### 9WP Notes

### **Vertical Motion Word Problems**

- I. Review Distance Models: The formula used is: D=R.T
  - D= distance

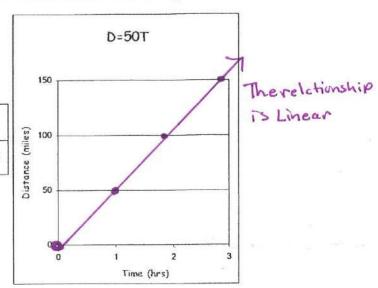
R= rate T= time

Rate is a constant and the relationship is LineAR

Example: A car travels at 50mph. How far will the car travel in 0, 1, 2, 3 hours? Complete the table and graph.

D = 50T 3 Time (hrs) Distance (miles) 100 150 50

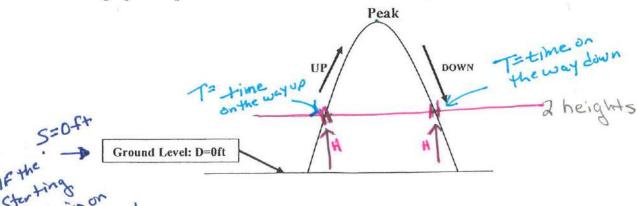
DISTANCE - FIND IT KI RATE - 50mph Time - 0, 1, 2, 3 hrs



- II. Vertical motion models describes the height of an object that is has no power to keep it self in the
  - Equation: H = -16T + VT + S (based on units in feet & seconds)
    - H= height of the object (in feet)
    - T= time the object has been in the air (in seconda)
    - · V= INITAL VERTICAL velocity (in ft/second)
    - S= INITIAL HEIGHT (in ft)

takes into account the effect of gravity but ignores other, less significant, factors such as air resistance.

O Vertical motion problems do NOT have a constant rate and the shape of the graph is a parabola.



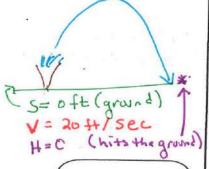
## 9.4

# Solve Polynomial Equations in Factored Form

Your Notes

KEYINFO

Looking for time (+)



The solution t = 0 means that before the water is sprayed, its height above the ground is 0 feet.

Example 4 Solve a multi-step problem

Fountain A fountain sprays water into the air with an initial vertical velocity of 20 feet per second. After how many seconds does it land on the ground?

Solution

Step 1 Write a model for the water's height above ground.

$$h = -16t^{2} + vt + s$$
Vertical motion model
$$h = -16t^{2} + 20t + 0 \quad v = 20 \quad \text{and } s = 0$$

$$h = -16t^{2} + 20 \quad \text{Simplify.}$$

Step 2 Substitute O+ for h. When the water lands, its height above the ground is O feet. Solve for t.

$$O = -16t^2 + 20T$$
Substitute O for h.
$$O = -4r(4T - s)$$
Factor right side.
$$-4T = 0 or 4T - s = 0$$
Zero-product property
$$T = 0 or 5/4$$
Solve for t.

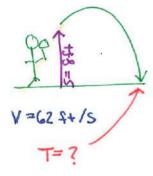
The water lands on the ground 1.25 seconds after it is sprayed.

# Sactor $ax^2 + bx + c$

**Goal** • Factor trinomials of the form  $ax^2 + bx + c$ .

#### **Your Notes**

Keyinfo



5=84 H= 0ff (when the bell hits the ground).

## Example 4 Write and solve a polynomial equation

Tennis An athlete hits a tennis ball at an initial height of 8 feet and with an initial vertical velocity of 62 feet per second.

- a. Write an equation that gives the height (in feet) of the ball as a function of the time (in seconds) since it left the racket.
- b. After how many seconds does the ball hit the ground?

