

All you need to know about...

Power Functions and Function Operations

Function Notation

The Symbol $f(x)$ is used in place of <u>y</u> .	Example: $y = 2x - 5 \Rightarrow f(x) = 2x - 5$
$f(x)$ is read as f of <u>x</u> .	This notation means the value of the function <u>f</u> at <u>x</u> .

Domain of a Function:

The values of x at which you are able to evaluate a function.

$$y = mx + b \quad y = ax^2 + bx + c$$

Linear, Quadratic, Polynomial Functions

D: All real #'s, \mathbb{R}

Power Functions

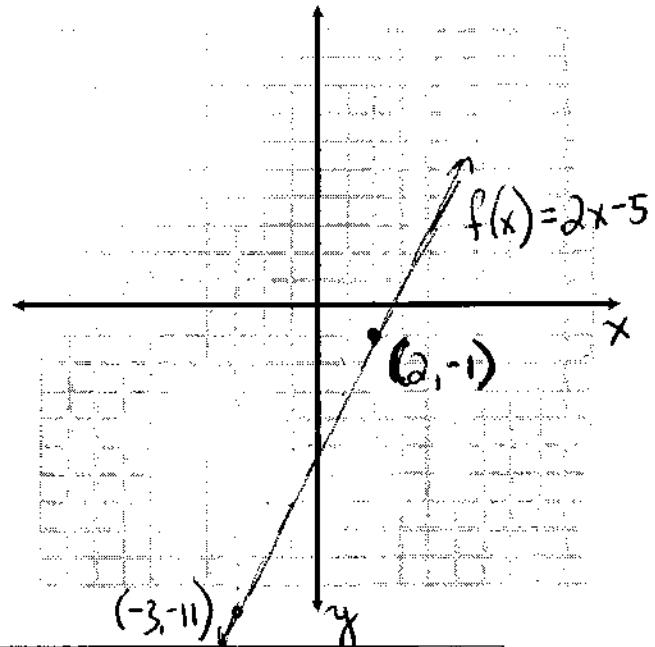
Even Roots $x^{1/2}$

Odd Roots $x^{1/3}$

D: All real #'s

nonnegative real #'s

$$x \geq 0$$



Evaluating a Function using Function Notation

Evaluate the function: $f(x) = 2x - 5$	Evaluate the function: $g(x) = x^2 + 3$
$f(2) = 2(2) - 5 \quad f(2) = -1$	$g(-1) = (-1)^2 + 3 \quad g(-1) = 4$
$f(-3) = 2(-3) - 5 \quad f(-3) = -11$	$g(4) = 4^2 + 3 \quad g(4) = 19$

Evaluate the function: $h(x) = 2x^{1/2}$	Evaluate the function: $j(x) = x^{1/3} - 5$
$h(9) = 2 \cdot 9^{1/2} \quad 2 \cdot 3 \quad h(9) = 6$	$j(-8) = (-8)^{1/3} - 5 \quad -2 - 5 \quad j(-8) = -7$
$h(-4) = 2 \cdot (-4)^{1/2}$ $2 \cdot \sqrt{-4}$	$j(1) = 1^{1/3} - 5 \quad 3 \sqrt[3]{1} - 5 \quad j(1) = -4$

No Real #

$$\frac{1}{-4} - 5$$

Types

Day 2

Operations with Functions

IR

OPERATION	Definition	Example: $f(x) = -x$, $g(x) = 2x + 1$ IR
Addition	$h(x) = f(x) + g(x)$	$h(x) = -x + 2x + 1$ $h(x) = x + 1 \quad D: \mathbb{R}$
Subtraction	$h(x) = f(x) - g(x)$	$h(x) = -x - (2x + 1)$ $= -x - 2x - 1$ $h(x) = -3x - 1 \quad D: \mathbb{R}$

Finding the Domain:

- The domain of $h(x)$ consists of the x -values that are in the domains of *both* $f(x)$ and $g(x)$.

Example 1

Adding Functions

Let $f(x) = 5x^{1/3}$ and $g(x) = 2x^{1/3}$ Find (a) the sum of the functions and (b) the domain of the sum.

Solution:

$$\begin{aligned} ① \quad f(x) + g(x) &= 5x^{1/3} + 2x^{1/3} \\ &= 7x^{1/3} \end{aligned}$$

$$\begin{aligned} ② \quad f(x) + g(x) &= 7x^{1/3} \\ &\quad D: \mathbb{R} \end{aligned}$$

Steps:

- ① Substitute
- ② Combine like radicals
- ③ Domain

Example 2

Subtracting Functions

Let $f(x) = 4x^{1/4}$ and $g(x) = 9x^{1/4} - 3$. Find (a) $f(x) - g(x)$ and (b) the domain of the difference.

