			
	a. 0.7	b. 0.18		x =	$\frac{63}{99} = \frac{7}{11}$		
	SOLVING EQUATION	Solve the equat	tion. Check your	solution.			
	31. $b - 0.4 = 3.1$	32. –3	3.2 + z = -7.4	33. -5.7 =	<i>w</i> - 4.6		
	34. $-6.1 = p + 2.2$	35. 8.2	2 = -4g	36. -3.3 <i>a</i> =	= 19.8		
	37. $\frac{3}{4} = \frac{1}{8} + v$	38. $\frac{n}{4.0}$	$\frac{1}{6} = -2.5$	39. -0.12 =			
EXAMPLE 5	40. $\frac{1}{2}m = 21$	• •	c = 32	42. $-7 = \frac{1}{5}$			
on p. 136 for Exs. 40-48	43. $\frac{3}{2}k = 18$	44. –	$21 = -\frac{3}{5}t$	45. $-\frac{2}{7}\nu =$			
	46. $\frac{8}{5}x = \frac{4}{15}$	47. $\frac{1}{3}$	$y=\frac{1}{5}$	48. $-\frac{4}{3} = \frac{4}{3}$	$\frac{2}{3}z$		
	GEOMETRY The rectangle or triangle has area A. Write and solve an equation to find the value of x.						
	49. $A = 54 \text{ in.}^2$	12 in.	50. A =	$= 72 \text{ cm}^2$	m		
	CHALLENGE Find	the value of h rei	ing the given info	ormation.			
	CHALLENGE Find 51. $4a = 6$ and b		52. a	-6.7 = 3.1 and $b =$	5a		
*							
138	O = WORKED-OUT S on p. WS1	DLUTIONS	★ = STANDAI TEST PR	RDIZED A AGTICE	= MULTIPLE REPRESENTATIONS		

3.2 Solve Two-Step Equations



You solved one-step equations. You will solve two-step equations. So you can find a scuba diver's depth, as in Example 4.

Key Vocabulary

•like terms, p. 97

- input, p. 35
- output, p. 35

by 2 and addition by 5. You typically solve such an equation by applying the inverse operations in the reverse order of the order of operations. This is shown in the table below.

The equation $\frac{x}{2} + 5 = 11$ involves two operations performed on x: division

Operations performed on x	Operations to isolate x
1. Divide by 2.	1. Subtract 5.
2. Add 5.	2. Multiply by 2.

EXAMPLE 1 Solve a	a two-step equation
Solve $\frac{x}{2} + 5 = 11$.	
$\frac{x}{2} + 5 = 11$	Write original equation.
$\frac{x}{2} + 5 - 5 = 11 - 5$	Subtract 5 from each side.
$\frac{x}{2}=6$	Simplify.
$2 \cdot \frac{x}{2} = 2 \cdot 6$	Multiply each side by 2.
<i>x</i> = 12	Simplify.
▶ The solution is 12. Che	ck by substituting 12 for x in the original equation.
CHECK $\frac{x}{2} + 5 = 11$	Write original equation.
$\frac{12}{2} + 5 \stackrel{?}{=} 11$	Substitute 12 for x.
11 = 11 🗸	Simplify. Solution checks.

GUIDED PRACTICE for Example 1

Solve the equation. Check your solution.

1. 5x + 9 = 24 **2.** 4y - 4 = 16 **3.** $-1 = \frac{z}{3} - 7$

EXAMPLE 2) Solve a two-step equation by combining like terms

REVIEW LIKE TERMS For help with combining like terms, see p. 97.	Solve $7x - 4x = 21$.			
	7x - 4x = 21	Write original equation.		
	3x = 21	Combine like terms.		
c	$\frac{3x}{3} = \frac{21}{3}$	Divide each side by 3.		
	<i>x</i> = 7	Simplify.		

EXAMPLE 3 Find an input of a function

The output of a function is 3 less than 5 times the input. Find the input when the output is 17.

Solution

STEP 7 Write an equation for the function. Let x be the input and y be the output.

y is 3 less than 5 times x.

STEP 2 Solve the equation for x when y = 17.

y = 5x - 3

y=5x-3	Write original function.
17 = 5x - 3	Substitute 17 for y.
17 + 3 = 5x - 3 + 3	Add 3 to each side.
20 = 5x	Simplify.
$\frac{20}{5} = \frac{5x}{5}$	Divide each side by 5.
4 = x	Simplify.

An input of 4 produces an output of 17.

CHECKy = 5x - 3Write original function. $17 \stackrel{?}{=} 5(4) - 3$ Substitute 17 for y and 4 for x. $17 \stackrel{?}{=} 20 - 3$ Multiply 5 and 4. $17 = 17 \checkmark$ Simplify. Solution checks.

🧹 Gu

GUIDED PRACTICE for Examples 2 and 3

Solve the equation. Check your solution.

4. 4w + 2w = 24 **5.** 8t - 3t = 35 **6.**

6. -16 = 5d - 9d

- 7. The output of a function is 5 more than -2 times the input. Find the input when the output is 11.
- 8. The output of a function is 4 less than 4 times the input. Find the input when the output is 3.

EXAMPLE 4 Solve a multi-step problem

SCUBA DIVING As a scuba diver descends into deeper water, the pressure of the water on the diver's body steadily increases.

The pressure at the surface of the water is 2117 pounds per square foot (lb/ft^2) . The pressure increases at a rate of 64 pounds per square foot for each foot the diver descends. Find the depth at which a diver experiences a pressure of 8517 pounds per square foot.



Solution

ANOTHER WAY

For an alternative method for solving

Example 4, turn to page 147 for the **Problem Solving** Workshop. **STEP 7** Write a verbal model. Then write an equation.

Pressure at given depth (lb/ft²)	=	Pressure at surface (lb/ft ²)	+	Rate of change of pressure (lb/ft ² per foot of depth)		Diver's depth (ft)
*		-		+		*
Р	=	2117	+	64	•	d

STEP 2 Find the depth at which the pressure is 8517 pounds per square foot.

 P = 2117 + 64d Write equation.

 8517 = 2117 + 64d Substitute 8517 for P.

 8517 - 2117 = 2117 - 2117 + 64d Subtract 2117 from each side.

 6400 = 64d Simplify.

 $\frac{6400}{64} = \frac{64d}{64}$ Divide each side by 64.

 100 = d Simplify.

A diver experiences a pressure of 8517 pounds per square foot at a depth of 100 feet.

CHECK	P = 2117 + 64d	Write original equation.
	8517 ² 2117 + 64(100)	Substitute 8517 for P and 100 for d.
	8517 差 2117 + 6400	Multiply 64 and 100.
	8517 = 8517 🗸	Simplify. Solution checks.

GUIDED PRACTICE for Example 4

- **9.** WHAT IF? In Example 4, suppose the diver experiences a pressure of 5317 pounds per square foot. Find the diver's depth.
- 10. JOBS Kim has a job where she makes \$8 per hour plus tips. Yesterday, Kim made \$53 dollars, \$13 of which was from tips. How many hours did she work?

3.2 EXERCISES

KEY

HOMEWORK O = WORKED-OUT SOLUTIONS on p. WS5 for Exs. 13, 19, and 39 * = STANDARDIZED TEST PRACTICE Exs. 2, 21, 40, 41, and 44 = MULTIPLE REPRESENTATIONS Ex. 43

SKILL PRACTICE

	1. VOCABULARY Copy and complete: To solve the equation $2x + 3x = 20$, you would begin by combining $2x$ and $3x$ because they are _?						
	2. ★ WRITING Describe the steps you would use to solv $4x + 7 = 15$.	e the equation					
EXAMPLE 1	SOLVING TWO-STEP EQUATIONS Solve the equation. Che	eck your solution.					
on p. 141	3. $3x + 7 = 19$ 4. $5h + 4 = 19$	5. $7d - 1 = 13$					
for Exs. 3–14	6. $2g - 13 = 3$ 7. $10 = 7 - m$	8. $11 = 12 - q$					
	9. $\frac{a}{3} + 4 = 6$ 10. $17 = \frac{w}{5} + 13$	11. $\frac{b}{2} - 9 = 11$					
	12. $-6 = \frac{z}{4} - 3$ 13. $7 = \frac{5}{6}c - 8$	14. $10 = \frac{2}{7}n + 4$					
EXAMPLE 2	COMBINING LIKE TERMS Solve the equation. Check you	r solution.					
on p. 142	15. $8y + 3y = 44$ 16. $2p + 7p = 54$	17. $11x - 9x = 18$					
for Exs. 15–23	18. $36 = 9x - 3x$ (19.) $-32 = -5k + 13k$	20. $6 = -7f + 4f$					
	21. ★ MULTIPLE CHOICE What is the first step you can take to solve the equation $6 + \frac{x}{3} = -2$?						
	Subtract 2 from each side. B Add 6 to each side.						
	 Divide each side by 3. Subtract 6 from each side. 						
	ERROR ANALYSIS Describe and correct the error in solving the equation.						
	22. $23.$ $-2x + x = 10$						
		$\frac{1}{2} = \frac{10}{-2}$					
	x = 3	$x^{2} - 2$ x = -5					
EXAMPLE 3 on p. 142	FINDING AN INPUT OF A FUNCTION Write an equation for the function described. Then find the input.						
for Exs. 24-26	24. The output of a function is 7 more than 3 times the input. Find the input when the output is -8 .						
	25. The output of a function is 4 more than 2 times the when the output is −10.						
	26. The output of a function is 9 less than 10 times the when the output is 11.	input. Find the input					

SOLVING EQUATIONS Solve the equation. Check your solution.

27. $5.6 = 1.1p + 1.2$	28. $7.2y + 4.7 = 62.3$	29. $1.2j - 4.3 = 1.7$
30. $16 - 2.4d = -8$	31. $14.4m - 5.1 = 2.1$	32. $-5.3 = 2.2v - 8.6$.
33. $\frac{c}{5.3} + 8.3 = 11.3$	34. $3.2 + \frac{x}{2.5} = 4.6$	35. $-1.2 = \frac{z}{4.6} - 2.7$

36. CHALLENGE Solve the equations 3x + 2 = 5, 3x + 2 = 8, and 3x + 2 = 11. Predict the solution of the equation 3x + 2 = 14. Explain.

PROBLEM SOLVING 37. DANCE CLASSES A dance academy charges \$24 per class **EXAMPLE 4** and a one-time registration fee of \$15. A student paid a on p. 143 total of \$687 to the academy. Find the number of classes for Exs. 37-40 the student took. Viome Rator for problem solving help at classzone.com **38.** CAR REPAIR Tyler paid \$124 to get his car repaired. The total cost for the repairs was the sum of the amount paid for parts and the amount paid for labor. Tyler was charged \$76 for parts and \$32 per hour for labor. Find the amount of time it took to repair his car. @HomeTator for problem solving help at classzone.com (39.) ADVERTISING A science museum wants to promote an upcoming exhibit by advertising on city buses for one month. The costs of the two types of advertisements being considered are shown. The museum has budgeted \$6000 for the advertisements. The museum decides to have 1 full bus wrap advertisement. How many half-side advertisements can the museum have? Half-side advertisement Full bus wrap advertisement \$800 for one month \$2000 for one month 40. * MULTIPLE CHOICE A skateboarding park charges \$7 per session to skate and \$4 per session to rent safety equipment. Jared rents safety equipment every time he skates. During one year, he spends \$99 for skating charges and equipment rentals. Which equation can be used to find x, the number of sessions lared attended? **(B)** 99 = 7x + 4x **(C)** 99 = 7x + 4(A) 99 = 7x**(D)** 99 = 4x + 7

41. ★ SHORT RESPONSE A guitar store offers a finance plan where you give a \$50 down payment on a guitar and pay the remaining balance in 6 equal monthly payments. You have \$50 and you can afford to pay up to \$90 per month for a guitar. Can you afford a guitar that costs \$542? Explain.

3.3 Solve Multi-Step Equations

isolate the variable.

C	Before	
C	Now	
C	Why?	

You solved one-step and two-step equations. You will solve multi-step equations.

So you can solve a problem about lifeguarding, as in Ex. 40.

Key Vocabulary

- like terms, p. 97
- distributive
- property, p. 96
- reciprocal, p. 915

EXAMPLE 1 Solve an equation by combining like terms

Solving a linear equation may take more than two steps. Start by simplifying

one or both sides of the equation, if possible. Then use inverse operations to

Solve $8x - 3x - 10 = 20$.	
8x - 3x - 10 = 20	Write original equation.
5x - 10 = 20	Combine like terms.
5x - 10 + 10 = 20 + 10	Add 10 to each side.
5x = 30	Simplify.
$\frac{5x}{5} = \frac{30}{5}$	Divide each side by 5.
x = 6	Simplify.

EXAMPLE 2 Solve an equation using the distributive property

Solve 7x + 2(x + 6) = 39.

METHOD 1 Show All Steps

7x + 2(x + 6) = 39

Solution

When solving an equation, you may feel comfortable doing some steps mentally. Method 2 shows a solution where some steps are done mentally.

REVIEW PROPERTIES For help with using the distributive property, see p. 96.

in · 2(n · 0) · 00
7x + 2x + 12 = 39
9x + 12 = 39
9x + 12 - 12 = 39 - 12
9x = 27
$\frac{9x}{9} = \frac{27}{9}$
x = 3

METHOD 2 Do Some Steps Mentally

7x + 2(x + 6)	=	39
7x + 2x + 12	=	39
9x + 12	=	39
9x	; =	27
ĸ	:=	3

EXAMPLE 3 Standardized Test Practice

Which equation represents Step 2 in the solution process?

ELIMINATE CHOICES You can eliminate choices B and C because -4 has not been distributed to both terms in the parentheses.

Solution

In Step 2, the distributive property is used to simplify the left side of the equation. Because -4(x-3) = -4x + 12, Step 2 should be 5x - 4x + 12 = 17.

▶ The correct answer is D. ④ ⑧ ⓒ ⑩

GIADED PRACTICE for Examples 1, 2, and 3

Solve the equation. Check your solution.

1. 9d - 2d + 4 = 32 **2.** 2w + 3(w + 4) = 27 **3.** 6x - 2(x - 5) = 46

USING RECIPROCALS Although you can use the distributive property to solve an equation such as $\frac{3}{2}(3x + 5) = -24$, it is easier to multiply each side of the equation by the reciprocal of the fraction.

EXAMPLE 4 Multiply by a reciprocal to solve an equation

Solve $\frac{3}{2}(3x + 5) = -24$. $\frac{3}{2}(3x + 5) = -24$ Write original equation. $\frac{2}{3} \cdot \frac{3}{2}(3x + 5) = \frac{2}{3}(-24)$ Multiply each side by $\frac{2}{3}$, the reciprocal of $\frac{3}{2}$. 3x + 5 = -16 Simplify. 3x = -21 Subtract 5 from each side. x = -7 Divide each side by 3.

GUIDED PRACTICE for Example 4

Solve the equation. Check your solution.

4.
$$\frac{3}{4}(z-6) = 12$$
 5. $\frac{2}{5}(3r+4) = 10$ **6.** $-\frac{4}{5}(4a-1) = 28$

EXAMPLE 5 Write and solve an equation

SUMMER CAMP You are planning a scavenger hunt for 21 campers. You plan to have 5 teams. One camper from each team will be the recorder and the rest will be searchers. How many searchers will each team have?

Solution

Let s be the number of searchers on each team. Then 1 + s is the total number of campers on each team.

Number of campers	-	Number of teams		Number of campers on each team	
21	=	5	•	(1 + s)	
:	21 = 5(1	+ s)	Write	equation.	
:	21 = 5 +	- 5s	Distr	ibutive property	
	16 = 5s		Subtr	ract 5 from each side.	
> 3	$s_{2} = s_{1}$		Divid	le each side by 5.	
b December 4	aaarah			Id require a total of 5(1 d	

REASONABLENESS The number of searchers must be a whole number.

CHECK

Because 4 searchers per team would require a total of 5(1 + 4) = 25 campers, 4 teams will have 3 searchers and 1 team will have 4 searchers.

GUIDED PRACTICE for Example 5

7. WHAT IF? In Example 5, suppose you decide to use only 4 teams. How many searchers should there be on each team?

3.3 EXERCISES



Skill Practice

- 1. VOCABULARY What is the reciprocal of the fraction in the equation $\frac{3}{5}(2x+8) = 18$?
- 2. **WRITING** Describe the steps you would use to solve the equation 3(4y 7) = 6.

EXAMPLE 1 on p. 148 for Exs. 3-11

COMBINING LIKE TERMS Solve the equation. Check your solution.

3.	p+2p-3=6	4.	12v + 14 + 10v = 80	5.	11w - 9 - 7w = 15
6.	5a + 3 - 3a = -7	7.	6c - 8 - 2c = -16	8.	9 = 7z - 13z - 21
9.	-2 = 3y - 18 - 5y	10.	23 = -4m + 2 + m	11.	35 = -5 + 2x - 7x



PROBLEM SOLVING



3.4 Solve Equations with **Variables on Both Sides**



You solved equations with variables on one side. You will solve equations with variables on both sides. So you can find the cost of a gym membership, as in Ex. 52.

Key Vocabulary identity

Some equations have variables on both sides. To solve such equations, you can collect the variable terms on one side of the equation and the constant terms on the other side of the equation.

Solve an equation with variables on both sides EXAMPLE 1

Solve 7 - 8x = 4x - 17.

ANOTHER WAY

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You could also begin solving the equation by subtracting 4x from each side to obtain 7 - 12x = -17. When you solve this equation for x, you get the same solution, 2.

7-8x=4x-17	Write original equation.
$rac{1}{2}$ 7 - 8x + 8x = 4x - 17 + 8x	Add 8x to each side.
7 = 12x - 17	Simplify each side.
24 = 12x	Add 17 to each side.
2 = x	Divide each side by 12.
The solution is 2. Check by sub	stituting 2 for x in the original equation.
CHECK $7 - 8x = 4x - 17$	Write original equation.
$7 - 8(2) \stackrel{?}{=} 4(2) - 17$	Substitute 2 for x.

$7 - 8(2) \stackrel{?}{=} 4(2) - 17$	Substitute 2 for x.
$-9 \stackrel{?}{=} 4(2) - 17$	Simplify left side.
$-9 = -9 \checkmark$	Simplify right side. Solution checks.

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Solve an equation with grouping symbols EXAMPLE 2

Solve $9x - 5 = \frac{1}{4}(16x + 60)$.				
$9x - 5 = \frac{1}{4}(16x + 60)$	Write original equation.			
9x-5=4x+15	Distributive property			
5x - 5 = 15	Subtract 4x from each side.			
$5x = 20^{\circ}$	Add 5 to each side.			
x = 4	Divide each side by 5.			

GUIDED PRACTICE for Examples 1 and 2

Solve the equation. Check your solution.

1. $24 - 3m = 5m$	2. $20 + c = 4c - 7$	3. $9 - 3k = 17 - 2k$
4. $5z - 2 = 2(3z - 4)$	5. $3 - 4a = 5(a - 3)$	6. $8y - 6 = \frac{2}{3}(6y + 15)$

EXAMPLE 3 Solve a real-world problem

CAR SALES A car dealership sold 78 new cars and 67 used cars this year. The number of new cars sold by the dealership has been increasing by 6 cars each year. The number of used cars sold by the dealership has been decreasing by 4 cars each year. If these trends continue, in how many years will the number of new cars sold be twice the number of used cars sold?

Solution

Let x represent the number of years from now. So, 6x represents the increase in the number of new cars sold over x years and -4x represents the decrease in the number of used cars sold over x years. Write a verbal model.

New cars sold this year	+	Increase in new cars sold over x years	= 2	Used cars sold this year	÷	Decrease in used cars sole over x years	d)
78	+	6 <i>x</i>	= 2(67	+	(-4 <i>x</i>))
		78 + 6x	x = 2(6)	(7 - 4x)	Write	equation.	
		78 + 6 <i>x</i>	r = 134	1-8x	Distril	butive property	r -
		78 + 143	x = 134	Ł	Add 8	x to each side.	
		14x = 56		4	Subtra	ct 78 from eac	h side.
		x = 4			Divide	e each side by 1	4.

The number of new cars sold will be twice the number of used cars sold in 4 years.

CHECK You can use a table to check your answer.

Year	0	1	2	3	4	The number of new
Used cars sold	67	63	59	55	51	cars sold is twice the number of used
New cars sold	78	84	90	96	102	cars sold in 4 years.

GUIDED PRACTICE, for Example 3

7. WHAT IF? In Example 3, suppose the car dealership sold 50 new cars this year instead of 78. In how many years will the number of new cars sold be twice the number of used cars sold?

NUMBER OF SOLUTIONS Equations do not always have one solution. An equation that is true for all values of the variable is an **identity**. So, the solution of an identity is all real numbers. Some equations have no solution.

EXAMPLE 4 Identify the number of solutions of an equation

Solve the equation, if possible.

a. 3x = 3(x + 4)

b.
$$2x + 10 = 2(x + 5)$$

Solution

a. 3x = 3(x + 4) Original equation

3x = 3x + 12 Distributive property

The equation 3x = 3x + 12 is not true because the number 3x cannot be equal to 12 more than itself. So, the equation has no solution. This can be demonstrated by continuing to solve the equation.

