EVALUATE EXPRESSIONS

FIND THE VALUE OF THE EXPRESSION

SOLVE EQUATIONS

FIND THE VALUE OF THE VARIABLE (x)

3.2 Solve Two-Step Equations

Goal • Solve two-step equations.

Your Notes

TO SOLVE EQUATIONS YOU ISOLATE X.

IDENTIFYING OPERATIONS FOR 2 STEP EQUATIONS

Identify the operations involved in the equation $3x + 7 = 19$.

FIRST ALWAYS SIMPLIFY BOTH SIDES

1. STEP 1 : UNDO ADD / SUBTRACTION
2. STEP 2 : UNDO MULT / DIVISION
3. YOU MUST ALWAYS CHECK BY SUBSTITUTING IN THE ORIGINAL EQUATION.

Example 1 *Solve a two-step equation*

Solve $3x + 7 = 19$.

Solution

When solving a two-step equation, apply the inverse operations in the reverse order of the order of operations.

$3x + 7 = 19$	Write original equation.
$-7 \quad -7$	Subtract 7 from each side.
$\frac{3x}{3} = \frac{12}{3}$	Simplify.
$x = 4$	Divide each side by 3.
	Simplify.

The solution is 4. CIRCLE IT.

CHECK

$3x + 7 = 19$	Write original equation.
$3(4) + 7 \stackrel{?}{=} 19$	Substitute 4 for x.
$12 + 7 \stackrel{?}{=} 19$	Multiply 3 by 4.
$19 = 19$ ✓	Simplify. Solution checks.

Your Notes

Checkpoint Solve the two-step equation. Check your solution.

1. $\frac{r}{4} - 12 = -5$

$+12 \quad +12$

$\frac{1}{4}\left(\frac{R}{4}\right) = 7 \cdot 4$

$R = 28$

C: $\frac{28}{4} - 12 = -5$

$7 - 12 = -5$

$-5 = -5$ ✓

2. $7k - 14 = 42$

$+14 \quad +14$

$\frac{7k}{7} = \frac{56}{7}$

$k = 8$

C: $7(8) - 14 = 42$

$42 = 42$ ✓

Show all steps

← MINIMUM WORK FOR Checks

Example 2 *Solve a two-step equation by combining like terms*

Solve $4a + 3a = 63$.

Solution

$4a + 3a = 63$ ← Write original equation.

Combine like terms. $4a + 3a = 7a$

$\frac{7a}{7} = \frac{63}{7}$

Divide each side by 7.

$a = 9$

Simplify.

The solution is $a = 9$.

ALWAYS SIMPLIFY BOTH SIDES FIRST

CHECK

$4a + 3a = 63$ Write original equation.

C: $4(9) + 3(9) \stackrel{?}{=} 63$ ← Check in orig EQ

$36 + 27 \stackrel{?}{=} 63$ ← START USE CALC FOR ARITHMETIC

$63 = 63$ ✓ ← Show EQUATION Checks

Checkpoint Solve the equation. Check your solution.

3. $5z + 4z = 36$

$\frac{9z}{9} = \frac{36}{9}$

$z = 4$

C: $5(4) + 4(4) = 36$

$36 = 36$ ✓

4. $5b - 2b = 9$

$\frac{3B}{3} = \frac{9}{3}$

$B = 3$

C: $5(3) - 2(3) = 9$

$15 - 6 = 9$

$9 = 9$ ✓

3.3 Solve Multi-Step Equations

Goal • Solve multi-step equations.

Your Notes

Example 1 *Solve an equation by combining like terms*

Solve $3t + 5t - 5 = 11$.

Solution

$8T - 5 = 11$

Write original equation.

Combine like terms.

$+5 \quad +5$

Add 5 to each side.

$8T = 16$

Simplify.

$\frac{8T}{8} = \frac{16}{8}$

Divide each side by 8.

$T = 2$

Simplify.

The solution is ___.

Check: $3(2) + 5(2) - 5 = 11$

$11 = 11$ ✓

SIMPLIFY

STEP I

ALWAYS SIMPLIFY BOTH SIDES

Example 2 *Solve an equation using the distributive property*

Solve $5a + 3(a + 2) = 22$.

$5a + 3a + 6 = 22$

Show All Steps

$8a + 6 = 22$

$-6 \quad -6$

$8a = 16$

$\frac{8a}{8} = \frac{16}{8}$

$a = 2$

C: $5(2) + 3(2+2) = 22$

$10 + 3(4) = 22$

$10 + 12 = 22$

$22 = 22$ ✓

Checkpoint Solve the equation. Check your solution.

1. $9d - 4d - 2 = 18$

$5D - 2 = 18$
$+2 \quad +2$
$\frac{5D}{5} = \frac{20}{5}$
$D = 4$

C: $9(4) - 4(4) - 2 = 18$
$36 - 16 - 2 = 18$
$18 = 18$ ✓

2. $2x + 7(x - 3) = 6$

$2x + 7x - 21 = 6$
$9x - 21 = 6$
$+21 \quad +21$
$\frac{9x}{9} = \frac{27}{9}$
$x = 3$

C: $2(3) + 7(3 - 3) = 6$
$6 = 6$ ✓

3. $40 = 2(10 + 4k) + 2k$

$40 = 20 + 8K + 2K$
$40 = 10K + 20$
$-20 \quad -20$
$\frac{20}{10} = \frac{10K}{10}$
$K = 2$

C: $40 = 2(10 + 4(2)) + 2(2)$
$40 = 2(18) + 4$
$40 = 40$ ✓

Example 3 *Multiply by a reciprocal to solve an equation*

Solve $\frac{3}{4}(a - 5) = 9$.

