```
Examples:
 AP Statistics - 6.3B2
                                              P(X<2) = P(X=0) + P(X=1)
                                              P(X \le 2) = P(X = 0) + P(X = 1) + P(X = 2)
 Goal: Understanding Binomial RV's
                                              P(X>3) \leftrightarrow P(X\geq4)
                                              P(X \ge 3) = 1 - P(X \le 2)
                                                                       P(X>3) = 1-P(X \le 3)
I. Binomial Setting: CYU (page 385):
                                             > BINONIAL RV W/ n=10 p=4/52
          LETX = FOF ACES
                                                 YES - Success is AN ACE! Failure NOT
     B= BINARY - SUCCESS OR FAILURE
                                                YES - SAMPLE WITH REPLACEMENT ACE
     = INDEPENDENT
                                                YES - FIXED TRIALS -10
     N= FIXED NUMBER OF TRIALS
                                  OF SUCCESS YES - FIXED PROBABILITY
      S = FIXED PRORABILITY
   2. her Y= # OVER 6 f+ tall
                                            -> NOT BINGMIAL RU (NOT INDEPENDENT)
                                                FAILURE - UNDER 6 ft
              Success - Duce 6 ft
     1 = NOT IN DEPENDENT - SELECTING
                                             WITHOUT REPLACEMENT FOR A SMALL
             FIXED TRIALS - 3
                                                                                SAMPLE
                                        CHANGE PROM PERSON TO
      S= V PROBABILITY WILL NOT
   3. LET W= # OF 55 rolled -> NOT BINGMIAL RV(NOT FIXED PROB.
               SUCCESS - ROLLA 5
                                         FAILURE - NOT A
               INDEPENDENT SINCE
                                        ROLLING A DIE - 1 TRIAL
                                                                      POESNOT
              NUMBER TRIALS
                           PROBABILITY
                                              65108D DIE
                                              $ 510 ED DIE
11.
    Binomial Probabilities:
                                       Example: Rolling Doubles
    In many games involving dice, rolling doubles is desirable. Rolling doubles mean the outcomes of two dice are the
    same, such as 1&1 or 5&5. The probability of rolling doubles when rolling two dice is 6/36 = 1/6. Suppose that a
    game player rolls the dice 4 times, hoping to roll doubles.
     (a) What is the probability that all 4 rolls are not doubles?
         Define the RV: LET X = THE NUMBER OF DOUBLES IN 4 ROLLS OF 2 DICE.
           Have the Binomial Conditions been met?
                                            FAILURE - NOT DOUBLES
                V. Success-ROLL DOUBLES
                    DICES ARE INDEPENDENT - 1 ROLL DOES NUT AFFECT ANOTHER ROLL
            N - V FIXED TRIALS - 4
                    FIXED PROBABILITY =
         State the parameters of the Binomial Distribution X HAS A BINOMIAL DISTRIBUTION
                                                       with n=4 p=16
           Give the probability statement:
             P(NO DOUBLES) => P(X=0)
           How many ways can you roll doubles 0 times in 4 attempts?
               1 WAY - THE ONLY OUTCOME - FFFF
         Calculate the probability
              P(x=0) = P(F.F.F.F) 

Since independent, we can
MULTIPLY PROBABILITIES
                         = P(F) = 1-16=5/6
                         = (5/6)4
                P(x=0)=,482
```

Remember: Binomial Models are DISCRETE RV's.

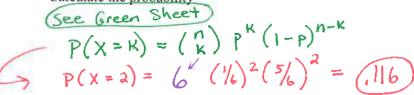
Example: Rolling Doubles (continued)

- (b) Find the probability that the player gets doubles once in four attempts.
 - P(X=1)Give the probability statement:
 - How many ways can you roll doubles 0 times in 4 attempts?

1ST TRY SEFE 4 POSSIBLE OUTCOMES TO
3RO TRY FESE ROLL DOVBLES ONCE IN 4 TRIES.
4TH TRY FEFS

- Calculate the probability THE LONG WAY: P(SFFF) = (1/6)(5/6)(5/6)(5/6) $P(FSFF) = (1/6)(5/6)^{3}$ P(SSFS) = (116) (5/6)3 P(FFFS) = (5/6)3(1/6) $P(x=1) = 4(1/6)(5/6)^3 = (.386)$
- (c) Find the probability that the player gets doubles twice in four attempts.
 - Give the probability statement: $P(X=\lambda)$
 - How many ways can you roll doubles 2 times in 4 attempts?

Calculate the probability



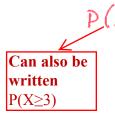
Secgreen Sheet TIP Check with:

binompdf (4, 1/6,2)

HOWTO FIND THE * OF COTLOMES

WITH CALCE

(d) Should the player be surprised if he gets doubles more than twice in four attempts? Justify your answer.



$$P(X > \lambda) = P(X = 3)$$

$$= {4 \choose 3} {1 \choose 6}^{3} {1 \choose 6}$$

$$= {4 \choose 4}^{3} {1 \choose 6}^{3} {1 \choose 6}$$

$$= P(x=3) + P(x=4) + (\frac{4}{4})(\frac{1}{6})^{4}(\frac{5}{6})^{6} + (\frac{4}{4})(\frac{1}{6})^{4}(\frac{5}{6})^{6} + (\frac{1}{6})^{3}(\frac{5}{6}) + (\frac{1}{6})^{4}(\frac{1}{6})^{4}(\frac{1}{6})^{6}$$

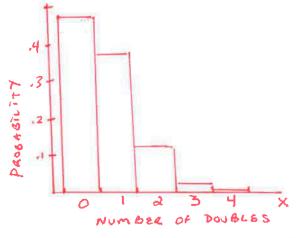
(e) Summarize the probability distribution of the Random Variable X in the following table Let X = number of doubles in 4 attempts, (X follows a binomial distribution with n = 4 and p = 1/6)

Value (x)	0	1 -	a	3	4	400
Probability	.482	.386	-116	.015	, 60 1	4 (L2)

(f) Create a histogram the probability distribution

Remember.