3x - 3x = 3x + 12 - 3x Subtract 3x from each side. $0 = 12 \times$ Simplify.

▶ The statement 0 = 12 is not true, so the equation has no solution.

b. 2x + 10 = 2(x + 5) Original equation

2x + 10 = 2x + 10 Distributive property

Notice that the statement 2x + 10 = 2x + 10 is true for all values of x. So, the equation is an identity, and the solution is all real numbers.



GUIDED PRACTICE for Example 4

Solve the equation, if possible.

8. 9z + 12 = 9(z + 3) **9.** 7w + 1 = 8w + 1 **10.** 3(2a + 2) = 2(3a + 3)

SOLVING LINEAR EQUATIONS You have learned several ways to transform an equation to an equivalent equation. These methods are combined in the steps listed below.

CONCEPT SUMMARYFor Your NotebookSteps for Solving Linear EquationsSTEP 1Use the distributive property to remove any grouping symbols.STEP 2Simplify the expression on each side of the equation.STEP 3Use properties of equality to collect the variable terms on one
side of the equation and the constant terms on the other side of
the equation.STEP 4Use properties of equality to solve for the variable.STEP 5Check your solution in the original equation.

3.4 EXERCISES





PROBLEM SOLVING

EXAMPLE 3 on p. 155 for Exs. 49–51 49. CAMPING The membership fee for joining a camping association is \$45. A local campground charges members of the camping association \$35 per night for a campsite and nonmembers \$40 per night for a campsite. After how many nights of camping is the total cost for members, including the membership fee, the same as the total cost for nonmembers?

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50. HIGH-SPEED INTERNET Dan and Sydney are getting high-speed Internet access at the same time. Dan's provider charges \$60 for installation and \$42.95 per month. Sydney's provider has free installation and charges \$57.95 per month. After how many months will Dan and Sydney have paid the same amount for high-speed Internet service?

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(51) LANGUAGES Information about students who take Spanish and students who take French at a high school is shown in the table. If the trends continue, in how many years will there be 3 times as many students taking Spanish as French?

Language	Students enrolled this year	Average rate of change	
Spanish	555	33 more students each year	
French	230	2 fewer students each year	

158

= WORKED-OUT SOLUTIONS on p. WS1 STANDARDIZED TEST PRACTICE



1.1 Evaluate Expressions



You used whole numbers, fractions, and decimals. You will evaluate algebraic expressions and use exponents. So you can calculate sports statistics, as in Ex. 50.

Key Vocabulary

- variable
- algebraic expression
- power
- base

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exponent

A **variable** is a letter used to represent one or more numbers. The numbers are the values of the variable. *Expressions* consist of numbers, variables, and operations. An **algebraic expression**, or *variable expression*, is an expression that includes at least one variable.

Algebraic expression		Meaning	Operation	
5(n)	, 5 • n	5 <i>n</i>	5 times n	Multiplication
$\frac{14}{y}$	14 ÷ y		14 divided by y	Division
6 + c			6 plus c	Addition
8 - x	9		8 minus x	Subtraction

To **evaluate an algebraic expression**, substitute a number for each variable, perform the operation(s), and simplify the result, if necessary.

EXAMPLE 1 Evaluate algebraic expressions

Evaluate the expression when n = 3.

USE A PROPERTY
Part (a) of Example 1
illustrates the transitive
property of equality: If
a = b and $b = c$, then
a = c. Because
13 • n = 13 • 3 and
13 · 3 = 39, 13 · n =
39. Two other properties
of equality are the
reflexive property
(a = a) and the
symmetric property
(if $a = b$, then $b \neq a$).

a. $13 \cdot n = 13 \cdot 3$	Substitute 3 for n.
= 39	Multiply.
b. $\frac{9}{n} = \frac{9}{3}$	Substitute 3 for n.
= 3	Divide.
c. $n-1 = 3-1$	Substitute 3 for n.
= 2	Subtract.
d. <i>n</i> + 8 = 3 + 8	Substitute 3 for n.
= 11	Add.



Chapter 1 Expressions, Equations, and Functions

EXAMPLE 2 Evaluate an expression

MOVIES The total cost of seeing a movie at a theater can be represented by the expression a + r where a is the cost (in dollars) of admission and r is the cost (in dollars) of refreshments. Suppose you pay \$7.50 for admission and \$7.25 for refreshments. Find the total cost.

Solution

Total cost = a + rWrite expression.= 7.50 + 7.25Substitute 7.50 for a and 7.25 for r.= 14.75Add.

The total cost is \$14.75.

EXPRESSIONS USING EXPONENTS A **power** is an expression that represents repeated multiplication of the same factor. For example, 81 is a power of 3 because $81 = 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3$. A power can be written in a form using two numbers, a **base** and an **exponent**. The exponent represents the number of times the base is used as a factor, so 81 can be written as 3^4 .

base exponent

$$3^4 = 3 \cdot 3 \cdot 3 \cdot 3$$

power 4 factors of 3

EXAMPLE 3 Read and write powers

Write the power in words and as a product.

	Power	Words	Product
Or a number raised to	a. 7 ¹	seven to the first power	7
he first power, you Isually do not write he exponent 1. For	b. 5 ²	five to the second power, or five <i>squared</i>	5•5
nstance, you write 7 ¹ simply as 7.	c. $\left(\frac{1}{2}\right)^3$	one half to the third power, or one half <i>cubed</i>	$\frac{1}{2}\cdot\frac{1}{2}\cdot\frac{1}{2}$
	d. z ⁵	z to the fifth power	Z * Z * Z * Z * Z * Z

GUIDED PRACTICE for Examples 2 and 3

5. WHAT IF? In Example 2, suppose you go back to the theater with a friend to see an afternoon movie. You pay for both admissions. Your total cost (in dollars) can be represented by the expression 2*a*. If each admission costs \$4.75, what is your total cost?

7. 2⁸

Write the power in words and as a product.

6. 9⁵

8. n^4

Evaluate powers EXAMPLE 4

Evaluate the expression.

USE A PROPERTY

Example 4 illustrates the substitution property of equality: If a = b, then a can be substituted for b in any expression or equation. Because $x = 2, x^4 = 2^4.$

b. n^3 when n = 1.5**a.** x^4 when x = 2Solution h. $n^3 = 1.5^3$ a. $x^4 = 2^4$ = (1.5)(1.5)(1.5) $= 2 \cdot 2 \cdot 2 \cdot 2$ = 3.375= 16 **GUIDED PRACTICE** for Example 4 Evaluate the expression. **10.** k^2 when k = 2.5 **11.** d^4 when $d = \frac{1}{3}$ **9.** x^3 when x = 8

REVIEW AREA

For help with area and volume, see pp. 922 and 925.

AND VOLUME AREA AND VOLUME Exponents are used in the formulas for the area of a square and the volume of a cube. In fact, the words squared and cubed come from the formula for the area of a square and the formula for the volume of a cube.



Evaluate a power EXAMPLE 5

STORAGE CUBES Each edge of the medium-sized pop-up storage cube shown is 14 inches long. The storage cube is made so that it can be folded flat when not in use. Find the volume of the storage cube.

Solution

 $V = s^3$ Write formula for volume.

 $= 14^3$ Substitute 14 for s.

= 2744**Evaluate power.**

The volume of the storage cube is 2744 cubic inches.



GUIDED PRACTICE for Example 5

12. WHAT IF? In Example 5, suppose the storage cube is folded flat to form a square. Find the area of the square.



SKILL PRACTICE

	1. VOCABULARY Identify the exponent and the base in the expression 6^{12} .					
	2. ★ WRITING n^5 when $n =$	<i>Describe</i> the steps 3 3. Then evaluate th	you would take to evalu ne expression.	ate the expression		
EXAMPLE 1	1 EVALUATING EXPRESSIONS Evaluate the expression.					
on p. 2 for Exs. 3–15	3. $15x$ when $x =$	4 4.0.	4r when $r = 6$	5. $w - 8$ when $w = 20$		
	6. $1.6 - g$ when	g = 1.2 7. 5	+ m when $m = 7$	8. $0.8 + h$ when $h = 3.7$		
	9. $\frac{24}{f}$ when $f = 8$			11. 2.5 <i>m</i> when $m = 4$		
	12. $\frac{1}{2}k$ when $k = \frac{1}{2}k$	$\frac{2}{3}$ 13. y	$-\frac{1}{2}$ when $y = \frac{5}{6}$	14. $h + \frac{1}{3}$ when $h = 1\frac{1}{3}$		
	15. ★ MULTIPLE	CHOICE What is the	e value of 2.5 <i>m</i> when <i>m</i>	= 10?		
	(A) 0.25	B 2.5	© 12.5	25		
EXAMPLE 3 on p. 3	WRITING POWERS	Write the power	in words and as a produ	ict.		
for Exs. 16–25	16. 12 ⁵	17. 7 ³	18. $(3.2)^2$	(19.) (0.3) ⁴		
	20. $\left(\frac{1}{2}\right)^8$	21. <i>n</i> ⁷	22. <i>y</i> ⁶	23. t^4		
	ERROR ANALYSIS	Describe and corre	ect the error in evaluati	ng the power.		
	$(0.4)^2 = 2(0.4)^2 =$			4 • 4 • 4 • 4 = 1024		
EXAMPLE 4	EVALUATING POW	ERS Evaluate the p		Charlen		
on p. 4 for Exs. 26–37	26. 3 ²	27. 10 ²	28. 1 ⁵	29. 11 ³		
	30. 5 ³	31. 3 ⁵	32. 2 ⁶	33. 6 ⁴		
	34. $\left(\frac{1}{4}\right)^2$	35. $\left(\frac{3}{5}\right)^3$	36. $\left(\frac{2}{3}\right)^4$	37. $\left(\frac{1}{6}\right)^3$		
	EVALUATING EXPR	ESSIONS Evaluate	the expression.			
	38. x^2 when $x = \frac{3}{4}$		39. p^2 when $p =$	= 1.1		
<u>e</u> .	40. $x + y$ when $x =$	11 and $y = 6.4$	41. kn when k	= 9 and n = 4.5		
	42. $w = z$ when $w = z$	= 9.5 and $z = 2.8$	43. $\frac{b}{c}$ when $b =$	24 and c = 2.5		
	44. ★ MULTIPLE C <i>x</i> = 10 and <i>y</i> =	HOICE Which expre 0.5?	ession has the greatest v	value when		
Ì	(A) xy	(B) <i>x</i> − <i>y</i>	$\textcircled{C} \frac{x}{y}$	(b) $\frac{y}{x}$		

45. * MULTIPLE CHOICE Let b be the number of tokens you bought at an arcade, and let u be the number you have used. Which expression represents the number of tokens remaining?

(A) b+u(B) b - u \bigcirc bu $\mathbf{D} = \frac{b}{v}$

- 46. COMPARING POWERS Let x and y be whole numbers greater than 0 with y > x. Which has the greater value, 3^x or 3^y ? Explain.
- 47. CHALLENGE For which whole number value(s) of x greater than 0 is the value of x^2 greater than the value of 2^x ? Explain.

PROBLEM SOLVING

EXAMPLE 2 on p. 3 for Exs. 48-50

48.
 GEOMETRY The perimeter of a square with a side length of s is given by the expression 4s. What is the perimeter of the square shown?

7.5 m

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49. LEOPARD FROG You can estimate the distance (in centimeters) that a leopard frog can jump using the expression 13ℓ where ℓ is the frog's length (in centimeters). What distance can a leopard frog that is 12.5 centimeters long jump?

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- 50. MULTI-STEP PROBLEM Jen was the leading scorer on her soccer team. She scored 120 goals and had 20 assists in her high school career.
 - **a.** The number n of points awarded for goals is given by 2g where g is the number of goals scored. How many points did Jen earn for goals?
 - **b.** The point total is given by n + a where a is the number of assists. Use your answer from part (a) to find Jen's point total.

EXAMPLE 5 on p. 4 for Exs. 51-52 51.) MULTI-STEP PROBLEM You are buying a tank for three fish. You have a flame angel that is 3.5 inches long, a yellow sailfin tang that is 5.5 inches long, and a coral beauty that is 3 inches long. The area (in square inches) of water surface the fish need is given by the expression 12f where f is the sum of the lengths (in inches) of all the fish in the tank.

- a. What is the total length of the three fish?
- b. How many square inches of water surface do the fish need?

52. **★ MULTIPLE CHOICE** For a snow sculpture contest, snow is packed into a cube-shaped box with an edge length of 8 feet. The box is frozen and removed, leaving a cube of snow. One cubic foot of the snow weighs about 30 pounds. You can estimate the weight (in pounds) of the cube using the expression 30V where V is the volume (in cubic feet) of the snow. About how much does the uncarved cube weigh?

- A 240 pounds
- **©** 15,360 pounds

B 1920 pounds

D 216,000 pounds

= WORKED-OUT SOLUTIONS 🛸 on p. WS1

★ = STANDARDIZED **TEST PRACTICE**

1.2 Apply Order of Operations



You evaluated algebraic expressions and used exponents. You will use the order of operations to evaluate expressions. So you can determine online music costs, as in Ex. 35.



Key Vocabulary order of operations

AND CONTRACTOR DOMANDO "I wanter "to share

Mathematicians have established an order of operations to evaluate an expression involving more than one operation.

KEY CO	NCEPT	For Your Notebook
Order o	f Operations	
STEP 1	Evaluate expressions inside	grouping symbols.
STEP 2	Evaluate powers.	
STEP 3	Multiply and divide from left	to right.
STEP 4	Add and subtract from left to	ə right.

EXAMPLE 1 **Evaluate expressions**

Evaluate	the expression $27 \div 3^2 \times 2 - 3$.		
STEP 1 There are no grouping symbols, so go to Step 2.			
STEP 2	Evaluate powers.		
	$27 \div 3^2 \times 2 - 3 = 27 \div 9 \times 2 - 3$	Evaluate power.	
STEP 3	Multiply and divide from left to right.		
	$27 \div 9 \times 2 - 3 = 3 \times 2 - 3$	Divide.	
	$3 \times 2 - 3 = 6 - 3$	Multiply.	
STEP 4	Add and subtract from left to right.		
	6 - 3 = 3	Şubtract.	
▶The va	lue of the expression $27 \div 3^2 \times 2 - 3$ is	3.	

GUIDED PRACTICE for Example 1

Evaluate the expression.

1. $20 - 4^2$

2. $2 \cdot 3^2 + 4$ **3.** $32 \div 2^3 + 6$ **4.** $15 + 6^2 - 4$

Chapter 1 Expressions, Equations, and Functions

GROUPING SYMBOLS Grouping symbols such as parentheses () and brackets [] indicate that operations inside the grouping symbols should be performed first. For example, to evaluate $2 \cdot 4 + 6$, you multiply first, then add. To evaluate 2(4 + 6), you add first, then multiply.

	EXAMPLE 2 Evaluate expr	essions with grouping symbols
	Evaluate the expression.	
	a. $7(13 - 8) = 7(5)$	Subtract within parentheses.
	= 35	Multiply.
	b. $24 - (3^2 + 1) = 24 - (9 + 1)$	Evaluate power.
	= 24 - 10	Add within parentheses.
	= 14	Subtract.
AVOID ERRORS When grouping	c. $2[30 - (8 + 13)] = 2[30 - 21]$	Add within parentheses.
symbols appear	= 2[9]	Subtract within brackets,
inside other grouping symbols, work from	= 18	Multiply.
the innermost grouping symbols outward.		

FRACTION BARS A fraction bar can act as a grouping symbol. Evaluate the numerator and denominator before you divide:

 $\frac{8+4}{5-2} = (8+4) \div (5-2) = 12 \div 3 = 4$

EXAMPLE 3 Evaluate an algebraic expression

Evaluate the expression when x = 4.

$\frac{9x}{3(x+2)} = \frac{9\cdot 4}{3(4+2)}$	Substitute 4 for x.
$=\frac{9\cdot 4}{3\cdot 6}$	Add within parentheses.
$=\frac{36}{18}$	Multiply.
= 2	Divide.
Algebra at class	zone.com

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GUIDED PRACTICE for Examples 2 and 3

Evaluate the expression.				
5. 4(3 + 9)	6. $3(8-2^2)$	7. 2[(9 + 3) ÷ 4]		
Evaluate the expression when $y = 8$.				
8. $y^2 - 3$	9. $12 - y - 1$	10. $\frac{10y+1}{y+1}$		

1.2 Apply Order of Operations

EXAMPLE 4 Standardized Test Practice

B \$123

A \$79

Solution

A group of 12 students volunteers to collect litter for one day. A sponsor provides 3 juice drinks and 2 sandwiches for each student and pays \$30 for trash bags. The sponsor's cost (in dollars) is given by the expression 12(3j + 2s) + 30 where *j* is the cost of a juice drink and *s* is the cost of a sandwich. A juice drink costs \$1.25. A sandwich costs \$2. What is the sponsor's cost?



ELIMINATE CHOICES

You can eliminate choices A and D by estimating. When *j* is about 1 and *s* is 2, the value of the expression is about 12(3 + 4) + 30, or \$114.

 $12(3j + 2s) + 30 = 12(3 \cdot 1.25 + 2 \cdot 2) + 30$ = 12(3.75 + 4) + 30 = 12(7.75) + 30 = 93 + 30 = 123 Substitute 1.25 for *J* and 2 for *s*. Multiply within parentheses. Add within parentheses. Multiply. Add.

The sponsor's cost is \$123. The correct answer is B. (A) (B) (C) (D).

(C) \$129

(D) \$210

Guided PRACTICE for Example 4

11. WHAT IF? In Example 4, suppose the number of volunteers doubles. Does the sponsor's cost double as well? *Explain*.

1.2 EXERCISES

 = WORKED-OUT SOLUTIONS on p. W51 for Exs. 16 and 35
 = STANDARDIZED TEST PRACTICE Exs. 2, 19, 31, 37, 39, and 40

SKILL PRACTICE

1. VOCABULARY According to the order of operations, which operation would you perform first in simplifying $50 - 5 \times 4^2 \div 2$?

EVALUATING EXPRESSIONS Evaluate the expression

2. **WRITING** Describe the steps you would use to evaluate the expression $2(3x + 1)^2$ when x = 3.

EXAMPLES 1 and 2

on pp. 8–9 for Exs. 3–21

by Algorithm LAF RESCONS' LValuate the expression.				
3. 13 - 8 + 3	4. $8 - 2^2$	5. 3 · 6 - 4	6. $5 \cdot 2^3 + 7$	
7. $48 \div 4^2 + \frac{3}{5}$	8. $1 + 5^2 \div 50$	9. $2^4 \cdot 4 - 2 \div 8$	10. $4^3 \div 8 + 8$	
11. (12 + 72) ÷ 4	12. 24 + 4 (3 + 1)	13. $12(6-3.5)^2 - 1.5$	14. 24 ÷ $(8 + 4^2)$	
15. $\frac{1}{2}(21+2^2)$	$16, \frac{1}{6}(6+18) - 2^2$	17. $\frac{3}{4}[13 - (2 + 3)]^2$	18. 8[20 - $(9 - 5)^2$]	

Chapter 1 Expressions, Equations, and Functions

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19. ★ MULTIPLE CHOICE What is the value of $3[20 - (7 - 5)^2]$? **A** 48 **B** 56 **(C)** 192 **D** 972 ERROR ANALYSIS Describe and correct the error in evaluating the expression. $(1 + 13) \div 7 + 7 = 14 \div 7 + 7$ = 14 + 14 \therefore = 1 = 1 = 11 = 11 = 11 = 11 = 11 = 11 20. The Martha 13" EVALUATING EXPRESSIONS Evaluate the expression. EXAMPLE 3 on p. 9 **22.** $An \sim 12$ when n = 7 **23.** $2 + 3x^2$ when x = 3 **24.** $6t^2 - 13$ when t = 2for Exs. 22-31 **25.** $11 + r^3 + 2r$ when r = 5 **26.** 5(w - 4) when w = 7 **27.** $3(m^2 - 2)$ when m = 1.5**28.** $\frac{9x+4}{3x+1}$ when x = 7 **29.** $\frac{k^2-1}{k+3}$ when k = 5 **30.** $\frac{b^3-21}{5b+9}$ when b = 331. **★ MULTIPLE CHOICE** What is the value of $\frac{x^2}{25} + 3x$ when x = 10? **A** 26 **B** 34 **C** 43 **D** 105 CHALLENGE Insert grouping symbols in the expression so that the value of the expression is 14. **32.** $9 + 39 + 22 \div 11 - 9 + 3$ **33.** $2 \times 2 + 3^2 - 4 + 3 \times 5$ **PROBLEM SOLVING** 34. SALES Your school's booster club sells school T-shirts. Half the **EXAMPLE 4** T-shirts come from one supplier at a cost of \$5.95 each, and half from on p. 10 another supplier at a cost of \$6.15 each. The average cost (in dollars) of for Exs. 34-37

a T-shirt is given by the expression $\frac{5.95 + 6.15}{2}$. Find the average cost.

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(35.) MULTI-STEP PROBLEM You join an online music service. The total cost (in dollars) of downloading 3 singles at \$.99 each and 2 albums at \$9.95 each is given by the expression 3 • 0.99 + 2 • 9.95.

a. Find the total cost.

b. You have \$25 to spend. How much will you have left?

