| AP Statistics – 6.2B | Name: | | |
|----------------------------------|-------|--|--|
| Goal: Combining Random Variables | Date: | | |

I. Example #1: CYU (page 370):

Always state what your random variables are and distributions given:

| X = | # OF CARS SOLD | DURING | 1 ST HOUR | ON A | RANDUMLY SELECTED | 1 |
|-----|------------------|----------|-----------|------|-------------------|---|
| Y = | # OF CARS LEASET | | | | FRIDAY | |
| T = | TOTAL SOF CARS | SOLD OR | LEASED | | | |
| B = | MANAGERS BON | US = 500 | × + 300 Y | | // | |

1. Find and interpret μ_t

MT = MX + MY = 1.1 + 0.7 = (1.8) ON AVERAGE, THIS DEALARSHIP SELLS OR LEASES 1.8 CARS IN THE FIRST HOUR OF BUSINESS ON FRIDAYS

2. Calculate or showing work clearly

$$6_{T}^{2} = 6_{X}^{2} + 6_{Y}^{2} = (.943)^{2} + (.64)^{2} = 1.299$$

 $6_{T}^{2} = \sqrt{1.299} = 1.14$

3. Calculate μ_b and σ_b showing work clearly BONUS: $500/g_a le = \frac{300}{LEASED}$ $M_B = 500 M_X + 300 M_Y = 500(1.1) + 300(-7) = M_B = \frac{4760}{1.1}$ $G_B^2 = (500 G_X)^2 + (300 G_Y)^2 = [500 \cdot .943]^2 + [300 \cdot .64]^2 = 259, 176.25$ $G_B = \frac{1}{500} \cdot .09$

- II. Example #2: CYU (page 372):
 - Define random variables. D = X - Y

X, Y and B were Defined in Example 1

1. Find and interpret µd. $M_{D} = M_{X} - M_{Y} = 1.1 - 0.7 = 0.4$ ON AVERAGE, THIS DEALERSHIP SELLS O.4 CARS MORE THAN IT LEASES DURING THE FIRST HOUR OF BUSINESS ON FRIDAYS.

2. Calculate σ_d showing work clearly. How does this compare with Example #2

$$6_{D}^{2} = 6_{\chi}^{2} + 6_{\chi}^{2} = (.943)^{2} + (.64)^{2} = 1.244$$

 $6_{D} = \sqrt{1.299} = 1.14$ The variances are the same!

3. Calculate μ_b and σ_b showing work clearly.

$$M_{B} = 500 M_{X} - 300 M_{Y} = 500(1.1) - 300(.7) = ($340)$$

$$G_{B} = \sqrt{(500.943)^{2} + (300.64)^{2}} = [$509.09] * NOTICE THIS IS THE SAME AS THE ABOVE 3.$$

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Rules for Combining Random Variable (p365 and 367)

Independent Random Variable (p365)

IV. Example #3

Random variables. Given independent random variables with means and standard deviations as shown, find the mean and standard deviation of:

| a) $2Y + 20$ b) $3X$ | | Mean | SD | |
|-------------------------|---|------|----|--|
| c) $0.25X + Y$ | X | 80 | 12 | |
| d) $X = 5Y$ | Y | 12 | 3 | |
| e) $X_1 + X_2 + X_3$ | | | 2 | |

LINEAR TRANSFORMATION OF Y A E(21+20) = 2My+20 = 2(12)+20 = [11=44] SD(2Y+20) = 2GY = 2(3) = G=6Constant does Not change Ucricbility B LINEAR TRANSFORMATION OF Y E(3x) = 3. Mx = 3(80) = [1=240 SD (3x)= 3.6x = 3(12) = 6 = 36 C-E include both linear transformations and combining RVIS IC E (.25X+Y) = .25/1x + My = .25(80) + 12 = [M=32 VAR (.25X+Y) = (.25 G_X^2 + G_Y^2 = (.25.12)²+3² = 18 [G=4.24] $D = (X - 5Y) = M_X - 5M_Y = 80 - 5(12) = M = 20$ $VAR(X-5Y) = G_X^2 + (5G_Y)^2 = 12^2 + (5\cdot3)^2 = 369$ E E (x, +x2 + x3) = lex + lex + lex = 80+80+80 M=240 $V_{AR}(X_1 + X_2 + X_3) = G_X^2 + G_X^2 + G_X^2 = 12^2 + 12^2 + 12^2 = 432$ 6 = 20.78

V. Example & "Apples"

Suppose that the weights of a certain variety of apples have weights that are approximately Normally distributed with a mean of 9 ounces and a standard deviation of 1.5 ounces. If bags of apples are filled by randomly selecting 12 apples, what is the probability that the sum of the weights of the 12 apples is less than 100 ounces?

LET A = A RANDOMLY SELECTED APPLE. WITH
$$N(q_1, s)$$

T = TOTAL WEICHT A1 + A2 + A3 ... A 12^{*}
* THE APPLES ARE RANDOMLY SELECTED SO WE
HAVE 12 INDEPENDENT UARIABLES
FIND P(T<100) $N(log 5.2)$ $M_T = M_{A1} + M_{A2} ... + M_{A12}$
= $P(Z < \frac{100}{5.2})$ $M_T = M_{A1} + M_{A2} ... + M_{A12}$
= $P(Z < \frac{100}{5.2})$ $M_T = M_{A1} + M_{A2} ... + M_{A12}$
= $P(Z < \frac{100}{5.2})$ $M_T = M_{A1} + M_{A2} ... + M_{A12}$
= $P(Z < \frac{100}{5.2})$ $M_T = M_{A1} + M_{A2} ... + M_{A12}$
= $P(Z < \frac{100}{5.2})$ $G_T = 5.2 \text{ oz}$
Conclude: There is about a 6.2%
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Will have a total weight of less than 100 ounces
VI. Example 3. "Speed Dating"

Suppose that the height M of male speed daters follows a Normal distribution with a mean of 70 inches and a standard deviation of 3.5 inches and the height F of female speed daters follows a Normal distribution with a mean of 65 inches and a standard deviation of 3 inches. What is the probability that a randomly selected male speed dater is taller than the randomly selected female speed dater with whom he is paired?

m = height of mele speed dater - N(70, 3.5) F = height of femile speed dater - N(65, 3)Assume m and F are independent P(M > F) = P(M-F > 0) LeT: D = m - F MD = Mm - MF = 70 - 6S = 5in $G_{D}^{2} = G_{M}^{2} + G_{F}^{2} = \sqrt{3.5^{2} + 3^{2}} = (4.61 inches)$ $N(S_{1}^{4.61}) = \frac{8599}{0N} = \frac{2}{5} = -1.08$ P(7 = 3/-1.08) = .8599 P(7 = 3/-1.08) = .8599

TOR IN ABOUT 86% OF SPEED DATING COUPLES, THE MALE WILL BE TALLER THAN THE FEMALE.