HISTOGRAM STAT PLOT XLIST --FREQ-LZ



Remember · Var Stat

(g) Find the Mean and Standard Deviation. Clearly show your work.
$$E(\vec{x}) = \mu_{x} = Z_{xi} p_{i} = 0(.482) + ... + 4(.00i) = ... + 4(.00i) =$$

Green Sheet Binomical Dist 6x= Jnp(1-p)

III. **Binomial Problem start to finish:** Example: Tastes as Good as the Real Thing?

The makers of a diet cola claim that its taste is indistinguishable from the full calorie version of the same cola. To investigate, an AP Statistics student named Emily prepared small samples of each type of soda in identical cups. Then, she had volunteers taste each cola in a random order and try to identify which was the diet cola and which was the regular cola. Overall, 23 of the 30 subjects made the correct identification.

If we assume that the volunteers really couldn't tell the difference, then each one was guessing with a 1/2 chance of being correct. Let X = the number of volunteers who correctly identify the colas.

(a) Explain why X is a binomial random variable.

INDEPENDENT? YES RANDOMLY ASSIGNED, ASSUMES VOLUNTEERS CANNOT TELL THE DIFFERENCE.

NUMBER? YES. THERE ARE 30 TRIALS

SUCCESS? YES. THE PROBABILITY OF GUESSING CORRECTLY IS This is A BINOMIAL DISTRIBUTION WITH n=30 and p=.5.7

(b) Find the mean and the standard deviation of X. Interpret each value in context. B (30.5

$$M_X = np = 30(.5) = (15)$$
 $C_X = \sqrt{np(1-p)} = \sqrt{30(12)(12)} = 2.74$

GX = \np(1-p) = \frac{30(12)(12)}{2.74} = 2.74 REPEATED MANY TIMES AND THE OF CORRECT GUESSES WOULD BE ABOUT 15

VART FROM IS BY ABOUT 2.74, ON AVERAGE.

(c) Of the 30 volunteers, 23 made correct identifications. Does this give convincing evidence that the volunteers can taste the difference between the diet and regular colas? $P(x > 23) = 1 - P(x \le 22) \leftarrow +he$ be nomial cdf ALWAYS Comes from the

= | - binomcdf(30, .5, 22) le ft

THERE IS A VERY SMALL CHANCE THAT THERE WOULD BE 23 OR MOLE CORRECT GUESSES IF THEY VOLUNTEERS COULDN'T TELL THE DIFFERENCE IN COLA'S. THEREFORE, WE HAVE CONVINCING EVIDENCE THAT THE VOLUNTEERS CAN TASTE THE DIFFERENCE.

IV. What you need to know about binomial and geometric RV's and their distributions

Remember: Binomial and Geometric Models are DISCRETE RV's. See page 1 for examples

	Binomial Setting (BINS)		Geometric Setting (BITS)
•	Binary? Each observation falls into one of two categories: success or failure.	•	Binary? Each observation falls into one of two categories: success or failure.
•	<u>Independent?</u> The <i>n</i> observations are all independent.	•	Independent? The <i>n</i> observations are all independent.
٠	Number? There is a fixed number n of observations.	•	<u>Trials</u> ? The variable of interest is "the number of trials required to obtain the 1 st success."
•	<u>Success</u> ? The probability of success, p, is the same for each observation.	•	Success? The probability of success, p, is the same for each observation.

<u>Independence</u> - knowing the result of one trial does not have any effect on the result of any other trial.

Binomial Distribution	Geometric Distribution			
 B(n,p) where n is the number of trials and p is the fixed probability 	G(p) where ○ p is the fixed probability			

Variables used in formulas below X=random variable n = number of trials	p = probability of success q = (1-p) = means "probability of failure" k = # of successes	
Binomial Probability To find the number of possible outcome:	Geometric Probability $P(X=k) = (1-p)^{k-1}p$ * where $k = number of trials until the first$	
$\left(\frac{n}{k}\right) = \frac{n!}{k!(n-k)!}$ Learn how to use calculator. No need to	success. Probability it takes more than n trials to see the	
memorize formula: $\binom{4}{2} = 4 n Cr 2 = 6$	1 st success: $P(x>k) = (1-p)^k$	
To find the probability for "k" successes: $P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$,.	
Binompdf(n,p,k) - "Point" density function	Geometpdf(p,k) - "Point" density function	
Remember to state distribution B(n,p) Binomcdf(n,p,k) - Cumulative density function	Remember to state distribution G(p) Geometcdf(p,k) — Cumulative density function	
Remember to state distribution B(n,p)	Remember to state distribution G(p)	
$\mu = np$	Don't memorize the formulas for the geometric	
$\sigma = \sqrt{np(1-p)}$	mean and standard deviation.	
Conditions: $np \ge 10$ and $n(1-p) \ge 10$ * Better approximation as n gets larger.	$\mu_{Y} = E(Y) = \frac{1}{n}$	
The approximation as it fore in Per-	P P	