Solution

$\frac{4}{3}\cdot\frac{3}{4}(a - 5) = \frac{9}{1}\cdot\frac{4}{3}$ Write original equation.

Multiply each side by $\frac{4}{3}$.

Mental step → $1 \cdot (a - 5) = 36/3$

$a - 5 = 12$
$+5 \quad +5$
$a = 17$

C: $\frac{3}{4}(17 - 5) = 9$
$3/4(12) = 9$
$9 = 9$ ✓

2 WAYS TO SOLVE THIS PROBLEM

① DISTRIBUTE 3/4

② MULTIPLY BOTH SIDES BY THE RECIPROCAL

Checkpoint Solve the equation. Check your solution.

5. $\frac{1}{2}(4x - 2) = 7$

$2x - 1 = 7$
$+1 \quad +1$
$\frac{2x}{2} = \frac{8}{2}$
$x = 4$

C: $\frac{1}{2}(4 \cdot 4 - 2) = 7$
$\frac{1}{2}(16 - 2) = 7$
$\frac{1}{2}(14) = 7$
$7 = 7$ ✓

3.2 HW #'s 6–18 (EVEN)

6) $G = 8$

8) $Q = 1$

10) $W = 20$

12) $Z = -12$

14) $n = 21$

16) $P = 6$

18) $X = 6$

3.3 HW #'s 8–16 (EVEN), 19, 33, 38

8) $Z = -5$

10) $m = -7$

12) $Z = 2$

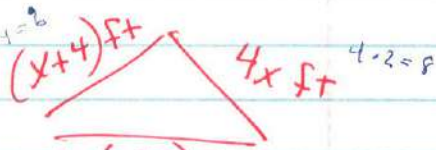
14) $m = 3$

16) $C = 5$

19) $D = 12$

33) KI

$P = 288$ inches $= 24$ ft



6 + 8 + 10 = 24 ft

$P = 24 = (x+4) + 4x + 10(x-1)$

$24 = x + 4 + 4x + 10x - 10$

$24 = 15x - 6$

$+6 \quad +6$

$\frac{30}{15} = \frac{15x}{15}$ $\quad x = 2$

The sides are 6 ft, 8 ft, 10 ft

38) KI: \$32.50 / ticket
plus \$3.30 / ticket
plus \$5.90 per order
Total spending = \$220.70

DEFINE VARIABLE:
$X =$ # tickets bought

DEFINE EQ:
$(\$32.50 + \$3.30)X + 5.90 = 220.70$

$X = 6$

BOUGHT 6 TICKETS

3.4 Solve Equations with Variables on Both Sides

Goal • Solve equations with variables on both sides.

EQUATIONS HAVE 3 TYPES OF SOLUTIONS

~~Your Notes~~

1. 1 SOLUTION $x = \#$
2. NO SOLUTION $x = \emptyset$
3. ALL REAL NUMBERS

VOCABULARY

Identity means that an EQUATION IS TRUE FOR ANY VALUE OF X.

SOLUTION → $x =$ all real numbers OR $x = \mathbb{R}$

Example 1 *Solve an equation with variables on both sides*

Solve $15 + 4a = 9a - 5$.

Solution

Collect variables on one side of the equation and constant terms on the other to solve equations with variables on both sides.

$15 + 4a = 9a - 5$ — Write original equation.

$-4a \quad -4a$ — Subtract $4A$ from each side.

$15 = 5A - 5$ — Simplify. (2 STEP EQUATION)

$+5 \quad +5$ — (1) Add 5 to each side.

$\frac{20}{5} = \frac{5A}{5}$ — Simplify.

$A = 4$ — (2) Divide each side by 5.

Simplify.

The solution is 4.

1. ALWAYS SIMPLIFY BOTH SIDES
2. GET THE VARIABLE ON ONE SIDE

CHECK — In original equation: Substitute 4 for a.

$15 + 4(\overset{a}{4}) \stackrel{?}{=} 9(\overset{a}{4}) - 5$

$15 + 16 \stackrel{?}{=} 36 - 5$ — Multiply.

$31 = 31$ ✓ — Solution checks.

Your Notes

Example 2 *Solve an equation with grouping symbols*

Solve $4t - 12 = 6(t + 3)$.

Solution

$4t - 12 = 6(t + 3)$ — Write original equation.

$4T - 12 = 6T + 18$ — Distributive property

$-4T \quad -4T$

$-12 = 2T + 18$ — Subtract $4T$ from each side.

$-18 \quad -18$

$-30 = 2T$ — Subtract 18 from each side.

$\frac{-30}{2} = \frac{2T}{2}$ — Divide each side by 2.

$T = -15$

C: $4(-15) - 12 = 6(-15 + 3)$

$-72 = -72$ ✓

Checkpoint Solve the equation. Check your solution.