#### Solution

a. Use the  $\sqrt{\text{ERTICAL MOTION Model}}$  to write an equation for the height h (in feet) of the ball.

$$h = -16t^2 + vt + s$$
 $h = -16t^2 + 62t + 8$ 
 $h = -16t^2 + 62t + 8$ 

b. To find the number of seconds that pass before the ball lands, find the value of t for which the height of the ball is \_o\_. Substitute \_o for h and solve the equation for t.

$$O = -16t^2 + 62t + 8$$
Substitute O for h.
$$O = -2(8T^2 - 31T - 4)$$
Factor out  $-2$ .
$$O = -2(8T + 1)(T - 4)$$
Factor the trinomial.
$$8T + 1 = 0 \text{ or } T - 4 = 0$$
Zero-product property
$$O = -4 + 8 = 0$$
Factor out  $-2$ .
$$O = -2(8T + 1)(T - 4)$$
Factor out  $-3$ .
$$O = -2(8T + 1)(T - 4)$$
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$$O = -3(8T + 1)(T - 4)$$
Factor out  $-3$ .

## 9.7

## **Factor Special Products**

Goal . Factor special products.

## Example 4 Solve a vertical motion problem

Falling Object A brick falls off of a building from a height of 144 feet. After how many seconds does the brick land on the ground?

#### Solution

Use the vertical motion model. The brick fell, so its initial vertical velocity is  $\bigcirc$ . Find the value of time t (in seconds) for which the height h (in feet) is  $\bigcirc$ .

$$h = -16T^{2} + \sqrt{1+8}$$

$$O = -16T^{2} + OT + 144$$

$$O = -16T^{2} + OT + 144$$

$$O = -16(T^{2} + 144)$$

$$O = -16(T^{2} - q)$$

$$O = -16(T^{2} + 144)$$

$$O = -16(T^{2} + 144)$$

$$O = -16(T^{2} + 144)$$

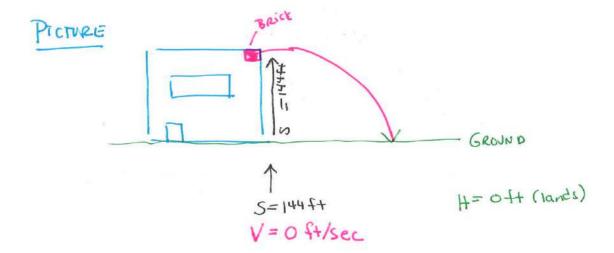
$$O = -16(T^{2} + OT + 144)$$

$$O = -16$$

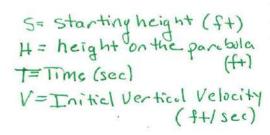
T-3=0 or T+3=0 Zero-product property

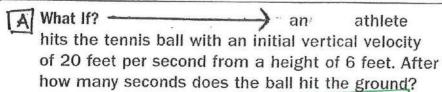
Solve for t.

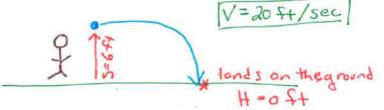
The brick lands on the ground 3seconds after it falls.

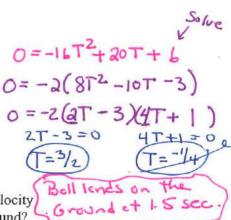


Memorize 
$$H = -16T^2 + VT + S$$
  
function  $h(t) = -16T^2 + VT + S$   
Checkpoint Complete the following exercise.



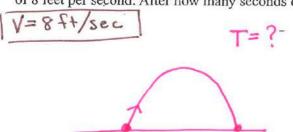






3 seconds

Jump Rope A child jumping rope leaves the ground at an initial vertical velocity of 8 feet per second. After how many seconds does the child land on the ground?



$$0 = -16T^{2} + 8T \pm 0^{2}$$

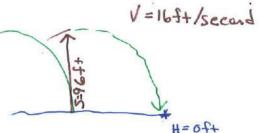
$$0 = -876T - 1)$$

$$-8T = 0$$

$$T = 0$$

$$T = 1/2$$
Child lands at . 5 seconds

Cliff Diving A cliff diver jumps from a ledge 96 feet above the ocean with an initial upward velocity of 16 feet per second. How long will it take until the diver enters the water?



Tennis Ball For a science experiment, you toss a tennis ball from a height of 32 feet with an initial upward velocity of 16 feet per second. How long will it take the tennis ball to reach the ground?

$$O = -16T^{2} + 16T + 32$$

$$O = -16(T^{2} + T^{2})$$

$$O = -16(T^{2} + T^{2})$$

$$O = -16(T^{2} + T^{2})$$

$$T = 2 \sec_{x} - 1 \sec_{x}$$
The bell hits the grand at 2 se conds