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36. **PHYSIOLOGY** If you know how tall you were at the age of 2, you can estimate your adult height (in inches). Girls can use the expression 25 + 1.17h where h is the height (in inches) at the age of 2. Boys can use the expression 22.7 + 1.37h. Estimate the adult height of each person to the nearest inch.

a. A girl who was 34 inches tall at age 2

b. A boy who was 33 inches tall at age 2

1.3 Write Expressions



You evaluated expressions.

You will translate verbal phrases into expressions. So you can find a bicycling distance, as in Ex. 36.

Key Vocabulary

- verbal model
- rate
- unit rate

To translate verbal phrases into expressions, look for words that indicate mathematical operations.

KEY CONCEPT	For You	For Your Notebook	
Translating Verbal Phrases			
Operation	Verbal Phrase	Expression	
Addition: sum, plus, total, more than, increased by	The sum of 2 and a number x	2 + x	
	A number n plus 7	<i>n</i> + 7	
Subtraction: difference, less than, minus, decreased by	The difference of a number <i>n</i> and 6	n - 6	
	A number y minus 5	y – 5	
Multiplication: times, product, multiplied by, of	12 times a number y	12y	
	$\frac{1}{3}$ of a number x	$\frac{1}{3}x$	
Division: quotient, divided by, divided into	The quotient of a number k and 2	$\frac{k}{2}$	

Order is important when writing subtraction and division expressions. For instance, "the difference of a number n and 6" is written n - 6, not 6 - n,

and "the quotient of a number k and 2" is written $\frac{k}{2}$, not $\frac{2}{k}$.

EXAMPLE 1 Translate verbal phrases into expressions

Verbal Phrase	Expression
a. 4 less than the quantity 6 times a number n	6n-4
b. 3 times the sum of 7 and a number y	3(7 + y)
c. The difference of 22 and the square of a number m	$22 - m^2$

GUIDED PRACTICE for Example 1

1. Translate the phrase "the quotient when the quantity 10 plus a number x is divided by 2" into an expression.

AVOID ERRORS When you translate

verbal phrases, the words 'the quantity' tell you what to group. In part (a), you write 6n - 4, not (6 - 4)n.
EXAMPLE 2 Write an expression

CHOOSE A VARIABLE

- To write an expression for a real-world problem, choose a letter that reminds you of the
- quantity represented, such as *t* for length.

CUTTING A RIBBON A piece of ribbon *l* feet long is cut from a ribbon 8 feet long. Write an expression for the length (in feet) of the remaining piece.

Solution

Draw a diagram and use a specific case to help you write the expression.

Suppose the piece cut is 2 feet long.



Suppose the piece cut is *l* feet long.



-8 ft------ (8 - 1) ft ----- l ft -----

The remaining piece is (8-2) feet long.

The remaining piece is (8 - l) feet long.

The expression $8 - \ell$ represents the length (in feet) of the remaining piece.

VERBAL MODEL A verbal model describes a real-world situation using words as labels and using math symbols to relate the words. You can replace the words with numbers and variables to create a *mathematical model*, such as an expression, for the real-world situation.

EXAMPLE 3 Use a verbal model to write an expression

TIPS You work with 5 other people at an ice cream stand. All the workers put their tips into a jar and share the amount in the jar equally at the end of the day. Write an expression for each person's share (in dollars) of the tips.

Solution



AVOID ERRORS

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Read the statement of the problem carefully. The number of people

- sharing tips is 6.
- **STEP 2** Translate the verbal model into an algebraic expression. Let *a* represent the amount (in dollars) in the jar.



An expression that represents each person's share (in dollars) is $\frac{u}{c}$.

GUIDED PRACTICE | for Examples 2 and 3

- 2. WHAT IF? In Example 2, suppose that you cut the original ribbon into p pieces of equal length. Write an expression that represents the length (in feet) of each piece.
- 3. WHAT IF? In Example 3, suppose that each of the 6 workers contributes an equal amount for an after-work celebration. Write an expression that represents the total amount (in dollars) contributed.

RATES A rate is a fraction that compares two quantities measured in different units. If the denominator of the fraction is 1 unit, the rate is called a unit rate. EXAMPLE 4 Find a unit rate READING A car travels 120 miles in 2 hours. Find the unit rate in feet per second. ******* Per means 'for each' or 120 miles _ 120 miles . 5280 feet . 'for every' and can also $\frac{1 \text{ hour}}{60 \text{ minutes}} \cdot \frac{1 \text{ minute}}{60 \text{ seconds}} = \frac{.88 \text{ feet}}{1 \text{ second}}$ 2 hours 2 hours be represented using 1 mile 1 second the symbol /, as in mi/h. The unit rate is 88 feet per second. EXAMPLE 5 Solve a multi-step problem TRAINING For a training program, each day you run a given distance and then walk to cool down. One day you run 2 miles and then walk for 20 minutes at a rate of 0.1 mile per 100 seconds. What total distance do you cover? Solution STEP 7 Convert your walking rate to miles per minute. 60 seconds _ 0.1 mile 6 miles = 0.06 mile100 seconds l minute 100 minutes 1 minute STEP 2 Write a verbal model and then an expression. Let m be the number of minutes you walk. Distance Walking Time spent run + rate walking (miles) (miles/minute) (minutes) 2 + 0.06m USE UNIT ANALYSIS Use unit analysis to check that the expression 2 + 0.06mYou expect the answer is reasonable. to be a distance in miles. You can use unit miles + $\frac{\text{miles}}{\text{minutes}} \cdot \frac{\text{minutes}}{\text{minutes}} = \text{miles} + \text{miles} = \text{miles}$ analysis, also called timensional analysis, Because the units are miles, the expression is reasonable. :o check that the **STEP 3** Evaluate the expression when m = 20. Expression produces in answer in miles. 2 + 0.06(20) = 3.2You cover a total distance of 3.2 miles. GUIDED PRACTICE for Examples 4 and 5 4. WHAT IF? In Example 5, suppose tomorrow you run 3 miles and then

walk for 15 minutes at a rate of 0.1 mile per 90 seconds. What total distance will you cover?

1.3 EXERCISES

HOMEWORK

KEY

Skill Practice 1. VOCABULARY Copy and complete: A(n) _? is a fraction that compares two quantities measured in different units. 2. **★ WRITING** Explain how to write $\frac{20 \text{ miles}}{4 \text{ hours}}$ as a unit rate. TRANSLATING PHRASES Translate the verbal phrase into an expression. **EXAMPLE 1** on p. 15 3. 8 more than a number x4. The product of 6 and a number y for Exs. 3-14 5. $\frac{1}{2}$ of a number m 6. 50 divided by a number h7. The difference of 7 and a number n8. The sum of 15 and a number x9. The quotient of twice a number t and 12 10. 3 less than the square of a number p(11.) 7 less than twice a number k12. 5 more than 3 times a number w 13. **★ MULTIPLE CHOICE** Which expression represents the phrase "the product of 15 and the quantity 12 more than a number x"? (A) $15 + 12 \cdot x$ **B** (15 + 12)x**(C)** 15(x+12)(1) $15 \cdot 12 + x$ 14. **★ MULTIPLE CHOICE** Which expression represents the phrase "twice the quotient of 50 and the sum of a number y and 8"? (A) $\frac{2 \cdot 50}{y} + 8$ (B) $2\left(\frac{50 + y}{8}\right)$ (C) $2\left(\frac{50}{y + 8}\right)$ (D) $\frac{2}{50} + (y + 8)$ **EXAMPLES** WRITING EXPRESSIONS Write an expression for the situation. 2 and 3 15. Number of tokens needed for v video games if each game takes 4 tokens on p. 16 16. Number of pages of a 5 page article left to read if you've read p pages for Exs. 15-21 17. Each person's share if p people share 16 slices of pizza equally 18. Amount you spend if you buy a shirt for \$20 and jeans for j dollars 19. Number of days left in the week if d days have passed so far 20. Number of hours in *m* minutes (21.) Number of months in y years EXAMPLE 4 UNIT RATES Find the unit rate in feet per second. on p. 17 300 yards $23. \ \frac{240 \text{ yards}}{1 \text{ hour}}$ for Exs. 22-27 24. 180 miles 2 hours 22. 25. 171 miles 1 minute 3 hours ERROR ANALYSIS Describe and correct the error in the units. 26. $\frac{\$2}{foot} \cdot 24 \text{ feet} = \frac{\$48}{ft^2}$ 9 yards $\cdot \frac{3 \text{ fest}}{1 \text{ yard}} \cdot \frac{\$2}{\text{foot}} = \frac{\$54}{\text{ft}}$

Chapter 1 Expressions, Equations, and Functions

1.4 Write Equations and Inequalities



You translated verbal phrases into expressions. You will translate verbal sentences into equations or inequalities. So you can calculate team competition statistics, as in Ex. 41.

Key Vocabulary

- equation
- inequality
- open sentence
- solution of an equation
- solution of an inequality

An **equation** is a mathematical sentence formed by placing the symbol = between two expressions. An **inequality** is a mathematical sentence formed by placing one of the symbols \langle , \leq , \rangle , or \geq between two expressions.

An **open sentence** is an equation or an inequality that contains an algebraic expression.

	KEY CONCEPT		For Your Notebook	
	Symbol Meaning		Associated Words	
2	=	is equal to	the same as	
-	<	is less than	fewer than	
-	≤	is less than or equal to	at most, no more than	
	>	is greater than	more than	
P ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ?	≥	is greater than or equal to	at least, no less than	

COMBINING INEQUALITIES Sometimes two inequalities are combined. For example, the inequalities x > 4 and x < 9 can be combined to form the inequality 4 < x < 9, which is read "x is greater than 4 and less than 9."

EXAMPLE 1 Write equations and inequalities

Verbal Sentence	Equation or Inequality
a. The difference of twice a number k and 8 is 12.	2k - 8 = 12
b. The product of 6 and a number <i>n</i> is at least 24.	$6n \ge 24$
c. A number y is no less than 5 and no more than 13	$3. \qquad 5 \le y \le 13$
Algebra at classzone.com	

GUIDED PRACTICE for Example 1

1. Write an equation or an inequality: The quotient of a number p and 12 is at least 30.

SOLUTIONS When you substitute a number for the variable in an open sentence like x + 2 = 5 or 2y > 6, the resulting statement is either true or false. If the statement is true, the number is a **solution of the equation** or a **solution of the inequality**.

EXAMPLE 2 Check possible solutions

Check whether 3 is a solution of the equation or inequality.

Equation/Inequality	Substitute	Conclusion
a. $8 - 2x = 2$	8 - 2(3) ≟ 2	2 = 2 ✓ 3 is a solution.
b. $4x - 5 = 6$	4(3) - 5 ≟ 6	$7 = 6 \times$ 3 is <i>not</i> a solution.
c. $2z + 5 > 12$	$2(3) + 5 \stackrel{?}{>} 12$	11 > 12 × 3 is <i>not</i> a solution.
d. $5 + 3n \le 20$	$5+3(3)\stackrel{?}{\leq}20$	$14 \le 20 \checkmark$ 3 is a solution.

USING MENTAL MATH Some equations are simple enough to solve using mental math. Think of the equation as a question. Once you answer the question, check the solution.

EXAMPLE 3 Use mental math to solve an equation

Equation	Think	Solution	Check	
a. $x + 4 = 10$	What number plus 4 equals 10?	6	6 + 4 = 10 🗸	
b. $20 - y = 8$	20 minus what number equals 8?	12	$20 - 12 = 8 \checkmark$	
c. $6n = 42$	6 times what number equals 42?	7	6(7) = 42 🗸	
d. $\frac{a}{5} = 9$	What number divided by 5 equals 9?	45	$\frac{45}{5} = 9\checkmark$	

GUIDED PRACTICE for Examples 2 and 3

Check whether the given number is a solution of the equation or inequality.2. 9 - x = 4; 53. b + 5 < 15; 74. $2n + 3 \ge 21$; 9Solve the equation using mental math.5. m + 6 = 116. 5x = 407. $\frac{r}{4} = 10$

READING A question mark above a symbol indicates a question. For instance, $8 - 2(3) \stackrel{?}{=} 2$ means "Is 8 - 2(3) equal to 2?"

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EXAMPLE 4 Solve a multi-step problem

MOUNTAIN BIKING The last time you and 3 friends went to a mountain bike park, you had a coupon for \$10 off and paid \$17 for 4 tickets. What is the regular price of 4 tickets? If you pay the regular price this time and share it equally, how much does each person pay?

Solution







STEP 2 Use mental math to solve the equation p - 10 = 17. Think: 10 less than what number is 17? Because 27 - 10 = 17, the solution is 27.

The regular price for 4 tickets is \$27.

STEP 3 Find the cost per person: $\frac{\$27}{4 \text{ people}} = \6.75 per person Each person pays \$6.75.

EXAMPLE 5) Write and check a solution of an inequality

BASKETBALL A basketball player scored 351 points last year. If the player plays 18 games this year, will an average of 20 points per game be enough to beat last year's total?

Solution

STEP 1 Write a verbal model. Let p be the average number of points per game. Write an inequality.

Number of games	•	Points per game	>	Total points last year
₩.		+		*
18	•	р	>	351

STEP 2 Check that 20 is a solution of the inequality 18p > 351. Because 18(20) = 360 and 360 > 351, 20 is a solution.

An average of 20 points per game will be enough.

GUIDED PRACTICE for Examples 4 and 5

- 8. WHAT (F? In Example 4, suppose that the price of 4 tickets with a half-off coupon is \$15. What is each person's share if you pay full price?
- **9.** WHAT IF? In Example 5, suppose that the player plays 16 games. Would an average of 22 points per game be enough to beat last year's total?

games $\cdot \frac{\text{points}}{\text{games}} = \text{points},$ so the inequality is reasonable.

USE UNIT ANALYSIS Unit analysis shows that

1.4 EXERCISES

HOMEWORK

 = WORKED-OUT SOLUTIONS on p. WS1 for Exs. 7 and 41
 = STANDARDIZED TEST PRACTICE Exs. 2, 16, 37, 44, 45, and 46

SKILL PRACTICE

- 1. VOCABULARY Give an example of an open sentence.
- 2. * WRITING Describe the difference between an expression and an equation.

EXAMPLE 1 on p. 21 for Exs. 3–16

- **3.** The sum of 42 and a number *n* is equal to 51.
- 4. The difference of a number z and 11 is equal to 35.
- 5. The difference of 9 and the quotient of a number t and 6 is 5.

WRITING OPEN SENTENCES Write an equation or an inequality.

- 6. The sum of 12 and the quantity 8 times a number k is equal to 48.
- 7. The product of 9 and the quantity 5 more than a number t is less than 6.
- 8. The product of 4 and a number w is at most 51.
- 9. The sum of a number b and 3 is greater than 8 and less than 12.
- 10. The product of 8 and a number k is greater than 4 and no more than 16.
- 11. The difference of a number t and 7 is greater than 10 and less than 20.

STORE SALES Write an inequality for the price p (in dollars) described.



ERROR ANALYSIS Describe and correct the error in writing the verbal sentence as an equation or an inequality.

14. The sum of a number n and 4 is no more than 13.15. The quotient of a number t and 4.2 is at most 15.



of the equation or inequality.



(C) 3b > 12

16. \star MULTIPLE CHOICE Which inequality corresponds to the sentence "The product of a number b and 3 is no less than 12"?

CHECK POSSIBLE SOLUTIONS Check whether the given number is a solution

(A) 3b < 12 (B) $3b \le 12$

(**D**) $3b \ge 12$

EXAMPLE 2 on p. 22 for Exs. 17–28

17. $x + 9 = 17; 8$	18. 9 + 4 y = 17; 1	19. $6f - 7 = 29; 5$
20. $\frac{k}{5} + 9 = 11; 10$	21. $\frac{r}{3} - 4 = 4$; 12	22. $\frac{x-5}{3} \ge 2.8; 11$
23. $15 - 4y > 6; 2$	24. $y = 3.5 < 6; 9$	25. $2 + 3x \le 8; 2$
26. 2 <i>p</i> − 1 ≥ 7; 3	27. $4z - 5 < 3; 2$	28. $3z + 7 > 20; 4$

2.1 Use Integers and **Rational Numbers**



You performed operations with whole numbers. You will graph and compare positive and negative numbers. So you can compare temperatures, as in Ex. 58.

Key Vocabulary

- whole numbers
- integers
- rational number
- opposites
- absolute value
- conditional statement

Whole numbers are the numbers 0, 1, 2, 3, ... and integers are the numbers \ldots , -3, -2, -1, 0, 1, 2, 3, \ldots (The dots indicate that the numbers continue without end in both directions.) Positive integers are integers that are greater than 0. Negative integers are integers that are less than 0. The integer 0 is neither negative nor positive.



Zero is neither negative nor positive.

EXAMPLE 1 Graph and compare integers

Graph -3 and -4 on a number line. Then tell which number is greater.



• On the number line, -3 is to the right of -4. So, -3 > -4.

RATIONAL NUMBERS The integers belong to the set of rational numbers. A rational number is a number $\frac{a}{b}$ where a and b are integers and $b \neq 0$. For Although you can write example, $-\frac{1}{2}$ is a rational number because it can be written as $\frac{-1}{2}$ or $\frac{1}{-2}$. The rational numbers belong to the set of numbers called the real numbers.



a negative fraction in different ways, you usually write it with the negative sign in front of the fraction.

GUIDED PRACTICE for Example 1

Graph the numbers on a number line. Then tell which number is greater.

1. 4 and 0

2. 2 and -5

3. -1 and -6

REVIEW FRACTIONS For help with writing fractions as decimals, see p. 916.

DECIMALS In decimal form, a rational number either terminates or repeats. For example, $\frac{3}{4} = 0.75$ is a *terminating decimal*, and $\frac{1}{3} = 0.333...$ is a repeating decimal.

EXAMPLE 2 Classify numbers

Tell whether each of the following numbers is a whole number, an integer, or a rational number: 5, 0.6, $-2\frac{2}{3}$, and -24.

Number	Whole number?	Integer?	Rational number?
5	Yes	Yes	Yes
•••> 0.6	No	No	Yes
$-2\frac{2}{3}$	No	No	Yes
24	No	Yes	Yes
	5 0.6 $-2\frac{2}{3}$	$5 Yes \\ \hline 0.6 No \\ \hline -2\frac{2}{3} No \\ \hline 0.6 No \\ $	5Yes 5 Yes 100 No 100 No 100 No 100 No 100 No

EXAMPLE 3 Order rational numbers

ASTRONOMY A star's color index is a measure of the temperature of the star. The greater the color index, the cooler the star. Order the stars in the table from hottest to coolest.

Star	Rigel	Arneb	Denebola	Shaula
Color index	-0.03	0.21	0.09 .	-0.22

Solution

Begin by graphing the numbers on a number line.



Read the numbers from left to right: -0.22, -0.03, 0.09, 0.21.

From hottest to coolest, the stars are Shaula, Rigel, Denebola, and Arneb.

GUIDED PRACTICE for Examples 2 and 3

Tell whether each number in the list is a whole number, an integer, or a rational number. Then order the numbers from least to greatest.

4. 3, -1.2, -2, 0

6. 3.6, -1.5, -0.31, -2.8

5. 4.5,
$$-\frac{3}{4}$$
, -2.1, 0.5
7. $\frac{1}{6}$, 1.75, $-\frac{2}{3}$, 0

OPPOSITES Two numbers that are the same distance from 0 on a number line but are on opposite sides of 0 are called **opposites**. For example, 4 and -4 are opposites because they are both 4 units from 0 but are on opposite sides of 0. The opposite of 0 is 0. You read the expression -a as "the opposite of a."



a. If a = -2.5, then -a = -(-2.5) = 2.5. **b.** If $a = \frac{3}{4}$, then $-a = -\frac{3}{4}$.

READING

The absolute value of a number is also

called its magnitude.

ABSOLUTE VALUE The **absolute value** of a number a is the distance between a and 0 on a number line. The symbol |a| represents the absolute value of a.

EV.	KEY CONCEPT	For Your Notebook		
WH	Absolute Value of a Number			
1111	Words If <i>a</i> is positive, then $ a = a$.	Example $ 2 = 2$		
ŧ	Words If a is 0, then $ a = 0$.	Example $ 0 = 0$		
	Words If a is negative, then $ a = -a$.	Example $ -2 = -(-2) = 2$		

EXAMPLE 5	Find	absolute	values	of numbers
			<i>,</i> ,	

AVOID ERRORS The absolute value of a number is never negative. If a number a is negative, then its absolute value, -a, is positive.

a. If $a = -\frac{2}{3}$, then $|a| = \left|-\frac{2}{3}\right| = -\left(-\frac{2}{3}\right) = \frac{2}{3}$. **b.** If a = 3.2, then |a| = |3.2| = 3.2.

CONDITIONAL STATEMENTS A **conditional statement** has a hypothesis and a conclusion. An **if-then statement** is a form of a conditional statement. The *if* part contains the hypothesis. The *then* part contains the conclusion.

conditional statement



In mathematics, if-then statements are either true or false. An if-then statement is true if the conclusion is always true when the hypothesis is satisfied. An if-then statement is false if for just one example, called a **counterexample**, the conclusion is false when the hypothesis is satisfied.