1. $3b + 7 = 8b + 2$

$-3B \quad -3B$

$7 = 5B + 2$

$-2 \quad -2$

$\frac{5}{5} = \frac{5B}{5}$ $\quad B = 1$

C: $3(1) + 7 = 8(1) + 2$

$10 = 10$ ✓

2. $6d - 6 = \frac{3}{4}(4d + 8)$

$6D - 6 = 3D + 6$

$-3D \quad -3D$

$3D - 6 = 6$

$+6 \quad +6$

$\frac{3D}{3} = \frac{12}{3}$ $\quad D = 4$

C: $6(4) - 6 = \frac{3}{4}(4 \cdot 4 + 8)$

$24 - 6 = 3/4\,(24)$

$18 = 18$ ✓

Example 3 *Identify the number of solutions of an equation*

Solve the equation, if possible.

SPECIAL CASES

Check mentally but do not need to write it

a. $4x + 5 = 4(x + 5)$ — Original equation

$4x + 5 = 4x + 20$ — Distributive property

$-4x \quad -4x$

$5 \neq 20$ (F)

$x =$ NO SOLUTION or $x = \phi$

When the variable drops out AND THE NUMBERS DO NOT EQUAL THEN THERE IS NO SOLUTION.

b. $6x - 3 = 3(2x - 1)$ — Original equation

$6x - 3 = 6x - 3$ — Distributive property

$-6x \quad -6x$

$-3 = -3$ (T)

$x =$ ALL REAL NUMBERS

When the variable drops out and the numbers are EQUAL THEN THERE IS AN INFINITE NUMBER OF SOLUTIONS.

Check

$x = 0 \rightarrow -3 = -3$ ✓ — 0 IS A SOLUTION

$x = 1 \rightarrow 3 = 3$ ✓ — 1 " " "

$x = 2 \rightarrow 9 = 9$ ✓ — 2 " " "

$x = 3 \rightarrow 15 = 15$ ✓ — 3 " " "

$x = 4 \rightarrow 21 = 21$ ✓ — 4 " " "

Your Notes

ADD

15 $4x - 3 = 3(x - 1)$

$4x - 3 = 3x - 3$

$+3 \quad +3$

$4x = 3x$

$-3x \quad -3x$

$x = 0$

C: $4(0) - 3 = 3(0 - 1)$

$-3 = -3$ ✓

Checkpoint Solve the equation, if possible.

3. $\frac{1}{2}(4t - 6) = 2t$

$2T - 3 = 2T$

$-2T \quad -2T$

$-3 \neq 0$

T = NO SOLUTION

$2 \cdot \frac{1}{2}(4T - 6) = 2T \cdot 2$

$4T - 6 = 4T$

4. $10m - 4 = -2(2 - 5m)$

$10m - 4 = -4 + 10m$

$-10m \quad -10m$

$-4 = -4$ (T)

X = ALL REAL NUMBERS

BOOK ANSWER: IDENTITY

STEPS FOR SOLVING LINEAR EQUATIONS

Step 1 **Use the** distributive property **to remove any grouping symbols.**

Step 2 Simplify **the expression on each side of the equation.**

Step 3 **Use the properties of equality to collect the** variable **terms on one side of the equation and the** constant **terms on the other side of the equation.**

Step 4 **Use the properties of equality to solve for the** variable.

Step 5 **Check your** solution **in the original equation.**

3.4 HW PG 157 #'s 4 – 14 (E), 18 – 26 (E), 41, 46

4) $K = 1$
C: $2 = 2$ ✓

6) $m = 3$
C: $20 = 20$ ✓

8) $P = -6$

10) $H = 3$
C: $8 = 8$ ✓

12) $R = 5$
C: $84 = 84$ ✓

14) $n = 7$
C: $45 = 45$ ✓

18) W = NO SOLUTION

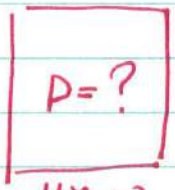
20) Z = NO SOLUTION

22) $X = -33$
C: $-656 = -656$ ✓

24) Y = ALL REAL NUMBERS

26) G = ALL REAL NUMBERS

46) KI



$4x - 2 = 3x + 7$
$-3x \quad -3x$
$x - 2 = 7$
$+2 \quad +2$
$x = 9$

$P = 4(34) = 136$

Perimeter = 136 UNITS

41) $14 - \frac{1}{5}(J - 10) = \frac{2}{5}(25 + J)$
$14 - \frac{1}{5}J + 2 = \frac{2}{5}J + 10$
$-\frac{1}{5}J + 16 = \frac{2}{5}J + 10$
$+\frac{1}{5}J \quad +\frac{1}{5}J$
$16 = \frac{3}{5}J + 10$
$-10 \quad -10$
$\frac{5}{3} \cdot 6 = \frac{3}{5}J \left(\frac{5}{3}\right)$
$30/3 = J$
$J = 10$

C: $14 - \frac{1}{5}(10 - 10) = \frac{2}{5}(25 + 10)$
$\frac{2}{5}(35)$
$14 = 14$ ✓

3.5 Write Ratios and Proportions

Goals • Find ratios and write and solve proportions.