Solution:

$$\begin{aligned} ① \quad f(x) - g(x) &= 4x^{1/4} - (9x^{1/4} - 3) \\ &= 4x^{1/4} - 9x^{1/4} + 3 \end{aligned}$$

$$f(x) - g(x) = -5x^{1/4} + 3$$

$$D: x \geq 0$$

Steps:

- ① Substitute. Don't forget $()$
- ② Dist the $-$
- ③ Combine like terms
- ④ Domain

More Operations with Functions

OPERATION	Definition	Example: $f(x) = -x$, $\boxed{g(x) = 2x + 1}$
Multiplication	$h(x) = f(x) \cdot g(x)$	$-x(2x+1)$ $-2x^2 - x$ D: $\boxed{\mathbb{R}}$
Division	$h(x) = \frac{f(x)}{g(x)}$	$\frac{-8}{2x+1}$ D: $x \neq -\frac{1}{2}$
Finding the Domain:		
1. The domain of $h(x)$ consists of the x -values that are in the domains of <i>both</i> $f(x)$ and $g(x)$. 2. The domain of a quotient does not include x -values for which $g(x) = 0$.		

Example 3

Multiplying Functions

Let $f(x) = 4x^{1/3}$ and $g(x) = x^{1/2} + 2$. Find (a) $f(x) \cdot g(x)$ and (b) the domain of the product.

Solution:

$$\begin{aligned} & 4\sqrt[3]{x} \cdot (x^{1/2} + 2) \\ & \boxed{4x^{5/6} + 8x^{1/3}} \quad D: \{x \mid x \geq 0\} \end{aligned}$$

Steps:

- ① subst.
- ② distribute
- ③ D:

Example 4

Dividing Functions

Let $f(x) = 4x^{1/3}$ and $g(x) = x^{1/2}$. Find (a) $\frac{f(x)}{g(x)}$ and (b) the domain of the quotient.

Solution:

$$\begin{aligned} & \frac{4x^{1/3}}{x^{1/2}} = 4x^{-1/6} \\ & = \frac{4}{x^{1/6}} \cdot x^{5/6} \\ & D: \{x \mid x > 0\} \quad \boxed{= \frac{4x^{5/6}}{x^{1/6}}} \end{aligned}$$

Steps:

- ① substitute
- ② divide
- ③ domain

Day 4

One Last Operation with Functions

OPERATION	Definition	Example: $f(x) = 3x + 2$, $\boxed{1}$ $g(x) = 2x$ $\boxed{1}$
Composition	$h(x) = f(g(x))$	$f(g(x)) = f(2x)$ $= 3(2x) + 2$ $6x + 2$ Domain: $\boxed{\mathbb{R}}$
$g(3) = 2(3)$ $= 6$	$f(g(3)) = f(6)$ $= 3 \cdot 6 + 2$ $18 + 2 = 20$	$g(f(x)) = g(3x + 2)$ $= 2(3x + 2)$ $= 6x + 4$ $\boxed{D: \mathbb{R}}$

Finding the Domain:

- The domain of $h(x)$ consists of the x -values that are in the domains of *both* $f(x)$ and $g(x)$.

Example 5

Composition of Functions

$$D: \mathbb{R}$$

$$D: x \geq 0$$

Let $f(x) = 9x^{2/3}$ and $g(x) = x^{1/2}$.

$$\text{Find: (a)} f(g(x)) = f(x^{1/2})$$

(b) the domain of $f(g(x))$.

$$f(g(x)) = f(x^{1/2}) = 9(x^{1/2})^{2/3} = 9x^{1/3}$$

$$D: x \geq 0$$

$$(c) g(g(x)) = g(x^{1/2})$$

$$= (x^{1/2})^{1/2} = x^{1/4}$$

$$D: x \geq 0$$

$$(d) g(f(8)) =$$

$$f(8) = 9 \cdot 8^{2/3} = 9 \cdot (\sqrt[3]{8})^2 = 9 \cdot 2^2 = 36$$

$$g(36) = 36^{1/2} = \sqrt{36} = 6$$

Example 6

Composition of Functions

Let $h(x) = x^2 + 3x$ and $g(x) = x - 2$. Find (a) $h(g(x))$ and (b) the domain of $h(g(x))$.

$$h(g(x)) = h(x-2)$$

$$= (x-2)^2 + 3(x-2)$$

$$D: \mathbb{R}$$

$$(x-2)^2 =$$

$$(x-2)(x-2)$$

$$FOIL$$

$$x^2 - 2x - 2x + 4$$

$$= x^2 - 4x + 4 + 3x - 6$$

$$= \boxed{x^2 - x - 2}$$