EXAMPLE 6 Analyze a conditional statement

Identify the hypothesis and the conclusion of the statement "If a number is a rational number, then the number is an integer." Tell whether the statement is true or false. If it is false, give a counterexample,

Solution

Hypothesis: a number is a rational number

Conclusion: the number is an integer

The statement is false. The number 0.5 is a counterexample, because 0.5 is a rational number but not an integer.



for Examples 4, 5, and 6

For the given value of a, find -a and |a|.

8. a = 5.3

9. $a \approx -7$

10. $a = -\frac{4}{9}$

= WORKED-OUT SOLUTIONS

on p. WS3 for Exs. 7, 29, and 53 = STANDARDIZED TEST PRACTICE Exs. 3, 4, 39, 50, 56, and 59

Identify the hypothesis and the conclusion of the statement. Tell whether the statement is true or false. If it is false, give a counterexample.

11. If a number is a rational number, then the number is positive.

HOMEWORK

12. If the absolute value of a number is positive, then the number is positive.

KEY

2.1 EXERCISES

SKILL PRACTICE

1. VOCABULARY Copy and complete: A number is a(n) ? if it can be written in the form $\frac{a}{b}$ where a and b are integers and $b \neq 0$.

- 2. VOCABULARY What is the opposite of -2?
- 3. *** WRITING** Describe the difference between whole numbers and positive integers.
- 4. * WRITING For a negative number x, is the absolute value of x a positive number or a negative number? Explain.

EXAMPLE 1 on p. 64 for Exs. 5-13 GRAPHING AND COMPARING INTEGERS Graph the numbers on a number line. Then tell which number is greater. 5 David 2

L	5. 0 and 7	6. $0 \text{ and } -4$	(7.) -5 and -6
	8. –2 and –3	9. 5 and -2	1012 and 8
l	111 and -5	12. 3 and -13	13. -20 and -2

EXAMPLES 2 and 3 on p. 65	CLASSIFYING AND ORDERING NUMBERS Tell whether each number in the list is a whole number, an integer, or a rational number. Then order the numbers from least to greatest.					
for Exs. 14-22	14. 3, -5, -2.4, l	15. 1.6, 1, -4	, 0	16. 0.25, -0.5, 0.2, -2		
	17. $-\frac{2}{3}$, -0.6, -1, $\frac{1}{3}$	1 8. -0.01, 0.1	, 0, – <u>1</u>	19. 16, -1.66, $\frac{5}{3}$, -1.6		
	20. $-2.7, \frac{1}{2}, 0.3, -7$	21. -4.99, 5,	<u>16</u> , −5.1	22. $-\frac{3}{5}$, -0.4, -1, -0.5		
EXAMPLES 4 and 5	FINDING OPPOSITES $A -a$ and $ a $.	IND ABSOLUTE VALUE	For the given y	alue of <i>a</i> , find		
on p. 66 for Exs. 23-34	23. $a = 6$	24. <i>a</i> = -3	25. $a = -18$	26. $a = 0$		
. 101 EKS. 25 54	27. <i>a</i> = 13.4	28. <i>a</i> = 2.7	29. $a = -6.1$	30. <i>a</i> = -7.9		
	31. $a = -1\frac{1}{9}$	32. $a = -\frac{5}{6}$	33. $a = \frac{3}{4}$	34. $a = 1\frac{1}{3}$		
EXAMPLE 6 on p. 67 for Exs. 35–38	conclusion of the com or <i>false</i> . If it is false, g	MAL STATEMENTS Ide ditional statement. To give a counterexample	ell whether the s	tatement is <i>true</i>		
		ositive integer, then th				
		gative, then its absolut		/e.		
	_	sitive, then its opposite				
	38. If a number is an	r is an integer, then the number is a rational number.				
	39. ★ MULTIPLE CHO	E CHOICE Which number is a whole number?				
	$\textcircled{A} \left -\frac{18}{9} \right $	B $-\frac{4}{3}$	© 1.6	D -(-7.963)		
	ERROR ANALYSIS Describe and correct the error in the statement.					
	40. The numbers —(— 8 , and —0. negative number	3 are	0.2	bers $ -3.4 , -(-8),$, and 0.87 tive numbers.		
	EVALUATING EXPRES	SIONS Evaluate the ex	pression when a	x = -0.75.		
	42. - <i>x</i>	43. $ x + 0.25$	44. $ x = 0.75$	5 45. $1 + -x $		
	46. 2 • (- <i>x</i>)	47. (- <i>x</i>) • 3	48. $ x + x $	49. $-x + x $		
		DICE Which number is				
	▲ -2.3	(₿) -0.3	© 1.3	(b) 2.3		
		at can you conclude at <i>in</i> your reasoning.	out the opposite	of the opposite of		
	52. CHALLENGE For than a? equal to	what values of <i>a</i> is the <i>a</i> ?	opposite of a gro	eater than a? less		
68	on pWS1	TIONS 🛧 =	STANDARDIZED TEST PRACTICE			



Key Vocabulary

additive identity

additive inverse

One way to add two real numbers is to use a number line. Start at the first number. Use the sign of the second number to decide whether to move left or right. Then use the absolute value of the second number to decide how many units to move. The number where you stop is the sum of the two numbers.





KEY CONCEPT For Your Notebook **Rules of Addition** WWWWWWWWWWWWW Words To add two numbers with the same sign, add their absolute values. The sum has the same sign as the numbers added. **Examples** 8 + 7 = 15-6 + (-10) = -16Words To add two numbers with different signs, subtract the lesser absolute value from the greater absolute value. The sum has the same sign as the number with the greater absolute value. **Examples** -12 + 7 = -518 + (-4) = 14

EXAMPLE 2 **Add real numbers**

Find the sum.

a. -5.3 + (-4.9) = -(|-5.3| + |-4.9|)= -(5.3 + 4.9)= -10.2 **b.** 19.3 + (-12.2) = |19.3| - |-12.2|= 19.3 - 12.2 **≃** 7.1

Rule of same signs Take absolute values. Add. Rule of different signs Take absolute values. Subtract.

PROPERTIES OF ADDITION Notice that both 3 + (-2) and -2 + 3 have the same sum, 1. So, 3 + (-2) = -2 + 3. This is an example of the commutative property of addition. The properties of addition are listed below.

KEY CONCEPT	For Your Notebook
Properties of Addition	
COMMUTATIVE PROPERTY The loss not change the sum.	e order in which you add two numbers
l gebra <i>a</i> + <i>b</i> ≈ <i>b</i> + <i>a</i>	Example $3 + (-2) = -2 + 3$
SSOCIATIVE PROPERTY The work of the system	vay you group three numbers in a sum
igebra $(a + b) + c = a + (b + b)$	c) Example $(-3 + 2) + 1 = -3 + (2 + 1)$
ENTITY PROPERTY The sum	of a number and 0 is the number.
gebra $a + 0 = 0 + a = a$	Example $-5 + 0 = -5$
VERSE PROPERTY The sum of	f a number and its opposite is 0.
gebra $a + (-a) = -a + a = 0$	Example $-6 + 6 = 0$

The identity property states that the sum of a number a and 0 is a. The number 0 is the **additive identity**. The inverse property states that the sum of a number a and its opposite is 0. The opposite of a is its **additive inverse**.

EXAMPLE 3 Identify properties of addition

Statement

Property illustrated

- **a.** (x + 9) + 2 = x + (9 + 2) **b.** 8.3 + (-8.3) = 0**c.** -y + 0.7 = 0.7 + (-y)
- Associative property of addition Inverse property of addition Commutative property of addition

EXAMPLE 4 Solve a multi-step problem

BUSINESS The table shows the annual profits of two piano manufacturers. Which manufacturer had the greater total profit for the three years?

Year	Profit (millions) for manufacturer A	Profit (millions) for manufacturer B
1	-\$5.8	-\$6.5
2	\$8.7	\$7.9
3	\$6.8	\$8.2



Solution

STEP 1 Calculate the total profit for each manufacturer.

: CHECK	Manufacturer A:	Manufacturer B:
REASONABLENESS	Total profit = $-5.8 + 8.7 + 6.8$	Total profit = $-6.5 + 7.9 + 8.2$
Use estimation to check reasonableness.	= -5.8 + (8.7 + 6.8)	= -6.5 + (7.9 + 8.2)
Manufacturer A: about	= -5.8 + 15.5	= -6.5 + 16.1
6 + 9 + 7, or 10. Manufacturer B: about	= 9.7	= 9.6
-7 + 8 + 8, or 9. Because 10 > 9, the	STEP 2 Compare the total profits: 9.7 > 9.	6.
because to > s, the		C*+

solution is reasonable. **Manufacturer A had the greater total profit**.

1	GUIDED PRACTICE	for Examples 2, 3, and 4		
	Find the sum.			
	5. -0.6 + (-6.7)	6. 10.1 + (-16.2)	7. -13.1 + 8.7	
	Identify the prope	rty being illustrated.		
	8. $7 + (-7) = 0$	9. $-12 + 0 = -12$	10. $4 + 8 = 8 + 4$	

11. WHAT IF? In Example 4, suppose that the profits for year 4 are -\$1.7 million for manufacturer A and -\$2.1 million for manufacturer B. Which manufacturer has the greater total profit for the four years?

2.2 EXERCISES

HOMEWORK KEY

= WORKED-OUT SOLUTIONS on p. WS3 for Exs. 13, 35, and 55 ***** = STANDARDIZED TEST PRACTICE Exs. 2, 50, 56, 57, and 58

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SKILL PRACTICE

	1. VOCABULARY What number is called the additive identity?		
	 * WRITING Without a numbers will be zero? 	ctually adding, how can	you tell if the sum of two
EXAMPLE 1	USING A NUMBER LINE Use a number line to find the sum.		
on p. 74 for Exs. 3–11	3. -11 + 3	41 + 6	5. 13 + (-7)
•••••••	6. 5 + (-10)	7. $-9 + (-4)$	8. -8 + (-2)
	914 + 8	10. $6 + (-12)$	11. -11 + (-9)
EXAMPLE 2	FINDING SUMS Find the su	m.	
on p. 75 for Exs. 12–25	12. -2.4 + 3.9	(13) -8.7 + 4.2	14. 4.3 + (-10.2)
101 103. 12 23	15. 9.1 + (-2.5)	16. $-6.5 + (-7.1)$	17. -11.4 + (-3.8)
	18. $4\frac{1}{5} + (-9\frac{1}{2})$	19. $8\frac{2}{3} + \left(-1\frac{3}{5}\right)$	20. $-12\frac{3}{4} + 6\frac{9}{10}$
	21. $-\frac{4}{9} + 1\frac{4}{5}$	22. $-3\frac{3}{7} + \left(-14\frac{3}{4}\right)$	23. $-7\frac{1}{12} + \left(-13\frac{7}{8}\right)$
	ERROR ANALYSIS Describe	and correct the error in	finding the sum.
< 2	24. −13 + (−15) = 28 ≥	25.	17 + (-31) = -48 X
; EXAMPLE 3	IDENTIFYING PROPERTIES	Identify the property bei	ng illustrated.
on p. 76 for Exs. 26-31	26. $-3 + 3 = 0$		6 + 1) + 7 = -6 + (1 + 7)
: 101 EAS. 20-51	28. 9 + (-1) = -1 + 9	29. -8	+0 = -8
	30. $(x+2) + 3 = x + (2+3)$) 31. y +	(-4) = -4 + y
EXAMPLE 4	FINDING SUMS Find the sur	m.	
on p. 76 for Exs. 32–37	32. $-13 + 5 + (-7)$	33. –1	8 + (-12) + (-19)
101 EASI 32 51	34. 0.47 + (-1.8) + (-3.8)	352	.6 + (-3.4) + 7.6
	36. $-3\frac{1}{2} + \left(-7\frac{2}{5}\right) + \left(-9\frac{3}{10}\right)$		$+\left(-6\frac{3}{5}\right)+3\frac{1}{4}$
	EVALUATING EXPRESSIONS	Evaluate the expression	for the given value of x .
	38. $3 + x + (-7); x = 6$		(-5) + 5; x = -3
	40. 9.6 + (-x) + 2.3; $x = -8$.7 + (-5.4) + (-x); x = 2.4

42. $1\frac{1}{4} + |x| + (-3\frac{1}{2}); x = -8\frac{2}{5}$

43. $|x| + (-3\frac{1}{4}) + (7\frac{3}{10}); x = -3\frac{1}{3}$

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KEY CONCEPT	For Your Notebook
Subtraction RuleWords To subtract b from a, add the oppoAlgebra $a - b = a + (-b)$ Example 14	
Words To subtract b from a, add the oppo	osite of b to a.
Algebra $a - b = a + (-b)$ Example 14	4 - 8 = 14 + (-8)
1	
EXAMPLE 1 Subtract real number	'S
Find the difference.	'S
and an a second s	*S b. 18 − (−7) = 18 + 7

/	GUIDED PRACTICE	for Example 1	
	Find the difference	е.	
	12 - 7	2. 11.7 – (–5)	3. $\frac{1}{3} - \frac{1}{2}$

Example 2Evaluate a variable expressionEvaluate a variable expressionEvaluate a variable expressionEvaluate a variable expressiony - x + 6.8 = 7.2 - (-2) + 6.8Substitute -2 for x and 7.2 for y.= 7.2 + 2 + 6.8Add the opposite of -2.= 16

EVALUATING CHANGE You can use subtraction to find the change in a quantity, such as elevation or temperature. The change in a quantity is the difference of the new amount and the original amount. If the new amount is greater than the original amount, the change is positive. If the new amount is less than the original amount, the change is negative.

EXAMPLE 3 Evaluate change

TEMPERATURES One of the most extreme temperature changes in United States history occurred in Fairfield, Montana, on December 24, 1924. At noon, the temperature was 63°F. By midnight, the temperature fell to -21°F. What was the change in temperature?

Solution

The change C in temperature is the difference of the temperature m at midnight and the temperature n at noon.

STEP1 Write a verbal model. Then write an equation.

Change in temperature	=	Temperature at midnight	_	Temperature at noon
4		+		*
С	=	m	-	n

STEP 2 Find the change in temperature.

C = m - n	Write equation.
= -21 - 63	Substitute values.
= -21 + (-63)	Add the opposite of 63.
= -84	Add -21 and -63.

▶ The change in temperature was -84°F.

USING A CALCULATOR To enter a negative number on a calculator, use the **(C)** key. To enter a subtraction sign, use the **(C)** key. You can use a calculator to check your answer in Example 3 using the following keystrokes.



(-) 21 - 63 ENTER

GUIDED PRACTICE for Examples 2 and 3

Evaluate the expression when x = -3 and y = 5.2.

4. x - y + 8 **5.** y - (x - 2)

6. (y - 4) - x

7. CAR VALUES A new car is valued at \$15,000. One year later, the car is valued at \$12,300. What is the change in the value of the car?

AVOID ERRORS

When a quantity decreases, the change is negative. So, the change found in Example 3 should be a negative number.

2.3 EXERCISES

HOMEWORK

on p. WS4 for Exs. 3, 21, and 43 *** = STANDARDIZED TEST PRACTICE** Exs. 2, 38, 39, 40, and 46 *** = MULTIPLE REPRESENTATIONS** Ex. 45

= WORKED-OUT SOLUTIONS

SKILL PRACTICE

- 1. VOCABULARY Use the subtraction rule to rewrite the expression -3 6 as an addition expression.
- 2. * WRITING Without actually subtracting, how can you tell whether a change in a quantity will be negative?

FINDING DIFFERENCES Find the difference. **EXAMPLE 1** on p. 80 **4.** 16 = 32 **5.** -11 = (-3)(3.)13 - (-5)6. -15 - 29 for Exs. 3-14 **7.** -35.9 - (-50) **8.** 14.7 - (-2.3) **9.** -3.6 - 22.2 **10.** -18.2 - (-15.4)**11.** $\frac{1}{2} - \frac{5}{6}$ **12.** $-\frac{5}{3} - \frac{8}{3}$ **13.** $\frac{1}{2} - \left(-\frac{1}{4}\right)$ **14.** $-\frac{7}{10} - \left(-\frac{2}{5}\right)$ EXAMPLE 2 ERROR ANALYSIS Describe and correct the error in evaluating the on p. 80 expression when x = 3 and y = -8. for Exs. 15-25 15. 16. x - y + 2 = 3 - 8 + 2x - (-4 + y) = 3 - [-4 + (-8)]= 3 + (-8) + 2= 3 - (-12)= -5 + 2= 3 - 12 = -3= -9 **EVALUATING EXPRESSIONS** Evaluate the expression when x = 7.1 and y = -2.5. 1 - 3 10 10 ---

17. $x = (-y)$	18. $y - x - 12$	19. $x - (-6) + y$
20. $x = (y = 13)$	21. $-y - (1.9 - x)$	22. $-y - x$
23. $x - y - 2$	24. $5.3 - (y - x)$	25. $x + y - 2.8$

EVALUATING CHANGE Find the change in temperature or elevation.

on p. 81 for Exs. 26–31

EXAMPLE 3

EVALUATING EXPRESSIONS Evaluate the expression when x = 3.6, y = 6.6, and z = -11.

32. $(x - y) - z $	33. $(x - -y) - z$	34. $x - y - z $
35. $(-x - y) - z - 5$	36. $x + y - z + 12.9$	37. $-z + y - x - (-2.4)$

27. From -45°F to 62°F

29. From 1200 meters to -80 meters

31. From -90.7 miles to 36.4 miles

38. \star **MULTIPLE CHOICE** If the value of the expression a - b is negative, which statement must be true?

(A) a > b (B) a = 0 (C) a < b (D) b = 0

Chapter 2 Properties of Real Numbers

26. From -5°C to -13°C

30. From 4.8°F to -12.6°F

28. From -300 feet to -100 feet





You added and subtracted real numbers. You will multiply real numbers. So you can calculate an elevation, as in Example 4.



For Your Notebook

Key Vocabulary multiplicative

identity

In the activity on page 87, you saw that $a \cdot (-1) = -a$ for any integer a. This rule not only lets you write the product of a and -1 as -a, but it also lets you write -a as (-1)a and a(-1). Using this rule, you can multiply any two real numbers. Here are two examples:



KEY CONCEPT

The Sign of a Product

Words The product of two real numbers with the same sign is positive.

Examples 3(4) = 12

Words The product of two real numbers with *different* signs is negative.

Examples 2(-5) = -10

-7(2) = -14

-6(-3) = 18

EXAMPLE 1 Multiply real numbers

Find the product.

	· · · · · · · · · · · · · · · · · · ·	<u>ـ</u>
MULTIPLY NEGATIVES	a. $-3(6) = -18$	Different signs: product is negative.
A product is negative	b. $2(-5)(-4) = (-10)(-4)$	Multiply 2 and -5.
if it has an <i>odd</i> number of negative	= 40	Same signs; product is positive.
 numbers. A product is positive if it has an even number 	c. $-\frac{1}{2}(-4)(-3) = 2(-3)$	Multiply $-\frac{1}{2}$ and -4 .
of negative numbers.	= -6	Different signs; product is negative.



PROPERTIES OF MULTIPLICATION Notice that both 4(-5) and -5(4) have a product of -20, so 4(-5) = -5(4). This equation is an example of the commutative property of multiplication. Properties of multiplication are listed below.



The identity property states that the product of a number a and 1 is a. The number 1 is called the multiplicative identity.

EXAMPLE 2 Identify properties of multiplication

Statement **a.** $(x \cdot 7) \cdot 0.5 = x \cdot (7 \cdot 0.5)$

b. $8 \cdot 0 = 0$

- **c.** $-6 \cdot \gamma = \gamma \cdot (-6)$
- **d.** $9 \cdot (-1) = -9$
- e. $1 \cdot v = v$

Property illustrated

Associative property of multiplication Multiplicative property of zero Commutative property of multiplication Multiplicative property of -1 Identity property of multiplication

GUIDED PRACTICE for Example 2

Identify the property illustrated.

- 4. $-1 \cdot 8 = -8$
- 6. $(y \cdot 4) \cdot 9 = y \cdot (4 \cdot 9)$
- **8.** $-5 \cdot (-6) = -6 \cdot (-5)$

5. $12 \cdot x = x \cdot 12$ 7. $0 \cdot (-41) = 0$ **9.** $-13 \cdot (-1) = 13$

2.4 Multiply Real Numbers

EXAMPLE 3 Use properties of multiplication

JUSTIFY STEPS

To justify a step, you name the property used. Sometimes a step is a calculation, as when you multiply 0.25 and -4 in Example 3.

Find the product $(-4x) \cdot 0.25$.	Justify your steps.
$(-4x) \cdot 0.25 = 0.25 \cdot (-4x)$	Commutative prop

J) • 0.25 -	$-0.23 \cdot (-4\lambda)$
=	$= [0.25 \cdot (-4)]x$
=	$= -1 \cdot x$
=	= - <i>x</i>

Commutative property of multiplication Associative property of multiplication Product of 0.25 and -4 is -1. Multiplicative property of --1

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EXAMPLE 4 Solve a multi-step problem

READING The average rate of change in elevation is the total change in elevation divided by the number of years that have passed.

was about 6416 feet. From 1900 to 1950, the average rate of change in elevation was about -0.12 foot per year. From 1950 to 2000, the average rate of change was about -0.526 foot per year. Approximate the elevation in 2000.