Your Notes

VOCABULARY

Ratio The use of division to compare 2 QUANTITIES

Proportion 2 RATIOS THAT ARE EQUIVALENT. EXAMPLE → $\frac{1}{2} = \frac{20}{40}$

RATIOS

1. A ratio uses Division to compare two quantities.
2. The ratio of two quantities, a and b, where b is not equal to 0, can be written in three ways:

$\frac{a}{b}$ $a:b$ a to b

3. Each ratio is read "the ratio of a to b".
4. Ratios should be written in Simplest form. EXAMPLE → $\frac{40}{60} = \frac{2}{3}$

Example 1 *Write a ratio*

Cell Phone Use A person makes 6 long distance calls and 15 local calls in 1 month.

a. Find the ratio of long distance calls to local calls.

b. Find the ratio of long distance calls to all calls.

Solution

a. $\frac{\text{long distance calls}}{\text{local calls}} = \frac{6}{15} = \frac{2}{5}$

b. $\frac{\text{long distance calls}}{\text{all calls}} = \frac{6}{21} = \frac{2}{7}$

$21 = 6 + 15$

Your Notes

Checkpoint Shawn and Myra are selling tickets to their school's talent show. Shawn sold 36 tickets, and Myra sold 44 tickets. Find the specified ratio.

1. The number of tickets Shawn sold to the number of tickets Myra sold

$\frac{\text{SHAWN}}{\text{MYRA}} = \frac{36}{44} = \boxed{\frac{9}{11}}$

2. The number of tickets Myra sold to the number of tickets Shawn and Myra sold

$\frac{\text{MYRA}}{\text{TOTAL}} = \frac{44}{80} = \boxed{\frac{11}{20}}$

Example 2 *Solve a proportion*

Solve the proportion $\frac{y}{15} = \frac{3}{5}$.

Solution

$\frac{y}{15} = \frac{3}{5}$ **Write original proportion.**

Use the same methods for solving equations to solve proportions with a variable in the numerator.

CROSS MULTIPLY AND DIVIDE

$\frac{5Y}{5} = \frac{3 \cdot 15}{5}$

$\boxed{Y = 9}$

Checkpoint Solve the proportion. Check your solution.

3. $\frac{9}{4} = \frac{c}{28}$

$\frac{4C}{4} = \frac{9 \times 28}{4}$

$\boxed{C = 63}$

C: $9/4 = 63/28$

$2.25 = 2.25$ ✓

4. $\frac{a}{32} = \frac{7}{8}$

$\frac{8A}{8} = \frac{7 \cdot 32}{8}$

$\boxed{A = 28}$

C: $28/32 = 7/8$

$.875 = .875$ ✓

Your Notes

Example 3 *Solve a multi-step problem*

Swimming Pool A empty swimming pool is being filled with water. After 5 minutes the pool has 400 gallons of water. If the pool has a volume of 11,200 gallons, how long does it take to fill the empty pool?

Solution

Step 1 **Write** a proportion involving two ratios that compare the amount of water in the pool to the amount of time.

$$\frac{400}{5} = \frac{11{,}200}{x}$$ ← gallons / ← minutes

Ratio is gallons to MINUTES

Step 2 **Solve** the proportion.

$\frac{400x}{400} = \frac{5(11{,}200)}{400}$

$x = 140$

The pool is full after 140 minutes. OR 2 HOURS AND 20 MIN

Checkpoint **Complete the following exercise.**

Homework

5. An Olympic sized pool has a volume of 810,000 gallons. If it is filled at the same rate as the pool in Example 3, how long will it take to fill the pool?

Rate: $\frac{400 \text{ gallons}}{5 \text{ minutes}} = \frac{810{,}000 \text{ gal}}{M}$ ← M = # Minutes

$\frac{400M}{400} = \frac{5(810{,}000)}{400}$

$M = 10{,}125$ minutes

168.75 hrs

Key – 2014
Revised so No Calc needed

3.6 Solve Proportions Using Cross Products

Goal • Solve proportions using cross products.

Your Notes

VOCABULARY

Cross product

$$\frac{a}{b} = \frac{c}{d}$$

Cross Product: $a \cdot d = b \cdot c$

NOTE IF THE CROSS PRODUCTS ARE EQUAL THEN IT IS A TRUE PROPORTION.

CROSS PRODUCTS PROPERTY

Words The cross products of a proportion are EQUAL.

Example $\frac{5}{6} = \frac{10}{12}$ $\quad 6 \cdot 10 = 60$, $5 \cdot 12 = 60$ They are EQUAL

Algebra If $\frac{a}{b} = \frac{c}{d}$ where $b \neq 0$ and $d \neq 0$, then $ad = bc$.

Your Notes

Example 1 *Solve a proportion using cross products*

Solve the proportion $\frac{5}{y} = \frac{15}{75}$.

Solution

$\frac{5}{y} = \frac{15}{75}$ — Write original proportion.

$\frac{15y}{15} = \frac{1}{5} \cdot \frac{75}{15}$ — Cross products property

$y = 25$ — Simplify.

The solution is ____.