LAKES In 1900 the elevation of Mono Lake in California

Solution

STEP 1 Write a verbal model.

New		O
elevation	#	ele
(feet)		

riginal Average rate evation of change +(feet) (feet/year)



STEP 2 Calculate the elevation in 1950. Use the elevation in 1900 as the original elevation. The time span is 1950 - 1900 = 50 years.

New elevation = $6416 + (-0.12)(50)$	Substitute values.
= 6416 + (-6)	Multiply ~0.12 and 50.

= 6410Add 6416 and -6.

\$7EP 3 Calculate the elevation in 2000. Use the elevation in 1950 as the original elevation. The time span is 2000 - 1950 = 50 years.

> New elevation = 6410 + (-0.526)(50)Substitute values.

ply —0

= 6383.7

0.526 and 50. Add 6410 and -26.3.

The elevation in 2000 was about 6383.7 feet above sea level.

~	the second se	for Examples 3 and 4
1		

Find the product. Justify your steps.

10. $\frac{3}{10}(5y)$

11. 0.8(-x)(-1)

12. (-y)(-0.5)(-6)

13. Using the data in Example 4, approximate the elevation of Mono Lake in 1925 and in 1965.

In Step 2, note that

CHECK

 $-0.12(50) \approx -0.1(50) =$ -5, and 6416 + (-5) = 6411, so 6410 is reasonable. In Step 3, $-0.526(50) \approx -0.5(50)$ = -25, and 6410 + (--25) = 6385, so 6383.7 is reasonable.

REASONABLENESS





SKILL PRACTICE

		the second s	and the second	
	I. VOCABULARY W	hat number is called th	ne multiplicative id	lentity?
		<i>scribe</i> the difference beand the multiplicative pr		property of
EXAMPLE 1	FINDING PRODUCTS	Find the product.		
on p. 88 for Exs. 3–18	34(7)	4. 11(-2)	59(-10)	6. -8(-11)
•	7. 5(-7.2)	8. (-2.5)(-1.3)	9. $-42\left(-\frac{1}{6}\right)$	10. $-\frac{1}{2}(-32)$
	111.9(3.3)(7)	12. 0.5(-20)(-3)	13. $-\frac{5}{6}(-12)(-4)$) 14. $-\frac{3}{4}(2)(-6)$
	15. -8(-4)(-2.5)	16. -1.6(-2)(-10)	17. $18\left(-\frac{2}{3}\right)\left(-\frac{1}{5}\right)$	18. $-\frac{3}{4}\left(-\frac{1}{3}\right)\left(-\frac{8}{9}\right)$
EXAMPLE 2	IDENTIFYING PROPE	RTIES Identify the proj	perty illustrated.	
on p. 89 for Exs. 19–27	19. $-\frac{2}{5} \cdot 0 = 0$	20. 0.3 • (-3)	$= -3 \cdot 0.3$	21. $-143 \cdot 1 = -143$
	22. $-1 \cdot (-6) = 6$	23. (-2 • 5) •	$4 = -2 \cdot (5 \cdot 4)$	24. $0 \cdot (-76.3) = 0$
	25. $1 \cdot (ab) = ab$	26. $(3x)y = 3$	(<i>xy</i>) 2	27. $s \cdot (-1) = -s$
EXAMPLE 3	USING PROPERTIES	Find the product. Just	fy your steps.	
on p. 90 for Exs. 28–36	28. y(-2)(-8)	29. -18(- <i>x</i>)	~	30. $\frac{3}{5}(-5q)$
	31. $-2(-6)(-7z)$	325(-4)(-	-2.1)(-z)	33. $-\frac{1}{5}(-10)(4)(-5c)$
	34. -5 <i>t</i> (- <i>t</i>)	35. -6 <i>r</i> (-2.8	ir) :	36. $\frac{1}{3} \left(-\frac{9}{10} \right) (-m) (-m)$
	EVALUATING EXPREMENTED and y = 3.6.	SSIONS Evaluate the ex	pression when x =	= -2
	37. $2x + y$	38. $-x - 3y$		39. <i>xy</i> - 5.4
	40. $ y - 4x$	41. $1.5x -]$	-y	42. $x^2 - y^2$
	ERROR ANALYSIS D	escribe and correct the	error in finding t	he product.
	431(7)(-3)(-	-2x) = 7(-3)(-2x)	44. (~5z)(~8	$)(z) = (-\partial)(-bz)(z)$
		= -21(-2x)		$= (-\delta)(-5)(z)(z)$
		$= [-21 \cdot (-2)] \times$	\sim	$= -40(z \cdot z)$ $= -40z^2$
		= 42x		$= -40z^2$

2.5 Apply the Distributive Property

Before Now Why? You used properties to add and multiply real numbers. You will apply the distributive property. So you can find calories burned, as in Example 5.

Key Vocabulary

- equivalent expressions
- distributive property
- term
- coefficient
- constant term

AVOID ERRORS

Be sure to distribute the factor outside of the

parentheses, not just to the first number.

parentheses to all of the numbers inside the

like terms

The models below show two methods for finding the area of a rectangle that has a length of (x + 2) units and a width of 3 units.





The expressions 3(x + 2) and 3(x) + 3(2) are equivalent because they represent the same area. Two expressions that have the same value for all values of the variable are called **equivalent expressions**. The equation 3(x + 2) = 3(x) + 3(2) illustrates the **distributive property**, which can be used to find the product of a number and a sum or difference.

KEY CONCEPT		For Your Notebook
The Distributive Property		
Let <i>a</i> , <i>b</i> , and <i>c</i> be real number	s.	
Words	Algebra	Examples
The product of a and $(b + c)$:	a(b+c) = ab + ac $(b+c)a = ba + ca$	3(4 + 2) = 3(4) + 3(2) (3 + 5)2 = 3(2) + 5(2)
The product of a and $(b - c)$:	a(b-c) = ab - ac $(b-c)a = ba - ca$	5(6-4) = 5(6) - 5(4) $(8-6)4 = 8(4) - 6(4)$

EXAMPLE 1 Apply the distributive property

Use the distributive property to write an equivalent expression.

a. 4(y+3) = 4y + 12 **b.** $(y+7)y = y^2 + 7y$ **c.** $n(n-9) = n^2 - 9n$ **d.** (2-n)8 = 16 - 8n

EXAMPLE 2 Distribute a negative number

Use the distributive property to write an equivalent expression.

a. -2(x + 7) = -2(x) + (-2)(7)Distribute -2.= -2x - 14Simplify.b. (5 - y)(-3y) = 5(-3y) - y(-3y)Distribute -3y. $= -15y + 3y^2$ Simplify.c. -(2x - 11) = (-1)(2x - 11)Multiplicative property of -1= (-1)(2x) - (-1)(11)Distribute -1.= -2x + 11Simplify.

TERMS AND COEFFICIENTS The parts of an expression that are added together are called **terms**. The number part of a term with a variable part is called the **coefficient** of the term.

READING

Note that -x has a coefficient of -1 even though the 1 isn't written. Similarly, x has a coefficient of 1.



A **constant term** has a number part but no variable part, such as 8 in the expression above. **Like terms** are terms that have the same variable parts, such as -x and 2x in the expression above. Constant terms are also like terms.

EXAMPLE 3 Identify parts of an expression

Identify the terms, like terms, coefficients, and constant terms of the expression 3x - 4 - 6x + 2.

Solution

Write the expression as a sum: 3x + (-4) + (-6x) + 2

Terms: 3x, -4, -6x, 2 **Coefficients:** 3, -6

Like terms: 3x and -6x; -4 and 2 Constant terms: -4, 2

GUIDED PRACTICE for Examples 1, 2, and 3

Use the distributive property to write an equivalent expression.

1. 2(x+3) 2. $-(4-\gamma)$

3. (m-5)(-3m) **4.** $(2n+6)\left(\frac{1}{2}\right)$

5. Identify the terms, like terms, coefficients, and constant terms of the expression -7y + 8 - 6y - 13.

COMBINING LIKE TERMS The distributive property allows you to combine like terms that have variable parts. For example, 5x + 6x = (5 + 6)x = 11x. A quick way to combine like terms with variable parts is to mentally add the coefficients and use the common variable part. An expression is *simplified* if it has no grouping symbols and if all of the like terms have been combined. EXAMPLE 4

Standardized Test Practice

(C) 5n+3

(D) n+3

ANOTHER WAY

In Example 4, you can rewrite the expression 4(n + 9) - 3(2 + n) as 4(n + 9) + (-3)(2 + n)and then distribute -3to the terms in 2 + n.

Simplify the expression 4(n + 9) - 3(2 + n).

(A) 5n + 30 (B) $n \div 30$

4(n + 9) - 3(2 + n) = 4n + 36 - 6 - 3n Distributive property = n + 30 Combine like terms.

The correct answer is B. (A) (B) (C) (D)

EXAMPLE 5 Solve a multi-step problem

EXERCISING Your daily workout plan involves a total of 50 minutes of running and swimming. You burn 15 calories per minute when running and 9 calories per minute when swimming. Let *r* be the number of minutes that you run. Find the number of calories you burn in your 50 minute workout if you run for 20 minutes.



ANOTHER WAY

For an alternative method for solving the problem in Example 5, turn to page 102 for the **Problem Solving** Workshop.

Solution

The workout lasts 50 minutes, and your running time is r minutes. So, your swimming time is (50 - r) minutes.

STEP 1 Write a verbal model. Then write an equation.

Amount burned (calories)	5	Burning when run (calories/m	ning		Running time (minutes)	+	Burning rate when swimming (calories/minute)		Swimming time (minutes)
С	Ħ	15		•	г	+	9	٠	(50 – <i>r</i>)
	<i>C</i> =	15r + 9(50)) – r)		Write eq	luat	ion.		L.
	=	15 <i>r</i> + 450	— 9r		Distribu	tive	property		
	=	6 <i>r</i> + 450			Combin	e lik	e terms.		
STEP 2	Finc	l the value	of C w	hei	$\mathbf{n} r \simeq 20.$,		
	C =	6 r + 450			ु Write ec	juat	ion.		
	=	6(20) + 4	50 = 57	7 Q	Substitu	te 2	0 for <i>r</i> . Then simpli	fy.	

> You burn 570 calories in your 50 minute workout if you run for 20 minutes.

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Guided PRACTICE for Examples 4 and 5

- 6. Simplify the expression 5(6 + n) 2(n 2).
- 7. WHAT IF? In Example 5, suppose your workout lasts 45 minutes. How many calories do you burn if you run for 20 minutes? 30 minutes?

2.5 EXERCISES



HOMEWORK

KEY

USING MENTAL MATH In Exercises 43–46, use the example below to find the total cost.



Use the distributive property and mental math to find the total cost of 5 picture frames at \$1.99 each.

Total cost = $5(1.99)$	Write expression for total cost.
= 5(2 - 0.01)	Rewrite 1.99 as 2 - 0.01.
= 5(2) - 5(0.01)	Distributive property
= 10 - 0.05	Multiply using mental math.
= 9.95	Subtract. The total cost is \$9.95.

43. 3 CDs at \$12.99 each

44. 5 magazines at \$3.99 each

9 points

10 points

45. 6 pairs of socks at \$1.98 per pair

46. 25 baseballs at \$2.98 each

TRANSLATING PHRASES In Exercises 47 and 48, translate the verbal phrase into an expression. Then simplify the expression.

- 47. Twice the sum of 6 and x, increased by 5 less than x
- 48. Three times the difference of x and 2, decreased by the sum of x and 10
- 49. CHALLENGE How can you use a(b + c) = ab + ac to show that (b + c)a = ba + ca is also true? Justify your steps.

PROBLEM SOLVING

EXAMPLE 5 on p. 98 for Exs. 50–52 **50. SPORTS** An archer shoots 6 arrows at a target. Some arrows hit the 9 point ring, and the rest hit the 10 point bull's-eye. Write an equation that gives the score *s* as a function of the number *a* of arrows that hit the 9 point ring. Then find the score if 2 arrows hit the 9 point ring.

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51. **MOVIES** You have a coupon for \$2 off the regular cost per movie rental. You rent 3 movies, and the regular cost of each rental is the same. Write an equation that gives the total cost C (in dollars) as a function of the regular cost r (in dollars) of a rental. Then find the total cost if a rental regularly costs \$3.99.

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52. ★ SHORT RESPONSE Each day you use your pay-as-you-go cell phone you pay \$.25 per minute for the first 10 minutes and \$.10 per minute for any time over 10 minutes. Write an equation that gives the daily cost C (in dollars) as a function of the time t (in minutes) when usage exceeds 10 minutes. Which costs more, using the phone for 10 minutes today and 15 minutes tomorrow, or using the phone for 25 minutes today? Explain.

= WORKED-OUT SOLUTIONS on p. WS1 TEST PRACTICE



SIGN OF A QUOTIENT Because division can be expressed as multiplication, the sign rules for division are the same as the sign rules for multiplication.

For Your Notebook

KEY CONCEPT

The Sign of a Quotient

- The quotient of two real numbers with the same sign is positive.
- The quotient of two real numbers with different signs is negative.
- The quotient of 0 and any nonzero real number is 0.

EXAMPLE 2 Divide real numbers

Find the quotient.

b.
$$-20 \div \left(-\frac{5}{3}\right) = -20 \cdot \left(-\frac{3}{5}\right) = -2$$

1

a.

GUIDED PRACTICE for Examples 1 and 2

Find the multiplicative inverse of the number. 1. -27 2. -8 3. $-\frac{4}{7}$ 4. $-\frac{1}{3}$

Find the quotient.

5. $-64 \div (-4)$ **6.** $-\frac{3}{8} \div \left(\frac{3}{10}\right)$ **7.** $18 \div \left(-\frac{2}{9}\right)$ **8.** $-\frac{2}{5} \div 18$

EXAMPLE 3

Find the mean

TEMPERATURES The table gives the daily minimum temperatures (in degrees Fahrenheit) in Barrow, Alaska, for the first 5 days of February 2004. Find the mean daily minimum temperature.

Day in February	1	2	3	4	5	
Minimum temperature (°F)	21	-29	-39	-39	-22	

To find the mean daily minimum temperature, find the sum of the

Solution

Point Barrow Observatory

CHECK REASONABLENESS The sum of the temperatures is about -20 + (-30) +(-40) + (-40) +(-20) = -150, and $-150 \div 5 = -30$, so the solution is reasonable.

minimum temperatures for the 5 days and then divide the sum by 5.
Mean =
$$\frac{-21 + (-29) + (-39) + (-39) + (-22)}{5}$$

= $-\frac{150}{5} = -30$

▶ The mean daily minimum temperature was -30°F.

104 Chapter 2 Properties of Real Numbers

AVOID ERRORS You cannot divide a real number by 0, because 0 does not have a multiplicative inverse. EXAMPLE 4 Simplify an expression



GUIDED PRACTICE for Examples 3 and 4

- 9. Find the mean of the numbers -3, 4, 2.8, and -1.5.
- 10. **TEMPERATURES** Find the mean daily maximum temperature (in degrees Fahrenheit) in Barrow, Alaska, for the first 5 days of February 2004.

Day in February	1	2	. 3	4	5
Maximum temperature (°F)	-3	-20	-21	-22	-18

Simplify the expression.

11. $\frac{2x-8}{-4}$ 12. $\frac{-6y+18}{3}$ 13. $\frac{-10z-20}{-5}$

OPERATIONS ON REAL NUMBERS In this chapter, you saw how to find the sum, difference, product, and quotient of two real numbers a and b. You can use the values of a and b to determine whether the result is positive, negative, or 0.

CONCEPT SUMMARY

For Your Notebook

Rules for Addition, Subtraction, Multiplication, and Division

Let a and b be real numbers.

Expression	a + b	a – b	a · b	a ÷ b
Positive if	the number with the greater absolute value is positive.	a > b.	a and b have the same sign $(a \neq 0, b \neq 0).$	a and b have the same sign $(a \neq 0, b \neq 0)$.
Negative if	the number with the greater absolute value is negative.	a < b.	a and b have different signs $(a \neq 0, b \neq 0)$.	a and b have different signs ($a \neq 0, b \neq 0$).
Zero if	a and b are additive inverses.	a = b.	a = 0 or b = 0.	$a = 0$ and $b \neq 0$.

2.6 EXERCISES

HOMEWORK KEY

= 3x - 2

100

Skill PRACTICE

	1. VOCABULARY Co its <u>?</u> is 1.	py and complete: The	product of a non2	zero number and		
	2. WRITING How can you tell whether the mean of <i>n</i> numbers is negative without actually dividing the sum of the numbers by <i>n</i> ? <i>Explain</i> .					
EXAMPLE 1	FINDING INVERSES F	ind the multiplicative	inverse of the nu			
on p. 103 for Exs. 3-10, 23	3. –18	49	51	6. $-\frac{1}{2}$		
, IOI EASI 5 10,	7. $-\frac{3}{4}$	8. $-\frac{5}{9}$	9. $-4\frac{1}{3}$	10. $-2\frac{2}{5}$		
EXAMPLE 2	FINDING QUOTIENTS	Find the quotient.		(2)		
on p. 104 for Exs. 11-22	11. -21 ÷ 3	12. -18 ÷ (-6)	13. $-1 \div \left(-\frac{7}{2}\right)$	$14. 15 \div \left(-\frac{3}{4}\right)$		
; IUI LA3: II 22	15. $13 \div \left(-4\frac{1}{3}\right)$	16. $-\frac{2}{3} \div 2$	17. $-\frac{1}{2} \div \frac{1}{5}$	18. $-\frac{1}{5} \div (-6)$		
	19. $-\frac{4}{7} \div (-2)$	20. $-1 \div \left(-\frac{6}{5}\right)$	21. $8 \div \left(-\frac{4}{11}\right)$	22. $-\frac{1}{3} \div \frac{5}{3}$		
	23. ★ MULTIPLE CHO	DICE If $-\frac{5}{7}x = 1$, what i	s the value of x?	10		
	(A) $-l\frac{2}{5}$	B $\frac{5}{7}$	© 1	D $\frac{12}{5}$		
: EXAMPLE 3	FINDING MEANS Find the mean of the numbers.					
on p. 104 for Exs. 24-32	24. -10, -8, 3	25. 12, -8, -		26. 18, -9, 0, -5		
	27. -2, 9, -3, 5	28. -1, -4, -	5, 10	29. 7, -4, 1, -9, -6		
	30. -5.3, -2, 1.3	31. 0.25, -4	, -0.75, -1, 6	32. -0.6, 0.18, -2, 5, -0.5		
EXAMPLE 4	SIMPLIFYING EXPRE	SSIONS Simplify the e	xpression.			
on p. 105 for Exs. 33-43	33. $\frac{6x-14}{2}$	34. $\frac{12y-8}{-4}$		$35. \frac{9z-6}{-3}$		
	36. $\frac{-6p+15}{6}$	37. $\frac{5-25q}{10}$		38. $\frac{-18-21r}{-12}$		
	39. $\frac{-24a-10}{-8}$	40. $\frac{-20b+7}{-5}$	<u>12</u>	41: $\frac{36-27c}{9}$		
	ERROR ANALYSIS <i>Describe</i> and correct the error in simplifying the expression.					
	42. $\frac{12 - 18x}{6} = (12 - 18)$	$-18x) \cdot \left(-\frac{1}{6}\right)$		$\frac{O}{2} = (-15x - 10) \cdot \left(-\frac{1}{5}\right)$		
	= 12(-	$-\frac{1}{6}$) $-18x\left(-\frac{1}{6}\right)$	\sim	$= -15x\left(-\frac{1}{5}\right) - 10\left(-\frac{1}{5}\right)$		

= -2 + 3x

EVALUATING EXPRESSIONS Evaluate the expression.

- 44. $\frac{2y-x}{x}$ when x = 1 and y = -445. $\frac{4x}{3y+x}$ when x = 6 and y = -846. $\frac{-9x}{y^2-1}$ when x = -3 and y = -247. $\frac{y-x}{xy}$ when x = -6 and y = -2
- **48. ★ WRITING** Tell whether division is commutative and associative. Give examples to support your answer.
- **49.** \star **MULTIPLE CHOICE** Let *a* and *b* be positive numbers, and let *c* and *d* be negative numbers. Which quotient has a value that is always negative?
- 50. CHALLENGE Find the mean of the integers from -410 to 400. Explain how you got your answer.
- 51. CHALLENGE What is the mean of a number and three times its opposite? *Explain* your reasoning.

PROBLEM SOLVING

example 2 on p. 104 for Ex. 52 52. **SPORTS** Free diving means diving without the aid of breathing equipment. Suppose that an athlete free dives to an elevation of -42 meters in 60 seconds. Find the average rate of change in the diver's elevation.

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EXAMPLE 3 on p. 104 for Exs. 53-54 53.

WEATHER The daily mean temperature is the mean of the high and low temperatures for a given day. The high temperature for Boston, Massachusetts, on January 10, 2004, was -10.6°C. The low temperature was -18.9°C. Find the daily mean temperature for that day.

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54. MULTI-STEP PROBLEM The table shows the changes in the values of one share of stock A and one share of stock B over 5 days.

Day of week	Monday	Tuesday	Wednesday	Thursday	Friday
Change in share value for stock A (dollars)	-0.45	-0.32	0.66	-1.12	1.53
Change in share value for stock B (dollars)	0.37	0.14	0.59	-0.53	1.02

- **a.** Find the average daily change in share value for each stock. Use estimation to check that your answers are reasonable.
- b. Which stock performed better over the 5 days? How much more money did the better performing stock earn, on average, per day?
- c. Can you conclude that the stock that performed better over all 5 days also performed better over the first 4 days of the week? *Explain* your reasoning.

2.7 Find Square Roots and Compare Real Numbers



You found squares of numbers and compared rational numbers. You will find square roots and compare real numbers. So you can find side lengths of geometric shapes, as in Ex. 52.

Key Vocabulary

- square root
- radicand
- perfect square
- irrational number
- real numbers

you will find the square roots of nonnegative numbers. For Your Notebook **KEY CONCEPT**

Recall that the square of 4 is $4^2 = 16$ and the square of -4 is $(-4)^2 = 16$.

The numbers 4 and -4 are called the square roots of 16. In this lesson,

- **Square Root of a Number**
 - Words If $b^2 = a$, then b is a square root of a.
 - **Example** $3^2 = 9$ and $(-3)^2 = 9$, so 3 and -3 are square roots of 9.

All positive real numbers have two square roots, a positive square root (or principal square root) and a negative square root. A square root is written with the radical symbol $\sqrt{}$. The number or expression inside a radical symbol is the radicand.



Zero has only one square root, 0. Negative real numbers do not have real square roots because the square of every real number is either positive or 0.

EXAMPLE 1 **Find square roots**

Evaluate the expression.

READING The symbol ± is read as 'plus or minus'	▶a. $\pm \sqrt{36} = \pm 6$	The positive and ne are 6 and -6.	egative square roots of 36	
and refers to both the	b. $\sqrt{49} = 7$	The positive square	e root of 49 is 7.	
positive square root and the negative square root.	c. $-\sqrt{4} = -2$	The negative squa	re root of 4 is -2.	
1	GUIDED PRACTICE	for Example 1		
	Evaluate the expre	ssion.		
	1. –√9	2. $\sqrt{25}$	3. $\pm \sqrt{64}$	4. −√81

PERFECT SQUARES The square of an integer is called a **perfect square**. As shown in Example 1, the square root of a perfect square is an integer. As you will see in Example 2, you need to approximate a square root if the radicand is a whole number that is *not* a perfect square.

💸 🤇 EXAMPLE 2 🕽 Approximate a square root

FURNITURE The top of a folding table is a square whose area is 945 square inches. Approximate the side length of the tabletop to the nearest inch.

Solution

You need to find the side length s of the tabletop such that $s^2 = 945$. This means that s is the positive square root of 945. You can use a table to determine whether 945 is a perfect square.

Number	28	29	30	31	32
Square of number	784	841	900	961	1024

As shown in the table, 945 is *not* a perfect square. The greatest perfect square less than 945 is 900. The least perfect square greater than 945 is 961.

900 < 945 < 961	Write a compound inequality that compares 945 with both 900 and 961.
$\sqrt{900} < \sqrt{945} < \sqrt{961}$	Take positive square root of each number.
30 < √945 < 31	Find square root of each perfect square.

The average of 30 and 31 is 30.5, and $(30.5)^2 = 930.25$. Because 945 > 930.25, $\sqrt{945}$ is closer to 31 than to 30.

The side length of the tabletop is about 31 inches.

USING A CALCULATOR In Example 2, you can use a calculator to obtain a better approximation of the side length of the tabletop.

2nd V 945) ENTER

The value shown can be rounded to the nearest hundredth, 30.74, or to the nearest tenth, 30.7. In either case, the length is closer to 31 than to 30.



GUIDED PRACTICE for Example 2

Approximate the square root to the nearest integer.

5. $\sqrt{32}$ 6. $\sqrt{103}$

 $7, -\sqrt{48}$

8. −√350

IRRATIONAL NUMBERS The square root of a whole number that is not a perfect square is an example of an *irrational number*. An **irrational number**, such as $\sqrt{945} = 30.74085...$, is a number that cannot be written as a quotient of two integers. The decimal form of an irrational number neither terminates nor repeats.
REAL NUMBERS The set of **real numbers** is the set of all rational and irrational numbers, as illustrated in the Venn diagram below. Every point on the real number line represents a real number.



READING

If you exclude 0 from

the whole numbers, the

resulting set is called

the natural numbers.

EXAMPLE 3 Classify numbers

Tell whether each of the following numbers is a real number, a rational number, an irrational number, an integer, or a whole number: $\sqrt{24}$, $\sqrt{100}$, $-\sqrt{81}$.

Number	Real number?	Rational number?	Irrational number?	Integer?	Whole number?
√24	Yes	No	Yes	No	No
√100	Yes	Yes	No	Yes	Yes
-\[1]	Yes	Yes	No	Yes	No

EXAMPLE 4 Graph and order real numbers

Order the numbers from least to greatest: $\frac{4}{3}$, $-\sqrt{5}$, $\sqrt{13}$, -2.5, $\sqrt{9}$.

Solution

Begin by graphing the numbers on a number line.



• Read the numbers from left to right: -2.5, $-\sqrt{5}$, $\frac{4}{3}$, $\sqrt{9}$, $\sqrt{13}$.

GUIDED PRACTICE for Examples 3 and 4

9. Tell whether each of the following numbers is a real number, a rational number, an irrational number, an integer, or a whole number: $-\frac{9}{2}$, 5.2, 0, $\sqrt{7}$, 4.1, $-\sqrt{20}$. Then order the numbers from least to greatest.

CONDITIONAL STATEMENTS In the activity on page 109, you saw that a conditional statement not in if-then form can be written in that form.

EXAMPLE 5 Rewrite a conditional statement in if-then form

Rewrite the given conditional statement in if-then form. Then tell whether the statement is *true* or *false*. If it is false, give a counterexample.

Solution

a. Given: No fractions are irrational numbers.

If-then form: If a number is a fraction, then it is not an irrational number.

The statement is true.

b. Given: All real numbers are rational numbers.

If-then form: If a number is a real number, then it is a rational number.

The statement is false. For example, $\sqrt{2}$ is a real number but *not* a rational number.

GUIDED PRACTICE for Example 5

Rewrite the conditional statement in if-then form. Then tell whether the statement is *true* or *false*. If it is false, give a counterexample.

- 10. All square roots of perfect squares are rational numbers.
- 11. All repeating decimals are irrational numbers.
- 12. No integers are irrational numbers.

2.7 EXERCISES

HOMEWORK KEY

on p. WS5 for Exs. 9, 19, and 47 *** = STANDARDIZED TEST PRACTICE** Exs. 2, 23, 41, 42, 48, and 51 *** = MULTIPLE REPRESENTATIONS** Ex. 52

) = WORKED-OUT SOLUTIONS

Skill PRACTICE

- 1. VOCABULARY Copy and complete: The set of all rational and irrational numbers is called the set of <u>?</u>.
- 2. *** WRITING** Without calculating, how can you tell whether the square root of a whole number is rational or irrational?

EXAMPLE 1	EVALUATING SQ	UARE ROOTS Evaluate t	he expression.	
on p. 110 for Exs. 3–14	3. √ 4	4. $-\sqrt{49}$	5. -√9	6. $\pm \sqrt{1}$
	7. √ 196	8. $\pm \sqrt{121}$	9. ±√2500	10. $-\sqrt{256}$
	11. $-\sqrt{225}$	12. √361	13. $\pm \sqrt{169}$	14. $-\sqrt{1600}$

EXAMPLE 2 on p. 111	APPROXIMATING SQ nearest integer.	UARE ROOTS Approxit	mate the square root	t to the
for Exs. 15-22	15. $\sqrt{10}$	16. $-\sqrt{18}$	17. $-\sqrt{3}$	18. $\sqrt{150}$
	$(19) -\sqrt{86}$	20. $\sqrt{40}$	21. $\sqrt{200}$	16. $\sqrt{150}$ 22. $-\sqrt{65}$
	13 400	20. ¥40	21. 7200	22 165
	23. ★ MULTIPLE CHO	NCE Which number is	between -30 and -2	25?
	(A) $-\sqrt{1610}$	$(\mathbf{B}) - \sqrt{680}$	$\bigcirc -\sqrt{410}$	$\bigcirc -\sqrt{27}$
EXAMPLES 3 and 4 on p. 112	in the list is a real nu	DERING REAL NUMBER Imber, a rational num Imber. Then order the	ber, an irrational nu	mber, an
for Exs. 24–29	24. $\sqrt{49}$, 8, $-\sqrt{4}$, -3		25. $-\sqrt{12}$, -3.7 , $\sqrt{2}$	9, 2.9
	26. -11.5, -\sqrt{121}, -1	$0, \frac{25}{2}, \sqrt{144}$	27. $\sqrt{8}, -\frac{2}{5}, -1, 0.6$	6, √6
	28. $-\frac{8}{3}$, $-\sqrt{5}$, 2.6, -1.	5, √ 5	29. −8.3, −√80, −	$\frac{17}{2}$, -8.25, $-\sqrt{100}$
EXAMPLE 5 on p. 113 for Exs. 30-33		DNAL STATEMENTS Rentes the state of the stat		
	30. All whole numbe	rs are real numbers.	:	
	31. All real numbers	are irrational number	s.	
	32. No perfect squar	es are whole numbers.		
	33. No irrational nur	nbers are whole numb	ers.	
	EVALUATING EXPRES	SIONS Evaluate the ex	pression for the give	en value of x.
	34. $3 + \sqrt{x}$ when $x =$	9	35. 11 – \sqrt{x} when	<i>x</i> = 81
	36. $4 \cdot \sqrt{x}$ when $x = 4$	49	37. $-7 \cdot \sqrt{x}$ when	x = 36
	38. $-3 \cdot \sqrt{x} - 7$ when	x = 121	39. $6 \cdot \sqrt{x} + 3$ whe	en x = 100
	an additive ident multiplicative in	whether each of the fo ity, additive inverses, a verses: whole numbers, able similar to the one	multiplicative identi , integers, rational nu	ty, and imbers, real
	41. ★ MULTIPLE CHO square?	HCE If $x = 36$, the value	e of which expressio	n is a perfect
	(A) $\sqrt{x} + 17$	(B) 87 – \sqrt{x}	$\textcircled{\textbf{C}} 5 \cdot \sqrt{x}$	(b) $8 \cdot \sqrt{x} + 2$
•		x > 0. Compare the value of the value of the compare the compare the compared of the compar		< x < 1 and for
8		l the first five perfect s Describe your method.	quares x such that 2	• \sqrt{x} is also a
		<i>n</i> be any whole numbe a rational number? <i>Ex</i>		

e worked-out solutions
 on p. WS1

* = STANDARDIZED TEST PRACTICE

1P

BIG IDEAS

For Your Notebook

Big Idea 🕧

Big Idea 🙆

Performing Operations with Real Numbers

To add or multiply two real numbers a and b, you can use the following rules:

Expression	Rule when a and b have the same sign	Rule when a and b have different signs
a + b	Add <i>a</i> and <i>b</i> . The sum has the same sign as <i>a</i> and <i>b</i> .	Subtract the lesser absolute value from the greater absolute value. The sum has the same sign as the number with the greater absolute value.
ab	The product is positive.	The product is negative.

You can use these rules to subtract or divide numbers, but first you rewrite the difference or quotient using the subtraction rule or the division rule.

Applying Properties of Real Numbers

You can apply the properties of real numbers to evaluate and simplify expressions. Many of the properties of addition and multiplication are similar.

Property	Addition	Multiplication		
Commutative property	a+b=b+a	ab = ba		
Associative property	(a + b) + c = a + (b + c)	(ab)c = a(bc)		
Identity property	a+0=0+a=a	$a \cdot 1 = 1 \cdot a = a$		
inverse property	a+(-a)=-a+a=0	$a \cdot \frac{1}{a} = \frac{1}{a} \cdot a = 1, a \neq 0$		
Distributive property	a(b + c) = ab + ac (and thr	ree variations)		

Big Idea 3

Classifying and Reasoning with Real Numbers

Being able to classify numbers can help you tell whether a conditional statement about real numbers is true or false. For example, the following statement is false: "All real numbers are integers." A counterexample is 3.5.

Numbers Description	
Whole numbers	The numbers 0, 1, 2, 3, 4,
Integers	The numbers , -3, -2, -1, 0, 1, 2, 3,
Rational numbers	Numbers of the form $\frac{a}{b}$ where <i>a</i> and <i>b</i> are integers and $b \neq 0$
Irrational numbers	Numbers that cannot be written as a quotient of two integers
Real numbers	All rational and irrational numbers

Worked-Out Solutions

This section of the book provides step-by-step solutions to exercises with circled exercise numbers. These solutions provide models that can help guide your work with the homework exercises.

The separate **Selected Answers** section follows this section. It provides numerous answers that you can use to check your own answers.

Chapter 1

Lesson 1.1 (pp. 5–7)

19. three tenths to the fourth power; $(0.3)^4 = 0.3 \cdot 0.3 \cdot 0.3 \cdot 0.3$

35. $\left(\frac{3}{5}\right)^3 = \frac{3}{5} \cdot \frac{3}{5} \cdot \frac{3}{5} = \frac{27}{125}$

51. a. Total length = 3.5 + 5.5 + 3 = 12

The total length is 12 inches.

b. Evaluate 12f for f = 12: 12(12) = 144

The area of water surface needed is 144 square inches.

Lesson 1.2 (pp. 10-12)

16.
$$\frac{1}{6}(6+18) - 2^2 = \frac{1}{6}(24) - 2^2$$

= $\frac{1}{6}(24) - 4$
= $4 - 4 = 0$

35. a. Total cost = $3 \cdot 0.99 + 2 \cdot 9.95$

$$= 2.97 + 19.90 = 22.87$$

The total cost is \$22.87.

b. Amount of money left = 25 - 22.87 = 2.13

The amount you have left is \$2.13.

Lesson 1.3 (pp. 18-20)

11. 7 less than twice a number k

Less than is subtraction after the next term, and twice a number is two times a number. The expression is 2k - 7.



The number of months is 12y.

33. a. 48 ounce container:

\$2.64	\$2.64 ÷ 48	\$.055
48 ounces	48 ounces ÷ 48	1 ounce
001		

The unit rate is \$.055 per ounce.

64 ounce container:

 $\frac{\$3.84}{64 \text{ ounces}} = \frac{\$3.84 \div 64}{64 \text{ ounces} \div 64} = \frac{\$.06}{1 \text{ ounce}}$ The unit rate is \$.06 per ounce.

- b. Since \$.055 is less than \$.06, the 48 ounce container costs less per ounce.
- c. Write a verbal model and an expression. Let *n* be the number of ounces.



$$= 0.06n - 0.055n$$

Evaluate the expression when n = 192.

0.06(192) - 0.055(192) = 0.96

The amount of money you save is \$.96.

Lesson 1.4 (pp. 24-26)

7. 5 more than a number t is written as t + 5.

The product of 9 and the quantity 5 more than a number t is written as 9(t + 5).

The product of 9 and the quantity 5 more than a number t is less than 6 is written as 9(t+5) < 6.

11

41. Write a verbal model. Then write an equation. Let w be the winning team's time.



173 - w = 6

Use mental math to solve the equation. Think: 173 less what number is 6?

Because 173 - 167 = 6, the solution is 167 hours.

Lesson 1.5 (pp. 31–33)

5. You know that the temperature in Rome, Italy, is 30°C, and the temperature in Dallas, Texas, is 83°F.

You want to find out which temperature is higher.

17. Step 1: You know the total weight of your backpack and its contents is $13\frac{3}{8}$ pounds. The total weight you want to carry is no more than 15 pounds. The weight of each bottle of water is

 $\frac{3}{4}$ pound. You want to find out how many extra bottles of water you can add to your backpack. First find the additional weight you can add to your backpack.

Step 2: Write a verbal model that represents what you want to find out. Then write an equation and solve it.

Step 3: Let w be the additional weight (in pounds) you can add to your backpack.



$$5 - 13\frac{5}{8} = w$$
$$1\frac{5}{8} = w$$

You can carry an additional $1\frac{5}{8}$ pounds, and each bottle weighs $\frac{3}{4}$ pound.

$$1\frac{5}{8} \div \frac{3}{4} = \frac{13}{8} \times \frac{4}{3} = \frac{52}{24} = 2\frac{1}{6}$$

Since you cannot carry a fraction of a bottle, round down to 2 bottles.

Step 4: You know that 2 is a solution; check to see if 3 could be a solution. The additional bottle of water weighs $\frac{3}{4}$ pound. Since $14\frac{7}{8}$ pounds is only $\frac{1}{8}$ pound less than the maximum of 15 pounds, and $\frac{3}{4} > \frac{1}{8}$, adding another bottle weighing $\frac{3}{4}$ pound would make the total weight more than 15 pounds. Therefore, the number of extra bottles of water you can add to your backpack is 2 bottles.

Lesson 1.6 (pp. 38-40)

- The pairing is not a function because the input ³/₄ is paired with two outputs, 3 and 5.
- You have 10 quarters that you can use for a parking meter.
 - a. Each time you put 1 quarter in the meter, you have 1 less quarter, so <u>the number of</u> <u>quarters left</u> is a function of <u>the number</u> <u>of quarters used</u>.
 - **b.** Let *y* represent the number of quarters you have left.



y = 10 - x

The domain of the function is: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10.

c. Make a table of inputs, x, and use y = 10 - x to find the corresponding outputs.

Input, x	0	1	2	3	4	5
Output, y	10	9	8	7	6	5
laput, x	6	7	8	9	10	
Output, y	4	3	2	1	0	

The range of the function is: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10.

Lesson 1.7 (pp. 46-48)

3. Make an input-output table using the given domain values.

x	0	1	2	3	4	5
V,	3	4	5	6	7	8

Plot a point for each ordered pair (x, y).

8		+ +	-
6		•	
6 5	-+-		-
	-	-	+
4 3 2		-	1
2	-	1.4	-
1		11	1

17. Number of voters v as a function of time t in years since 1984.

Years since 1984	Votors	Votors (millions)
0	92,652,680	93
4	91,594,693	92
8	104,405,155	104
12	96,456,345	96
16	105,586,274	106

The *t*-values range from 0 to 16, so label the *t*-axis from 0 to 18 in increments of 2 units. The *v*-values (in millions) range from 93 to 106, so label the *v*-axis from 90 to 114 in increments of 4 units.



Chapter 2



7. Graph -5 and -6 on a number line.

-7 -6 -6 -4 -3 -2 -1 0 1 2

On the number line, -5 is to the right of -6, so -5 > -6. The number -5 is greater.

29. If a = -6.1, then -a = -(-6.1) = 6.1.

If a = -6.1, then |a| = |-6.1| = 6.1.

53. Graph the numbers on a number line.

Read the numbers from left to right: -206, -170, -135, 2, 5.

From lowest elevation to highest elevation, the locations are Fondo, Frink, Alamorio, Calexico, and Date City. **Lesson 2.2** (pp. 77-79) **13.** -8.7 + 4.2 = -(|8.7| - |4.2|) = -(8.7 - 4.2) = -4.5**35.** -2.6 + (-3.4) + 7.6 = [-2.6 + (-3.4)] + 7.6

= -6 + 7.6 = 1.6

55. a. You know the first lens has a strength of -4.75 diopters and the second lens has a strength of 6.25 diopters.

You want to know the strength of the new lens.

Calculate the sum of -4.75 and 6.25:

-4.75 + 6.25 = 1.5

The strength of the new lens is 1.5 diopters.

b. You know the first lens has a strength of ~2.5 diopters and the second lens has a strength of -1.25 diopters.

You want to know the strength of the new lens.

Calculate the sum of -2.5 and -1.25:

-2.5 + (-1.25) = -3.75

The strength of the new lens is -3.75 diopters.

c. You know the first lens has a strength of 1.5 diopters and the second lens has a strength of -3.75 diopters. The greater the absolute value of the strength of a lens, the stronger the lens.

You want to know which new lens is stronger.

Find the absolute value of each lens in part (a) and part (b) and choose the greater.

|1.5| = 1.5 |-3.75| = 3.75

The new lens in part (b) has a greater absolute value, and is therefore stronger.

Lesson 2.3 (pp. 82–84)
3.
$$13 - (-5) = 13 + 5 = 18$$

21. When $x = 7.1$ and $y = -2.5$,
 $-y - (1.9 - x) = -(-2.5) - (1.9 - 7.1)$
 $= 2.5 - [1.9 + (-7.1)]$
 $= 2.5 - (-5.2)$
 $= 2.5 + 5.2 = 7.7$

43. Write a verbal model. Then write an equation.

Change in temperature	=	Temperature inside	-	Temperature outside
--------------------------	---	-----------------------	---	------------------------

C = i - t

Substitute 12.2 for i and -2.4 for t.

$$C = 12.2 - (-2.4)$$

$$C = 12.2 + 2.4 = 14.6$$

The change in temperature is 14.6°C.