C: $\frac{5}{25} = \frac{15}{75}$ ← reduce fractions

$\frac{1}{5} = \frac{1}{5}$ ✓

STEP I

KI:

3T food with 16oz water

80oz to feed plants

Example 2 *Write and solve a proportion*

Plant Food To feed your plants, you need to mix 3 tablespoons of plant food with 16 ounces of water. If it takes 80 ounces of water to feed all of your plants, how many tablespoons of plant food are needed? ← DEFINE VARIABLE

STEP II

VARIABLE

x = # of T of plant food

↑ must have UNITS

Solution

Step 3 Write a proportion involving two ratios that compare the amount of plant food with the amount of water.

$\frac{3}{16} = \frac{x}{80}$ ← amount of plant food / ← amount of water

Step 4 Solve the proportion.

$\frac{16x}{16} = \frac{3 \cdot 80^{5}}{16_{1}}$ — Write proportion.

$x = 15$ — Cross product property / Simplify.

STEP 5 WRITE ANSWER IN A SENTENCE

You need 15 tablespoons of plant food for 80 ounces of water.

Your Notes

Checkpoint Solve the proportion. Check your solution.

1. $\frac{5}{n} = \frac{25}{45}$

$\frac{1}{5} \cdot 45 = \frac{25}{25} n$

$5 = n$ (n=9)

C: $\frac{5}{9} = \frac{25}{45}$ ÷5

$\frac{5}{9} = \frac{5}{9}$ ✓

2. $\frac{6}{b} = \frac{3}{b-2}$

$6(b-2) = 3b$

$6b - 12 = 3b$

$-6b \quad -6b$

$-12 = -3b$

$\frac{-12}{-3} = \frac{-3b}{-3}$ → (b=4)

C: $\frac{6}{4} = \frac{3}{4-2}$

$\frac{3}{2} = \frac{3}{2}$ ✓

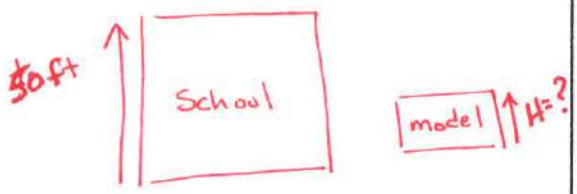
3. In Example 2, suppose it takes 120 ounces to feed all of the plants. How many tablespoons of plant food are needed?

$\frac{3}{16} = \frac{x}{120}$ → $\frac{16x}{16} = \frac{3(120)}{16}$

$x = \frac{360}{16} = 22.5$

Need 22.5 tablespoons of plant food

KI:



Scale factor: 1 ft = 75 ft

Variable

H = height of the model (ft)

Example 3 *Use a scale model*

Scale Model An architect creates a scale model of a school. The school is 50 feet high. The ratio of the model to the actual school is 1 foot to 75 feet. Estimate the height of the model.

Solution

Write and solve a proportion to find the height h of the scale model.

$\frac{H}{50} = \frac{1}{75}$ ← height of model (feet) ← actual height (feet) — Ratio (scale factor)

$\frac{75H}{75} = \frac{50}{75}$ Cross products property

$H = \frac{2}{3}$ Simplify.

The height of the scale model is $\frac{2}{3}$ foot, or 8 inches.

$\frac{2}{3} \cdot 12 = 8$

Checkpoint Complete the following exercise.

4. In Example 3, suppose the ratio of the model to the actual school is 1 foot to 100 feet. Estimate the height of the model.

$\frac{\text{MODEL}}{\text{ACTUAL}} = \frac{H}{50} = \frac{1}{100}$ ← scale factor

$\frac{100H}{100} = \frac{50}{100}$

H = 1/2 ft or 6 in

HEIGHT OF THE MODEL IS 1/2 ft or 6 in

N 3.6 HW Pg 171 #'s 13, 19-25, 33-34

(13) $\frac{11}{w} = \frac{33}{w+24}$

$11(w+24) = 33w$

$264 = 22w$

$w = 12$

C: $\frac{11}{12} = \frac{33}{12+24}$

$\frac{11}{12} = \frac{33}{36}$

$\frac{11}{12} = \frac{11}{12}$ ✓

(19) $\frac{7}{3} = \frac{2x+5}{x}$

$7x = 3(2x+5)$

$x = 15$

(20) $\frac{a}{9a-2} = \frac{1}{8}$

$8a = 9a - 2$

$-a = -2$

$a = 2$

(21) $\frac{24}{5z+4} = \frac{4}{z-1}$

$24(z-1) = 4(5z+4)$

$4z = 40$

$z = 10$

(22) $\frac{c-8}{-2} = \frac{11-4c}{11}$

$11(c-8) = -2(11-4c)$

$11c - 88 = -22 + 8c$

$3c = 66$

$c = 22$

(23) $\frac{k-8}{7+k} = \frac{-1}{5}$

$5(k-8) = -1(k+7)$

$5k - 40 = -k - 7$

$6k = 33$

$k = 5.5$

(24) $\frac{2}{-3} = \frac{4v+4}{2v+14}$

$2(2v+14) = -3(4v+4)$

$4v + 28 = -12v - 12$

$16v = -40$

$v = -2.5$

(25) $\frac{m+1}{4} = \frac{3m+6}{7}$

$7(m+1) = 4(3m+6)$

$7m + 7 = 12m + 24$

$-17 = 5m$

$m = -3.4$

C: $-.6 = -.6$ ✓

KS: Biscuits / Flour

(33) $\frac{12 \text{ BISCUITS}}{2 \text{ C FLOUR}} = \frac{30 \text{ BISCUITS}}{x \text{ C FLOUR}}$

X = # C flour

$x = 5$

Need 5 CUPS FLOUR

WP proportion ⟶ $\frac{12}{2} = \frac{30}{x}$

(34) $\frac{7.2 \text{ MIN}}{8 \text{ PHOTO'S}} = \frac{x \text{ MIN}}{20 \text{ PHOTO'S}}$

KS: $\frac{\text{MIN}}{\text{PHOTO}}$

X = # photos

$x = 18$

WILL TAKE 18 MIN. TO UPLOAD 20 PHOTO'S

WP Proportion $\frac{7.2}{8} = \frac{x}{20}$

N 3.6 x HW

EXTRA CREDIT

Pg 172 #'s 35-39

KI: $\frac{CM}{KM}$

D = distance in KM

35 $\frac{1\text{ cm}}{15\text{ Km}} = \frac{6\text{ cm}}{D}$ DISTANCE = 90 Km

36 $\frac{1\text{ cm}}{15\text{ Km}} = \frac{3.2\text{ cm}}{D}$ $D = 48$ Distance is 48 Km

37 $\frac{1\text{ cm}}{15\text{ Km}} = \frac{.5\text{ cm}}{D}$ $D = 7.5$ Distance is 7.5 Km

38 $\frac{1\text{ cm}}{15\text{ Km}} = \frac{4.7\text{ cm}}{D}$ $D = 70.5$ DISTANCE is 70.5 Km

39 KI: MODEL 1m : 25m

EMPIRE STATE is 443.2 m

What is the height of the model?

H = model height (m)

$$\frac{1}{25} = \frac{H}{443.2}$$

$$H = \frac{443.2 \times 1}{25}$$

$H = 17.728$

Model is 17.728 m tall

2 METHODS TO SOLVE PROPORTIONS

① PROPORTION METHOD
② WRITE AN EQUATION TO SOLVE

3.7 Solve Percent Problems

Goal • Solve percent problems.

Your Notes

SOLVING PERCENT PROBLEMS USING PROPORTIONS

METHOD I

You can represent "a is p percent of b" by using the proportion

$$\frac{a}{b} = \frac{p}{100} \quad \text{OR} \quad \frac{\text{IS}}{\text{OF}} = \frac{\%}{100}$$

where a is a part of the base b and $P/100$ or $p\%$, is the percent

METHOD I

Example 1 *Find a percent using a proportion*

What percent of 50 is 33?

Solution

Write a proportion when 50 is the base and 33 is part of the base.

$$\frac{33}{50} = \frac{P}{100} \leftarrow \text{Write proportion.}$$

$$\frac{50P}{50} = \frac{33 \cdot 100^{2}}{50_{1}}$$

$$P = 66\%$$

Solve

Cross products property

33 is 66% of 50.

Don't forget % sign

METHOD I: $\frac{IS}{OF} = \frac{\%}{100}$

Your Notes

Checkpoint Use a proportion to answer the question.

1. What percent of 80 is 28?

$\frac{P}{100} = \frac{28}{80} \Rightarrow 80P = 28 \cdot 100 \Rightarrow \frac{80P}{80} = \frac{2800}{80} \Rightarrow P = 35$

$P = 35\%$

2. What percent of 90 is 36?

$\frac{P}{100} = \frac{36}{90} \Rightarrow \frac{90P}{90} = \frac{3600}{90} \Rightarrow P = 40$

$P = 40\%$

METHOD II

THE PERCENT EQUATION

You can represent "a is p percent of b" by using the equation:

EQ: $a = p\% \cdot b$

where a is a part of the base b and $p\%$ is the percent.

TRANSLATE

"IS" means =

"OF" means multiply

Variables

P = percent

N = number

Example 2 *Find a percent using the percent equation*

What percent of 250 is 100?

① WORDS → TRANSLATE

$\frac{P}{100} \cdot 250 = 100$ Write percent equation.

② SOLVE IT

$\frac{P \cdot 250}{250} = \frac{100}{250}$

$P = \frac{100}{250} = \frac{2}{5}$ → decimals

$P = .4$ Write decimal as a percent.

$P = 40\%$

100 is 40% of 250

CHECK with proportion method

$\frac{P=40}{100} = \frac{100}{250}$

$40 \cdot 250 = 100 \cdot 100$ Cross products

$10,000 = 10,000$ ✓

$\frac{2}{5}$ divide $5\overline{)2}$

Your Notes

Example 3 *Find a part of a base using the percent equation*

WRITE

What number is 75% of 300?

Solution

$N = .75 \cdot 300$ Write percent equation.

$N = 225$

Change %'s to decimals!!

C: $\frac{225}{300} = \frac{75}{100}$

$225(100) = 300(75)$

$22,500 = 22,500$ ✓

225 is 75% of 300

Checkpoint Use the percent equation to answer the question.