Lesson 2.4 (pp. 91–93)

11.
$$-1.9(3.3)(7) = (-6.27)(7) = -43.89$$

31. $-2(-6)(-7z) = [-2(-6)](-7z)$
 $= 12(-7z)$
 $= [12 \cdot (-7)]z$
 $= -84z$
51. Write a verbal model.

Calculate the original price.

Original price = (\$3.50)(50) = \$175

Calculate the change in price.

Change in price = (-\$.25)(50) = -\$12.50

Calculate the total value.

Total value =
$$(3.50)(50) + (-0.25)(50)$$

= 175 + (-12.50) = 162.50

The total value is \$162.50.

Lesson 2.5 (pp. 99–101)

- 9. (p-3)(-8) = p(-8) 3(-8) = -8p + 24
- 23. Write the expression as a sum: $7x^2 + (-10) + (-2x^2) + 5$

Terms: $7x^2$, -10, $-2x^2$, 5

Like terms: $7x^2$ and $-2x^2$; -10 and 5

Coefficients: 7, -2

Constant terms: -10, 5

51. Write a verbal model. Then write an equation,

C = 3(r-2) or C = 3r - 6

Find the value of C when r = 3.99.

$$C = 3(3.99 - 2)$$

= 3(3.99) - 3(2)

$$= 11.97 - 6 = 5.97$$

The total cost is \$5.97.

Lesson 2.6 (pp. 106-108)

13.
$$-1 \div \left(-\frac{7}{2}\right) = -1 \cdot \left(-\frac{2}{7}\right) = \frac{2}{7}$$

35. $\frac{9z-6}{-3} = (9z-6) \div (-3)$
 $= (9z-6) \cdot \left(-\frac{1}{3}\right)$
 $= 9z \cdot \left(-\frac{1}{3}\right) - 6 \cdot \left(-\frac{1}{3}\right)$
 $= -3z + 2$

53. To find the daily mean temperature for a day, find the sum of the high and low temperatures for that day and then divide the sum by 2.

Mean =
$$\frac{-10.6 + (-18.9)}{2} = \frac{-29.5}{2} = -14.75$$

The daily mean temperature was -14.75°C.

Lesson 2.7 (pp. 113-116)

- 9. Since $50^2 = 2500, \pm \sqrt{2500} = \pm 50$.
- 19. Write a compound inequality that compares $-\sqrt{86}$ with both $-\sqrt{100}$ and $-\sqrt{81}$.

$$-\sqrt{100} < -\sqrt{86} < -\sqrt{81}$$

Take the square root of each number.

 $-10 < -\sqrt{86} < -9$

Because 86 is closer to 81 than to 100, $-\sqrt{86}$ is closer to -9 than to -10. So $-\sqrt{86}$ is about -9.

47. You need to find the side length s of the mazes such that s^2 is the given area in square feet, so s is the positive square root of the area. Then identify the side length as rational or irrational.

Dallas: $s^2 = 1225$, s = 35; rational

San Francisco: $s^2 = 576$, s = 24; rational

Corona: $s^2 = 2304$, s = 48; rational

Waterville: $s^2 = 900$, s = 30; rational

The side lengths are 35 feet, 24 feet, 48 feet, and 30 feet. All the lengths are rational numbers.

Chapter 3

Lesson 3.1 (pp. 137–140)

13. -2 = n - 6

-2 + 6 = n - 6 + 6

$$4 = n$$

55. Let w represent the width of the trampoline.

$$A = \ell \cdot w$$

$$187 = 17 \cdot w$$

$$\frac{187}{17} = \frac{17w}{17}$$

$$11 = w$$

The width of the trampoline is 11 feet.

Lesson 3.2 (pp. 144–146) 13. $7 = \frac{5}{6}c - 8$ $7 + 8 = \frac{5}{6}c - 8 + 8$ $15 = \frac{5}{6}c$

$$5 \quad 18 = c$$

$$-32 = -5k + 13k$$

$$-32 = 8k$$

$$\frac{-32}{8} = \frac{8k}{8}$$

$$-4 = k$$

19.

 $\frac{6}{10} \cdot 15 = \frac{6}{10} \cdot \frac{5}{10}c$

39. Write a verbal model. Then write an equation. Let *h* be the number of half-side advertisements.



$$6000 = 2000(1) + 800h$$

$$6000 = 2000 + 800h$$

Solve the equation.

6000 = 2000 + 800h

$$6000 - 2000 = 2000 - 2000 + 800h$$

$$\frac{4000}{800} = \frac{800h}{800}$$
$$\frac{5}{5} = h$$

The museum can have 5 half-side advertisements.

WORKED-OUT SOLUTIONS

17.

$$-3 = 12y - 5(2y - 7)$$

$$-3 = 12y - 10y + 35$$

$$-3 = 2y + 35$$

$$-3 - 35 = 2y + 35 - 35$$

$$-38 = 2y$$

$$\frac{-38}{2} = \frac{2y}{2}$$

$$-19 = y$$

39. Let x be the amount of space you should leave between posters (in feet).

Lesson 3.4 (pp. 157-159)

13.
$$40 + 14j = 2(-4j - 13)$$
$$40 + 14j = -8j - 26$$
$$40 + 14j + 8j = -8j + 8j - 26$$
$$40 + 22j = -26$$
$$40 - 40 + 22j = -26 - 40$$
$$22j = -66$$
$$j = -3$$

51. Let x represent the number of years. So 33x represents the increase in the number of students taking Spanish, and 2x represents the decreased number of students who are taking French.



So it will be after 3 more school years, or in about 4 years, when the number of students taking Spanish will be 3 times the number of students taking French.

Lesson 3.5 (pp. 165-167)

17.
$$\frac{16}{48} = \frac{n}{36}$$
$$36 \cdot \frac{16}{48} = 36 \cdot \frac{n}{36}$$
$$\frac{576}{48} = n$$
$$12 = n$$

49. Find the total number of pizzas: 96 + 144 + 240 = 480.

The ratio of large pizzas to all pizzas is

 $\frac{\text{number of large pizzas}}{\text{total number of pizzas}} = \frac{240}{480} = \frac{1}{2}.$

25. First create a table of values by substituting the domain values into the function.

x	$y=2\mu-5$
-2	y = 2(-2) - 5 = -9
-1	y = 2(-1) - 5 = -7
0	y = 2(0) - 5 = -5
1	y = 2(1) - 5 = -3
2	y = 2(2) - 5 = -1

The table gives the ordered pairs (-2, -9), (-1, -7), (0, -5), (1, -3), and (2, -1).

Graph the function by plotting these points. The range of the function is the y-values from the table: -9, -7, -5, -3, -1.

		у		1
	-	-		+-
++-		⊢	+	-
11-	1		11	1
1+	t	┢		+
	T			
	L			
	-	-		-

37. The table represents a function because there is exactly one low temperature for each day in the first week of February.

To graph the data, plot the ordered pairs (day, record low).

	y			1			1	
								0
	1		-1			1		
		1						
- 3	\square							I.
-1								x
			1		1			

Lesson 4.2 (pp. 219-221)

3. Test (-2, 3):

2y + x = 4

 $2(3) + (-2) \ge 4$ Substitute -2 for x and 3 for y.

So, (-2, 3) is a solution of 2y + x = 4.

11. First, solve the equation for y.

$$y + x = 2$$
$$y + x - x = 2 - x$$
$$y = 2 - x$$

Use this equation to create a table of values,

x	-2	-1	0	1	2
V	4	3.	2	1	0

Plot at least three of the points whose ordered pairs (x, y) are indicated by the table. Draw a line through the plotted points.





Since the scientist is studying the organisms in the first 4 kilometers of Earth's crust, the domain of the function is $0 \le d \le 4$. The range of the function is $20 \le T \le 120$. The

temperature 4 kilometers from the surface is 120°C.

b. Notice in the table for part (a) that the temperatures between 20°C and 95°C occur when the distance from the surface is between 0 kilometers and 3 kilometers.

				1
80		1	+	fì
	1	r +	+	a)
60 40 20	X	++-	+	9
20¥	-	+-+-	+	is
0	1	2 3	4 4	10

The domain of the function is now $0 \le d \le 3$ and the range is $20 \le T \le$ 95. So this section of crust is 3 kilometers deep.

Lesson 4.3 (pp. 229-232)



$$0 = -4x + 3$$

$$-3 = -4x$$

$$\frac{3}{4} = x$$

The x-intercept is $\frac{3}{4}$.

Substitute 0 for x in y = -4x + 3 and solve for y.

 $\gamma = -4(0) + 3 = 0 + 3 = 3$

The y-intercept is 3.

Plot the two points that correspond to the intercepts and draw a line through them.



13.

$$\frac{11}{w} = \frac{33}{w + 24}$$

$$11(w + 24) = 33w$$

$$11w + 264 = 33w$$

$$11w - 11w + 264 = 33w - 11w$$

$$264 = 22w$$

$$12 = w$$

39. The ratio of model to height is $\frac{\text{height of model}}{\text{actual height}}$. Write and solve a proportion.

 $\frac{1}{25} = \frac{x}{443.2}$ 443.2 = 25x 17.728 = x

The height of the model is 17.728 meters.

Lesson 3.7 (pp. 179-181)

13. $a = p\% \cdot b$

- = 115% · 60
- = 1.15 · 60
- = 69 69 is 115% of 60.
- **35. a.** The survey shows that 36% of the 250 listeners who participated in the survey are "tired of" the song.
 - $a = p\% \cdot b$
 - = 36% 250
 - = 0.36 + 250
 - = 90

90 listeners are "tired of" the song.

b. The survey shows that 14% of the 250 listeners who participated in the survey "love" the song.

$$a = p\% \cdot b$$

$$= 14\% \cdot 250$$

35 listeners "love" the song.

17.
$$30 = 9x - 5y$$

 $30 + 5y = 9x - 5y + 5y$
 $30 + 5y = 9x$
 $30 - 30 + 5y = 9x - 30$
 $5y = 9x - 30$
 $y = \frac{9}{5}x - 6$
33. a. $C = 12x + 25$
 $C - 25 = 12x + 25 - 25$
 $C - 25 = 12x$
 $\frac{C - 25}{12} = x$
b. $\$145: \frac{C - 25}{12} = x$
 $\frac{145 - 25}{12} = x$
 $10 = x$

Losson 2.0

For \$145, you bowled 10 league nights.

\$181:
$$\frac{C-25}{12} = x$$

 $\frac{181-25}{12} = x$
 $13 = x$

For \$181, you bowled 13 league nights.

$$\$205: \frac{C-25}{12} = x$$
$$\frac{205-25}{12} = x$$
$$15 = x$$

For \$205, you bowled 15 league nights.

Chapter 4

Lesson 4.1 (pp. 209-212)

15. To plot Q(-1, 5), begin at the origin. First move 1 unit to the left, then 5 units up. Point Q is in Quadrant II.

1			y	
	0			
_				
	+++			
		-1		
+		-	$\left \right $	

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Selected Answers

Chapter 1

1.1 Skill Practice (pp. 5–6) 1. exponent: 12, base: 6 3. 60 5. 12 7. 12 9. 3 11. 10 13. $\frac{1}{3}$ 17. seven to the third power, 7 · 7 · 7 19. three tenths to the fourth power, 0.3 · 0.3 · 0.3 · 0.3 21. *n* to the seventh power, $n \cdot n \cdot n \cdot n \cdot n \cdot n \cdot n \cdot 23$. *t* to the fourth power, $t \cdot t \cdot t \cdot t$ 25. The base was used as the exponent and the exponent was used as the base; $5^4 = 5 \cdot 5 \cdot 5 \cdot 5 =$ 625. 27. 100 29. 1331 31. 243 33. 1296 35. $\frac{27}{125}$ 37. $\frac{1}{216}$ 39. 1.21 41. 40.5 43. 9.6

1.1 Problem Solving (pp. 6–7) **49.** 162.5 cm **51. a.** 12 in. **b.** 144 in.² **53.** New England Patriots

1.2 Skill Practice (pp. 10–11) I. Square 4. 3.8 5. 14 7. $3\frac{3}{5}$ 9. $63\frac{3}{4}$ 11. 21 13. 73.5 15. $12\frac{1}{2}$ 17. 48 21. $\frac{1}{2}$ was multiplied by 6 before squaring 6; $20 - \frac{1}{2} \cdot 6^2 =$ $20 - \frac{1}{2} \cdot 36 = 20 - 18 = 2$. 23. 29 25. 126 27. 0.75 29. 3 33. $(2 \times 2 + 3)^2 - (4 + 3) \times 5$

1.2 Problem Solving (pp. 11-12) **35. a.** \$22.87 **b.** \$2.13 **37.** Sample answer: $(3 \times 4) + 5$ **39. a.** \$380, \$237.99; \$142.01 **b.** Sample answer: You could write an expression showing the difference of your income and expenses as 10s - (4.50m + 12.99).

1.2 Graphing Calculator Activity (p. 13) 1.5 3.0.429 5.0.188 7.40.9 BMI units

1.3 Skill Practice (pp. 18–19) 1. rate 3. x + 8 5. $\frac{1}{2}m$ 7. 7 – n 9. $\frac{2t}{12}$ 11. 2k – 7 15. 4v 17. $\frac{16}{p}$ 19. 7 – d21. 12y 23. 0.2 ft/sec 25. 83.6 ft/sec 27. Feet should cancel out; \$54. 29. \$19.50 for 1 h

1.3 Problem Solving (pp. 19–20) 31. 19.95*t* + 3; \$102.75 **33. a.** \$.055, \$.06 **b.** 48 oz container **c.** \$.96 **35.** \$500 **37. a.** $12g + h + \frac{1}{4}c$ **b.** 247; 376.75; 242

1.4 Skill Practice (pp. 24-25) 1. Sample answer: 3x + 5 = 20 **3.** 42 + n = 51 **5.** $9 - \frac{t}{6} = 5$ **7.** 9(t + 5) < 6 **9.** 8 < b + 3 < 12 **11.** 10 < t - 7 < 20 **13.** $p \ge 12.99$ **15.** The wrong inequality symbol is used; $\frac{t}{4.2} \le 15$. 17. solution 19. not a solution 21. not a solution 23. solution 25. solution 27. not a solution 29. 5 31. 12 33. 9 35. 3x - 2 = x + 5; solution

1.4 Problem Solving (pp. 25–26) **39.** 7.5 mi **41.** 167 h **43.** \$100 **45. a.** $6r + 5(10 - r) \ge 55$ **b.** Yes; you will earn \$30 running errands and \$25 walking dogs; 30 + 25 = 55. c. Yes; if you work 10 hours running errands, you will earn \$60. You will not meet your goal if you work all 10 hours walking dogs.

1.5 Skill Practice (p. 31) **1.** Sample answer: d = rt**3.** You know the cost of materials and the amount you hope to make. You need to find the amount you should charge for each collar. You need to know the number of collars you made, which is missing. **5.** You know the temperature in Rome and the temperature in Dallas. You know the formula to convert Fahrenheit temperatures to Celsius temperatures. You need to find the higher temperature. **7.** The formula for perimeter should be used, not area; $P = 2\ell + 2w$; P = 2(200) + 2(150) = 700; \$10(700) = \$7000. **9.** P = I - E

1.5 Problem Solving (pp. 32–33) 15. 46.25 in.² 17. 2 water bottles 19. a. 960 ft b. 480 ft

21 . a .	Room size (feet)	1 by 1	2.by 2	3 by 3	4 by 4	5 by 5
	Remaining area (square feet)	`431	428	423	416	407

b. $1 \le s \le 5; 5 \text{ ft}$

1.5 Problem Solving Workshop (p. 34)

1.9 pieces of cake; Equation: Let c be the number of pieces of cake; 9c = 99, c = 11. Diagram: Draw a diagram of a 9 inch by 11 inch pan and cut the cake into 3 inch by 3 inch pieces. From the diagram you see

that you can cut 9 such pieces. The diagram shows that you cannot actually cut 11 square pieces because of the shape of the pan.

3. The equation should be 3x + 6 = 12 because there are only 3 spaces between the 4 floats; 3(2) + 6 = 12.

1.6 Skill Practice (pp. 38-39) 1. input; output
3. domain: 0, 1, 2, and 3, range: 5, 7, 15, and 44
5. domain: 6, 12, 21, and 42, range: 5, 7, 10, and 17
7. not a function 9. The pairing is a function.
Each input is paired with only one output.

	Sample	Input	t 0	utput	Input	t 0	utpu
		0-	f	5	0		5
		2-		6	1		6
		3-4-	T.	9	2		7
		4-5-	H	10	3		7
					4		9
				-	5		10
	laput	4	5	7	8	12	
	Million .		-				
	Output	7.5	8.5	10.5	11.5	15.5	-
		7.5					5
	Output	7.5					5
	Output range: 7	7.5 7.5, 8.	5, 10.	5, 11.	5, and		5
•	Output range: 7 Input	7.5 7.5, 8. 4 5	5, 10. 6 6	5, 11. 9 7.5	5, and		5
•	Output range: 7 Input Output	7.5 7.5, 8. 4 5	5, 10. 6 6	5, 11. 9 7.5	5, and		5

21. y = x - 8

1.6 Problem Solving (pp. 39-40) 23. a. the number of quarters left; the number of quarters used **b.** y = 10 - x; domain: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10

c.	Input	0	1	2	3	4	5	6	7	8	9	1 0
	Output	10	9	8	7	6	5	4	3	2	1	0

range: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, and 10

25. y = 100 + 20m; independent variable: *m*, the number of months; dependent variable: *y*, the amount of money saved; domain: m > 0, range: $y \ge 100$; \$340

27.a.	2	3	4	5
	A, B, C	D, E, F	G, H, I	J, K, L
Γ	6	7	8	9
	M, N, O	P, Q, R, S	T, U, V	W, X, Y, Z

No; because there is more than one output for each input.

b.	A	B	С	D	Ε	F	6	H	I.	J	к	L		
	2	2	2	3	3	3	4	4	4	5	5	5		
	М	N	0	P	Q	R	S	т	U	۷	W	X	γ	Z
	6	6	6	7	7	7	7	8	8	8	9	9	9	9

Yes; because there is only one output for each input.

1.6 Graphing Calculator Activity (p. 41) **1.** 50°F; scroll down until you see the output 10, look to see that the input is 50.

Inpot	0	1	2	3
Output	5	5.75	6.5	7.25
Input	1	2	3	4

1.7 Skill Practice (pp. 46-47) 1. domain; range





9. The domain and range are graphed backwards.



11. y = 2x - 2; domain: 1, 2, 3, and 4, range: 0, 2, 4, and 6

1.7 Problem Solving (pp. 47-48)



17.	Years since 1984	Veters	Voters (millions)
	0	92,652,680	93
	4	91,594,693	92
	8	104,405,155	104
	12	96,456,345	96
	16	105,586,274	106



19. a. increases **b.** Yes; 27.5 grams is between the mass of an egg that is just under 38 millimeters long and an egg that is just over 38 millimeters long.

Extension (p. 50) 1. function 3. not a function 5. function 7. Not a function. Sample answer: There could be many students whose first names have 4 letters, for instance, but their last names could all have a different number of letters. 9. Function; for each of your birthdays, you have only one height.

Chapter Review (pp. 53-56) 1. 7, 12 3. algebraic expression 5. 16 7. 10 9. 400 11. 25 in.^2 13. 9 15. 8 17. $\frac{1}{3}$ 19. 52 21. 18 23. z = 5 25. $3x^2$ 27. 2.95n + 2.1929. 13 + $t \ge 24$ 31. solution 33. 240 ft²

35.	Input	10	12	15	20	21
	Output	5	7	10	15	16
	range: 5 y = x + y		• y 16	and]	.6	
			12		•	

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8	
	_
12	R
	-

Chapter 2

2.1 Skill Practice (pp. 67-68) 1. rational number 3. Zero is in the set of whole numbers, but not in the set of positive integers. 5-13. Check students' graphs. 5.7 7. -5 9.5 11. -1 13. -2 15. 1.6: rational number, 1: whole number, integer, rational number, -4: integer, rational number, 0: whole number, integer, rational number; -4, 0, 1, 1.6 17. $-\frac{2}{3}$: rational number, -0.6: rational number, -1: integer, rational number, $\frac{1}{2}$: rational number; -1, $-\frac{2}{3}$, -0.6, $\frac{1}{3}$ 19. 16: whole number, integer, rational number, -1.66: rational number, $\frac{5}{3}$: rational number, -1.6: rational number; -1.66, -1.6, $\frac{5}{3}$, 16 21. -4.99: rational number, 5: whole number, integer, rational number, $\frac{16}{3}$: rational number, -5.1: rational number; $-5.1, -4.99, 5, \frac{16}{3}$ **23.** -6, 6 **25.** 18, 18 **27.** -13.4, 13.4 **29.** 6.1, 6.1 **31.** $1\frac{1}{9}$, $1\frac{1}{9}$ **33.** $-\frac{3}{4}$, $\frac{3}{4}$ **35.** Hypothesis: a number is a positive integer, conclusion: the number is a whole number; true. 37. Hypothesis: a number is positive, conclusion: its opposite is positive; false. Sample answer: The opposite of 2 is -2, a negative number. 41. -|-0.2| is a negative number. Sample answer: In the number -|-0.2|, remove both negative signs. 43.1 45.1.75 47.2.25 49.1.5

2.1 Problem Solving (pp. 69-70) 53. Fondo, Frink, Alamorio, Calexico, Date City 55. -3.4; the absolute value of -3.4 is less than the absolute value of -3.8, so it is closer to 0, the exact pitch. 57. a. 500 Hz b. The intensity decreases until 500 Hz and then increases. 59. a. Sun, Sirius, Canopus, Arcturus, Capella, Achernar; Canopus, Achernar, Arcturus, Capella, Sirius, Sun b. Rigel's apparent magnitude is greater than the Sun's apparent magnitude, so it is dimmer than the Sun; Rigel's absolute magnitude is less than the Sun's absolute magnitude, so it is brighter than the Sun. c. No. Sample answer: The apparent magnitude of Arcturus is less than the apparent magnitude of Achernar, but the absolute magnitude of Arcturus is greater than the absolute magnitude of Achernar.