Check w/ proportion

3. What percent of 75 is 60?

$\frac{P \cdot 75}{75} = \frac{60}{75}$ $\frac{12}{15} = \frac{4}{5}$

$P = .8$ → $P = 80\%$

C: $\frac{80}{100} = \frac{60}{75}$

$80(75) = 60(100)$

$6,000 = 6,000$ ✓

4. What number is 40% of 80?

$N = .4 \cdot 80$

$N = 32$

C: $\frac{32}{80} = \frac{40}{100}$

$3,200 = 3,200$ ✓

Example 4 *Find a base using the percent equation*

25 is 12.5% of what number?

Solution

Change 12.5% → .125

Write percent equation.

$25 = .125 \cdot N$

$N = 200$

25 is 12.5% of 200.

C: $\frac{12.5}{100} = \frac{25}{200}$

$2,500 = 2,500$ ✓

Your Notes

Checkpoint Use the percent equation to answer the question.

5. 60 is 25% of what number?

EQ → $\frac{60}{.25} = \frac{.25 \cdot N}{.25}$

$n = \frac{6000}{.25}$

Proportion → $\frac{60}{N} = \frac{25}{100}$

$\frac{25N}{25} = \frac{60 \cdot 100^{4}}{25_{1}}$

$N = 240$

6. 75 is 150% of what number?

EQ → $\frac{75}{1.50} = \frac{1.50 \cdot N}{1.50}$

$n = \frac{7500}{150}$

$n = \frac{750}{15} = \frac{150}{3}$

Proportion → $\frac{75}{N} = \frac{150}{100}$

$\frac{150N}{150} = \frac{75 \cdot 100^{4\,2}}{150_{6\,3}}$

$n = \frac{150}{3}$

$N = 50$

TYPES OF PERCENT EQUATIONS

Percent Problem	Example	Equation
(1) Find a percent.	What percent of 252 is 84?	P. 252 = 84
(2) Find part of a base.	What number is 30% of 90?	N = .30 · 90
(3) Find a base.	16 is 20% of what number?	16 = .20 · N

IS → =

OF → ×

Change %'s to decimals

Homework

EVEN'S ON NEXT PAGE

n3.7 HW Pg 179 #'s 1, 2, 3–17 (odd)

1. IN THE STATEMENT: 54 is 15% OF 360

ANSWER: Percent is 15.
Part (IS) is 54.
Base (OF) is 360.

$\frac{\text{IS (PART)}}{\text{OF (BASE)}} = \frac{P}{100}$

2. "28 is 35% OF 80" → Proportion: $\frac{28}{80} = \frac{35}{100}$

a Goes in Numerator; Percent is .35 (P); b Goes in denominator

3. $\frac{27}{75} = \frac{P}{100}$ $P \cdot 75 = 27$ $P = 36$ → 36%

5. $\frac{35}{100} \cdot \frac{N}{80}$ $N = .35 \cdot 80$ $N = 28$

#'s 3, 5: $\frac{\text{IS}}{\text{OF}} = \frac{P}{100}$

7. $\frac{81}{N} = \frac{54}{100}$ $81 = .54 \cdot N$ $N = 150$

#'s 9–17: % EQUATIONS

9. $P \cdot 80 = 56$ $P = .7$ $P = 70\%$ $\frac{56}{80} = \frac{P}{100}$

11. $P \cdot 153 = 9.18$ $P = .06$ $P = 6\%$ $\frac{P}{100} = \frac{9.18}{153}$

13. $N = 1.15 \cdot 60$ $N = 69$ $\frac{N}{60} = \frac{115}{100}$

15. $7 = .28 \cdot N$ $N = 25$ $\frac{7}{N} = \frac{28}{100}$

17. $41.8 = .44 \cdot N$ $N = 95$ $\frac{41.8}{N} = \frac{44}{100}$

3.7 (EVENS) Pg 179

	EQ	Proportion
(4)	$P \cdot 120 = 66$, $P = .55$	$\frac{66}{120} = \frac{P}{100}$, $P = 55\%$
(6)	$N = .60 \cdot 85$, $N = 51$	$\frac{60}{100} = \frac{N}{85}$
(8)	$42 = 2.00 \cdot N$, $N = 21$	$\frac{200}{100} = \frac{42}{N}$
(10)	$P \cdot 225 = 99$, $P = .44$	$\frac{P}{100} = \frac{99}{225}$, $P = 44\%$
(12)	$N = .18 \cdot 150$, $N = 27$	$\frac{18}{100} = \frac{N}{150}$
(14)	$N = .82 \cdot 215$, $N = 176.3$	$\frac{82}{100} = \frac{N}{215}$
(16)	$189 = .9 \cdot N$, $N = 210$	$\frac{90}{100} = \frac{189}{N}$

KEY

3.8 Rewrite Equations and Formulas

Goal • Write equations in function form and rewrite formulas.

Your Notes

FUNCTION FORM

↓

$y = mx + b$

↑ slope ↑ y-intercept

VOCABULARY

Function form IS THE SAME AS $y = mx + b$

* GIVEN AN EQUATION WITH X AND Y YOU ISOLATE Y ($y =$ ___)

Literal equation are EQUATION WITH 2 OR MORE VARIABLES (AKA Letters)

Example 1 *Rewrite an equation in function form*

Write $2x + 2y = 10$ in function form.

Solution

Solve the equation for y.