Extension (p. 72) 1. {1, 3, 5, 6, 7, 9}, {3, 9} 3. {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}, \emptyset 5. $R = \{2, 4, 6, 8, 10\}, f = \{(1, 2), (2, 4), (3, 6), (4, 8), (5, 10)\}$ 7. $R = \{4, 8, 12, 16, 20\}, f = \{(1, 4), (5, 8), (9, 12), (13, 16), (17, 20)\}$ 9. the set of integers, \emptyset

2.2 Skill Practice (pp. 77-78) **1.** 0 **3.** -8 **5.** 6 7. -13 **9.** -6 **11.** -20 **13.** -4.5 **15.** 6.6 **17.** -15.2 **19.** $7\frac{1}{15}$ **21.** $1\frac{16}{45}$ **23.** $-20\frac{23}{24}$ **25.** The numbers have different signs, so their absolute values should have been subtracted, 17 + (-31) = -14. **27.** Associate property of addition **29.** Identity property of addition **31.** Commutative property of addition **33.** -49 **35.** 1.6 **37.** $5\frac{19}{60}$ **39.** -3 **41.** -9.5 **43.** $7\frac{23}{60}$ **45.** 0 **47.** 7.4 **49.** -(-18) + (-18); 0

2.2 Problem Solving (pp. 78-79) 53. 7°F

55. a. 1.5 diopters **b.** -3.75 diopters **c.** part (b) **57. a.** your friend **b.** No, if you score 2 double eagles, you will have the same score.

2.3 Skill Practice (pp. 82–83) 1. -3 + (-6) 3. 18 5. -87. 14.1 9. -25.8 11. $-\frac{1}{3}$ 13. $\frac{3}{4}$ 15. 8 was substituted for y instead of -8; 3 - (-8) + 2 = 3 + 8 + 2 = 13. 17. 4.6 19. 10.6 21. 7.7 23. 7.6 25. 1.8 27. 107°F 29. -1280 m 31. 127.1 mi 33. 8 35. -4.2 37. 16.4 39. No; Sample answer: 5 - (3 - 2) = 4, but (5 - 3) - 2 = 0 and 5 - 3 = 2, but 3 - 5 = -2.

2.3 Problem Solving (pp. 83–84) **43.** 14.6°C **45. a.** *d* = *t* - 342

b. [t	d	341.7 and 340.9; you can tell if
	341.7	-0.3	t – 342 is negative. 47. a. 6°; 19° b. –4°
	-343.8	1.8	47.4.0,17 04
	340.9	-1.1	
	342.7	0.7]

2.3 Spreadsheet Activity (p. 85) 1. 6 hand grips 3. 4.902; the difference in the lengths has the smallest absolute value.

2.4 Skill Practice (pp. 91-92) 1.1 3. -28 5.90

7. -36 **9.** 7 **11.** -43.89 **13.** -40 **15.** -80 **17.** $2\frac{2}{5}$

19. Multiplicative property of zero 21. Identity property of multiplication 23. Associative property of multiplication 25. Identity property of multiplication 27. Multiplicative property of -1
 29. 18x; 18x, same signs, product is positive.
 31. -84z; 12(-7z), product of -2 and -6 is 12; [12 • (-7)]z, associative property of multiplication; -84(z), product of 12 and -7 is -84; -84z, multiply.

33. -40c; 2(4)(-5c), product of $-\frac{1}{5}$ and -10 is 2;

8(-5c), product of 2 and 4 is 8; [8 \cdot (-5)]c, associative property of multiplication; -40(c), product of 8 and -5 is -40; -40c, multiply. **35.** 16.8 r^2 ; [-6 $r \cdot$ (-2.8)]r, associative property of multiplication; [-6 \cdot (-2.8) $\cdot r$]r, commutative property of multiplication; (16.8r)r, product of -6 and -2.8 is 16.8; 16.8($r \cdot r$), associative property of multiplication; 16.8 r^2 , multiply **37.** -0.4 **39.** -12.6 **41.** -6.6 **43.** -1(7) = -7, not 7; -1(7)(-3)(-2x) = -7(-3)(-2x) = 21(-2x) = -42x **45.** true **47.** true

2.4 Problem Solving (pp. 92-93) 51. \$162.50

55. a. f = 11,250 + (-30t), f = 135,000 + (-240t)**b.** 11,160 gal, 134,280 gal c. Rhododendron; 45,000 gal; the Rhododendron takes 375 hours to burn all of its fuel; the Spokane takes 562.5 hours to burn all of its fuel; to find the number of hours the Rhododendron will take to burn all its fuel, use the equations in part (a) and find the additive inverse of 11,250, then divide it by -30; to find the number of hours the Spokane will take to burn all its fuel, use the equations in part (a) and find the additive inverse of 135,000, then divide it by -240.

Extension (p. 95) 1.
$$\begin{bmatrix} 16 & 4 \\ 8 & 12 \end{bmatrix}$$
 3. $\begin{bmatrix} -15 & -4 & -9 \\ -2 & 2 & -5 \end{bmatrix}$
5. Cannot be performed. 7. $\begin{bmatrix} -28 & -49 \\ 3\frac{1}{2} & 3\frac{1}{9} \end{bmatrix}$ 9. $\begin{bmatrix} -72 \\ 20.4 \\ 4.2 \end{bmatrix}$

1.	Calcium (mg)	Potassium (mg),	13.	-41 78	-99 91
	263.52	290.36	I	L	••1
-	270.84	341.6			
	246.44	324.52			

1

2.5 Skill Practice (pp. 99–100) 1. 4, -9 3. The negative was not distributed to the -8; 5y - (2y - 8) = 5y - 2y + 8 = 3y + 8. 5. 4x + 12 7. 5m + 25 9. -8p + 2411. 4r - 6 13. $6v^2 + 6v$ 15. $2x^2 - 6x$ 17. $\frac{1}{4}m - 2$ 19. 4n - 6 21. terms: -7, 13x, 2x, 8; like terms: -7 and 8, 13x and 2x; coefficients: 13, 2; constant terms: -7, 8 23. terms: $7x^2$, -10, $-2x^2$, 5; like terms: $7x^2$ and $-2x^2$, -10 and 5; coefficients: 7, -2; constant terms: -10, 5 25. terms: 2, 3xy, -4xy, 6; like terms: 2 and 6, 3xy and -4xy; coefficients: 3, -4; constant terms: 2, 6 29. 5y 31. 9a - 2 33. 8r + 8 35. 3m + 537. 10w - 35 39. 15s + 6 41. 34 - 24w; 72 - 108w43. \$38.97 45. \$11.88 47. 2(6 + x) + (x - 5); 3x + 7

2.5 Problem Solving (pp. 100–101) **51.** C = 3r - 6; \$5.97 **53.** s = d(x + y + z) = dx + dy + dz

2.5 Problem Solving Workshop (p. 102) 1. \$330 3. \$287.50

2.6 Skill Practice (pp. 106–107) **1.** multiplicative inverse **3.** $-\frac{1}{18}$ **5.** -1 **7.** $-1\frac{1}{3}$ **9.** $-\frac{3}{13}$ **11.** -7 **13.** $\frac{2}{7}$ **15.** -3 **17.** $-2\frac{1}{2}$ **19.** $\frac{2}{7}$ **21.** -22 **25.** $-1\frac{2}{3}$ **27.** $2\frac{1}{4}$ **29.** $-2\frac{1}{5}$ **31.** 0.1 **33.** 3x - 7 **35.** -3z + 2 **37.** $\frac{1}{2} - \frac{5}{2}q$ **39.** $3a + 1\frac{1}{4}$ **41.** 4 - 3c **43.** -2 was added instead of subtracted; $\frac{-15x - 10}{-5} = (-15x - 10) \cdot (-\frac{1}{5}) =$ $-15x(-\frac{1}{5}) - 10(-\frac{1}{5}) = 3x + 2$ **45.** $-1\frac{1}{3}$ **47.** $\frac{1}{3}$

2.6 Problem Solving (pp. 107-108) **53.** -14.75° C **57. a.** -0.034 **b.** Yes; it will improve to -0.012. **c.** If the player had the same number of aces as service errors, then a = e, so $f = \frac{a-a}{s} = 0$; if all the serves were aces, *a* would be equal to *s* and *e* would be 0, so $f = \frac{s-0}{s} = \frac{s}{s} = 1$; if all the serves were errors, then e = s and a = 0, so $f = \frac{0-s}{s} = \frac{-s}{s} = -1$.

2.7 Skill Practice (pp. 113–114) 1. real numbers 3. 2 5. -3 7. 14 9. ± 50 11. -15 13. ± 13 15. 3 17. -219. -9 21. 14 25. $-\sqrt{12}$: real number, irrational number, -3.7: real number, rational number, $\sqrt{9}$: real number, rational number, integer, whole number, 2.9: real number, rational number; -3.7, $-\sqrt{12}$, 2.9, $\sqrt{9}$ 27. $\sqrt{8}$: real number, irrational number, $-\frac{2}{5}$: real number, rational number, -1: real number, rational number, integer, 0.6: real number, rational number, $\sqrt{6}$: real number, irrational number; -1, $-\frac{2}{5}$, 0.6, $\sqrt{6}$, $\sqrt{8}$ 29. -8.3: real number, rational number, $-\frac{17}{2}$: real number, $-\sqrt{80}$: real number, irrational number, $-\frac{17}{2}$: real number, rational number, $-\sqrt{80}$: real number, -8.25: real number, rational number, rational number, $-\sqrt{100}$: real number, rational number, rational number, $-\sqrt{100}$: real number, rational number, rational number, rational number, $-\sqrt{100}$: real number, rational number, rational number, rational number, rational number, integer; $-\sqrt{100}$, $-\sqrt{80}$, $-\frac{17}{2}$, -8.3, -8.25 31. If a number is a real number, then it is an irrational number; false. Sample answer: 3 is a real number and a rational number. 33. If a number is an irrational number, then it is not a whole number; true. 35. 2 37. -42 39. 63 41. B

2.7 Problem Solving (pp. 115-116) 45. 60 in. 47. 35 ft 49. 2.2 ft 51. a. 144 tiles b. 16 ft. *Sample answer*: If the homeowner can buy 144 tiles that are each 256 square inches, then the total area is (144 tiles)(256 square inches per tile) = 36,864 square inches. Divide 36,864 square inches by 144 square inches to find the number of square feet, 256 square feet. If the area of the square is 256 square feet, take the square root of 256 to find the side length, 16 feet.

Extension (p. 118) 1. The sum is even. **3.** The sum is odd. **5.** Not closed **7.** Identity property of multiplication; Distributive property; Inverse property of multiplication; Property of zero

Chapter Review (pp. 121–124) I. terms: -3x, -5, -7x, -9; coefficients: -3, -7; constant terms: -5, -9; like terms: -3x and -7x, -5 and -9 3. real number, rational number 5. real number, rational number, integer 7. -6, -5.2, $-\frac{3}{8}$, $-\frac{1}{4}$, 0.3 9. 0.2, 0.2 11. $-\frac{7}{8}$, $\frac{7}{8}$ 13. 3 15. -3.5 17. $-1\frac{3}{14}$ 19. -\$.23 million 21. -1023. -6.1 25. $-\frac{31}{36}$ 27. $2\frac{1}{2}$ 29. -60 31. -18 33. 6x; $x \cdot (-18) = -\frac{1}{3}(-18)(x)$, commutative property of multiplication; 6(x), product of $-\frac{1}{3}$ and -18; 6x, multiply 35. 2.74 ft 37. -3y - 27 39. 3x + 8 **41.** $9n - 3\frac{1}{2}$ **43.** -14 **45.** $\frac{2}{3}$ **47.** 3x - 5 **49.** 2n + 1**51.** -6 **53.** ± 15 **55.** -7 **57.** 17 **59.** $-\sqrt{4}$, -0.3, 0, 1.25, $\sqrt{11}$

Chapter 3

3.1 Skill Practice (pp. 137–138) 1. inverse operations **3.3 5.5 7.** -3 **9.7 11.17 13.4 17.4 19.6 21.** -15**23.** 15 **25.** 48 **27.** 22 **29.** The student multiplied x by 100 to produce a number with a decimal part identical to the decimal part of x. When the student subtracted, the result was a whole number. **35.** -2.05 **37.** $\frac{5}{8}$ **39.** 0.06 **41.** 96 **43.** 12 **45.** -56**47.** $\frac{3}{5}$ **49.** 54 = 12x; 4.5 in.

3.1 Problem Solving (pp. 139-140) 53. 1046.6 ft

55. 11 ft **57. a.** $\frac{4}{7}x = 200$ **b.** Plants; if you solve the equation in part (a) you find that there are 350 species of birds.

59. a.	t	d	b. d		1		1	4 sec
	1	6.5	30	-	+-	H	1	
	2	13	25 20		1			
	3	19.5	15 10		•		-	1.
	4	26	5	•			-	
	5	32.5		1	2 :	3 4	5 1	5

c. 26 = 6.5t; 4 sec 61. a. 171 hits b. 215 hits c. No; if Mueller had fewer hits than Wells but had a higher batting average, he must have had fewer at bats than Wells.

3.2 Skill Practice (pp. 144–145) **1.** like terms **3.** 4 **5.** 2 **7.** -3 **9.** 6 **11.** 40 **13.** 18 **15.** 4 **17.** 9 **19.** -4**23.** The division of -2x + x by -2 is done incorrectly. *Sample answer:* If like terms are combined as the first step, the second line would be -x = 10 and the final result would be x = -10. **25.** y = 2x + 4; -7 **27.** 4 **29.** 5 **31.** 0.5 **33.** 15.9 **35.** 6.9

3.2 Problem Solving (pp. 145–146) 37. 28 classes **39.** 5 half-side advertisements **41.** Yes; the equation \$542 = \$50 + 6x gives the monthly cost of a guitar that costs \$542. Solving the equation gives x = \$82 per month, so you can afford the guitar. **43. a.** y = 12x

11. 3			· · · · · · · · · · · · · · · · · · ·			
b.	x (hours)	Marissa	Ayan	Total		
	1	5	7	12		
	2	10	14	24		
	3	15	21	36		
	4	20	28	48		
	5	25	35	60		

SELECTED ANSWERS

с. У				about 4.5 h
60			-	
48				
36	+-	•		
36 24	-+		-	
12			-	
0	1 1	1 + 1	1.2	

3.2 Problem Solving Workshop (p. 147) 1.7 players 3.4 chairs

3.3 Skill Practice (pp. 150–151) 1. $\frac{5}{3}$ 3. 3 5. 6 7. -2 9. -8 11. -8 13. 4 15. -9 17. -19 19. 12 21. -2 23. -9 25. -3 times -6 is 18, not -18; 5x - 3x + 18 =2, 2x + 18 = 2, 2x = -16, x = -8. 27. 2 29. 3 31. -5 33. 2 35. 9.5 in., 6 in.; if you use the perimeter formula $P = 2\ell + 2w$ and substitute 3.5 + w for ℓ , the solution is w = 6.

3.3 Problem Solving (pp. 152-153) 39. 0.75 ft

41. a. 34 mo **b.** 307 ft per mo **c.** After the work crews merged; before the work crews merged they were working at a rate of 115 + 137 = 252 feet per month, and after merging at a rate of 307 feet per month.

3.4 Skill Practice (pp. 157–158) 1. identity 3. -25. -4 7. -7 9. 8 11. -4 13. -3 17. Sample answer: Distribute the 3 to get 6z - 15 = 2z + 13, then subtract 2z from each side to get 4z - 15 = 13, next add 15 to each side to get 4z = 28, finally divide each side by 4 to get z = 7. 19. 2 21. -7 23. no solution 25. no solution 27. The 3 was not distributed to both terms; 3x + 15 = 3x + 15, 15 = 15, so the equation is an identity. 29. Sample answer: 5x + 4 = 5x; the number 5x cannot be equal to 4 more than itself. 31. 2 33. -4 35. 6 37. identity 39. 2 41. 10 43. identity 45. 60

3.4 Problem Solving (pp. 158–159) 49. 9 nights 51. about 4 yr 53. a. 23.4t = 24(t - 0.3); 12 sec b. about 4.4 sec c. No; it would take 12 seconds for the sheepdog to catch up to the collie and it only takes 4.4 seconds for the collie to complete the last leg.

3.4 Spreadsheet Activity (p. 160) 1.2 3.4

3.5 Skill Practice (pp. 165–166) 1. ratios 3. no; 7 to 9 5. yes 7. $\frac{6}{5}$ 9. 22 11. 48 13. 15 15. 40 17. 12 21. Multiply each side by 6, not $\frac{1}{6}$; $6 \cdot \frac{3}{4} = 6 \cdot \frac{x}{6}$, $4\frac{1}{2} = x$. 23. $\frac{3}{8} = \frac{x}{32}$; 12 25. $\frac{x}{4} = \frac{8}{16}$; 2 27. $\frac{b}{10} = \frac{7}{2}$; 35 29. $\frac{12}{18} = \frac{d}{27}$; 18 31. 1.8 33. 2.4 35. 4 37. 4 39. 2 41. 3.5 43. Yes. Sample answer: $\frac{3}{6} = \frac{4}{8}$ **3.5 Problem Solving** (pp. 166–167) **45.** $\frac{2}{145}$ **47.** $\frac{2}{5}$ **49.** $\frac{1}{2}$ **51.** 45 goals **53. a.** $\frac{10}{23}$ **b.** 110 lift tickets **c.** 40 snowboarders

3.6 Skill Practice (pp. 171–172) **1.** cross product **3.** 6 **5.** 24 **7.** 1 **9.** -49 **11.** 2 **13.** 12 **17.** Use the cross products property to multiply 4 by x and 16 by 3; $4 \cdot x = 3 \cdot 16, 4x = 48, x = 12$. **19.** 15 **21.** 10 **23.** 5.5 **25.** -3.4 **27.** 4.2 **29.** -5.9 **31. a.** Multiplication property of equality **b.** Multiply **c.** Simplify

3.6 Problem Solving (pp. 172–173) 33.5 c 35. 90 km 37. 7.5 km 39. 17.728 m 41. 80 yd; find the actual length of the field by using the ratio 1 in.:20 yd, then use that number to find the width of the soccer field by using the ratio 3:2.

Extension (p. 175) 1, 24 in. 3, 16 m 5, 37.5 ft

3.7 Skill Practice (pp. 179–180) 1. percent: 15, base: 360, part: 54 **3.** 36% **5.** 28 **7.** 150 **9.** 70% **11.** 6% **13.** 69 **15.** 25 **17.** 95 **21.** 76.5% needs to be changed to 0.765; 153 = 0.765 • b, b = 200. **23.** 96% **25.** 150 **27.** 6% **29.** 30% **31.** No. *Sample answer:* The area of the smaller square would be 16% of the area of the larger square because the percent needs to be squared.

3.7 Problem Solving (pp. 180-181) 33.8%

35. a. 90 listeners **b.** 35 listeners **37.** 59.3%; 16.5%; 13.2%; 11.0% **39. a.** \$48 **b.** \$66.25 **c.** The bicycle in part (a); it will cost \$192, the bicycle in part (b) will cost \$198.75.

Extension (p. 183) 1. increase; 25% 3. decrease; 45% 5. decrease; 33% 7. 20.3 9. 35.2 11. 20% increase 13. 48.0 people per square mile

3.8 Skill Practice (pp. 187–188) 1. literal equation **3.** $x = \frac{c}{b-a}$; -2 **5.** x = bc - a; 9 **7.** x = a(c - b); 28 **9.** b should have been subtracted from both sides, not added; $ax = -b, x = -\frac{b}{a}$. **11.** y = 7 - 2x **13.** 4 - 3x = y **15.** $2 + \frac{6}{7}x = y$ **17.** $\frac{9}{5}x - 6 = y$ **19.** $y = \frac{1}{2}x + \frac{1}{3}$ **21.** $h = \frac{S-2B}{P}$ **25.** y = 18 - 5x**27.** $\ell = \frac{S}{\pi r} - r$; **13.03 cm 29.** Sample answer: You

want to find how long it will take to drive 150 miles if you drive at an average rate of 55 miles per hour.

3.8 Problem Solving (pp. 188-189) **33. a.** $x = \frac{C-25}{12}$ **b.** 10 nights; 13 nights; 15 nights **35.** Divide each side by the total bill, b, to get $\frac{a}{b} = p\%$.