$2x + 2y = 10$ ← Write original equation. ISOLATE Y

$-2x \quad -2x$

$2y = -2x + 10$ Subtract $2x$ from each side.

$\frac{2y}{2} = \frac{-2x}{2} + \frac{10}{2}$ Divide each side by 2. (ALL TERMS DIVIDE BY 2)

$y = -x + 5$

The equation $y = -x + 5$ is written in function form.

Example 2 *Solve a literal equation*

Solve $a + by = c$ for a.

Solution

$a + by = c$ ← Write original equation. literal and solve for a

$-by \quad -by$

$a = c - by$ Subtract by from each side.

The solution is $a = c - by$.

Your Notes

KI

I = interest $'s

P = investment $'s

r = interest rate (% → decimal)

t = years

Formula: $I = PRT$

Example 3 *Solve and use a formula*

The interest *I* on an investment of *P* dollars at an interest rate *r* for *t* years is given by the formula $I = Prt$.

a. Solve the formula for the time *t*.

b. Use the rewritten formula to find the time it takes to earn $100 interest on $1000 at a rate of 5.0%.

Solution

Solve for t to get a New formula

a. $\frac{I}{Pr} = \frac{Prt}{Pr}$ **Write original formula.**

$\frac{I}{PR} = t$ $\quad t = \frac{I}{Pr}$ **Divide each side by** Pr.

b. Substitute $100 for *I*, $1000 for *P*, and 5% for *r* in the rewritten formula. (5% → .05)

$t = \frac{I}{Pr}$ **Write rewritten formula.**

$t = \frac{100}{1000 \cdot .05}$ **Substitute.** Simplify → $t = \frac{100}{50}$

$t = 2$ **Simplify.**

It will take 2 years to earn $100 in interest.

Checkpoint **Write the equation in function form.**

1. $2x + y = 5$

$-2x \quad -2x$

$y = -2x + 5$

2. $3 + 3y = 9 - 6x$

$-3 \quad -3$

$\frac{3y}{3} = \frac{6}{3} - \frac{6x}{3}$

$y = -2x + 2$

Checkpoint **Complete the following exercises.**

3. Solve $a + by = c$ for *b*.

$-a \quad -a$

$\frac{by}{y} = \frac{c-a}{y}$

$b = \frac{c-a}{y}$

4. In Example 3, solve the equation for *P*. Find the investment *P* if $I = \$400$, $r = 4\%$ (.04), and $t = 4$ years.

Variable Term is Constant Last

Homework

Write a new formula for P

$\frac{I}{rt} = \frac{Prt}{rt}$

$P = I$

Use the formula to answer?

$P = \frac{I}{rt}$

$P = \frac{400}{.04(4)1} = \frac{10000}{104} = \frac{2,500}{1}$

NAME
Date
Period

3.8 pg 187 #1-8, 11-13, 20-22

(1) LITERAL EQUATION (write sentence)

(2) To Solve $I = prt$ for t.

① divide each side by pr

② New formula $\boxed{t = \frac{I}{Pr}}$

(3) $ax = bx - c$

$-bx \quad -bx$

$ax - bx = -c$

$\frac{x(a-b)}{(a-b)} = \frac{-c}{(a-b)}$

$\boxed{x = \frac{-c}{a-b}}$

(4) $a(x+b) = c$

$ax + ab = c$

$-ab \quad -ab$

$\frac{ax}{a} = \frac{c-ab}{a}$

$\boxed{x = \frac{c+ab}{a}}$

Cross multiply

(5) $\frac{c}{1} = \frac{x+a}{b}$

$b \cdot c = x + a$

$-a \quad -a$

$\boxed{x = bc - a}$

(6) $\frac{x}{a} = \frac{b}{c}$

$\frac{ab}{c} = \frac{cx}{c}$

$\boxed{x = \frac{ab}{c}}$

(7) $\frac{x}{a} + b = c$

$-b \quad -b$

$\frac{x}{a} = (c-b)a$

$\boxed{x = a(c-b)}$

(8) $ax + b = cx - d$

$-cx \quad -cx$

$ax - cx + b = -d$

$-b \quad -b$

$ax - cx = -b - d$

$x(a-c) = -b-d$

$\frac{x(a-c)}{a-c} = \frac{-b-d}{a-c}$

$\boxed{x = \frac{-b-d}{a-c}}$ or $\boxed{x = \frac{b+d}{c-a}}$

(11) $y = -2x + 7$

(12) $5x + 4y = 10$

$-5x \quad -5x$

$4y = -5x + 10$

$\frac{4y}{4} = \frac{-5x}{4} + \frac{10}{4}$

$\boxed{y = -5/4\,x + 5/2}$

(13) $y = -3x + 4$

(20) $V = \ell w h$

$\frac{V}{\ell h} = \frac{\ell w h}{\ell h}$

$\boxed{w = \frac{V}{\ell h}}$

(21) $S = 2B + Ph$

$-2B \quad -2B$

$S - 2B = Ph$

$\frac{S-2B}{P} = \frac{Ph}{P}$

$\boxed{h = \frac{S-2B}{P}}$

(22) $\ell = 24f$

$\frac{\ell}{24} = \frac{24f}{24}$

$\boxed{f = \frac{\ell}{24}}$