(FREEN E(x) = Lx = Exi. Pi

VAR(x) = 62 = Z (xi - Mx)2 Pi

AP Statistics – 6.1	Name: KEY
Goal: Understanding Discrete and Continuous Random Variables	Date:

Warm Up CYU (page 349): Discrete RV's

- Always state what your random variable is: X = THE NUMBER OF CARS SOLD DURING THE 15H HOUR
- Calculate the mean of X by hand and interpret in context E(x) = Lex = 0(,3) +1(,4) +2(,2) +3(,1) = 0+,4+,4+,3 = 1,1 | E(x)=Zxipi * THE LONG-RUN AVERAGE, OVER MANY FRIDAY MORNINGS, WILL BE ABOUT I. I CARS SOLD.
- Calculate the standard deviation of X by hand and interpret in context $\sqrt{AR(x)} = 6\frac{2}{x} = \sum (x_1 \mu_x)^2 \cdot Pi = (0 1.1)^2 (.3) + (1 1.1)^2 (.4) + (2 1.1)^2 (.2)
 + (3 1.1)^2 (.1) = .363 + .004 + .162 + .361$ = 1.89SD(x) = Gx = 189 = (943)

* ON AVERAGE, THE NUMBER OF CARS SOLD ON A RANDOMLY SELECTED FRIDAY WILL DIFFER FROM THE MEAN(I.I) BY ABOUT . 94 CARS SOLD

II. Discrete Random Variables

Example: "National Hockey League's Goals"

In 2010, there were 1319 games played in the regular NHL season. Imagine selecting one of these games at random and then randomly selecting one of the two teams that played in the game. Define the random variable X= number of goals scored by a randomly selected team in a randomly selected game. The table below gives the probability distribution of X:

Goals:	0	1	2	3	4	5	6	7	8	9
Probability:	0.061	0.154	0.228	0.229	0.173	0.094	0.041	0.015	0.004	0.001

1st ALWAYS STATE THE RV -> X= # of goals sweed by a randomly selected fleam
in a randomly selected game.

- (a) Explain that the probability distribution for X is legitimate.
 - 1 ALL THE PROBABILITIES (Pi) IS A NUMBER BETWEEN O ANDI
 - 2 THE SUM OF THE PROBABILITIES IS 1 (ZPI=1)

(TREEN E(x) = Lx = Exipi VAR(x)= 62 = Z (xi - 1/x) Pi

KEY AP Statistics - 6.1 Name: Goal: Understanding Discrete and Continuous Random Variables Date:

I. Warm Up CYU (page 349): Discrete RV's

- Always state what your random variable is: X = THE NUMBER OF CARS SOLD DORING THE ISH HOUR OF BUSINESS ON A RANDONLY SELECTED FRIDAY
- Calculate the mean of X by hand and interpret in context E(x)= lex = 0(,3) +1(,4)+2(,2)+3(,1) = 0+,4+,4+,3= |1,1| E(x)= Zxipi * THE LONG-RUN AVERAGE, OVER MANY FRIDAY MORNINGS, WILL BE ABOUT I. I CARS SOLD.
- Calculate the standard deviation of X by hand and interpret in context $\sqrt{AR(x)} = 6\frac{2}{x} = \sum (x_1 \mu_x)^2 \cdot P = (0 1.1)^2 (.3) + (1 1.1)^2 (.4) + (2 1.1)^2 (.2) + (3 1.1)^2 (.1) = .363 + .004 + .162 + .361$ = 1.89SD(X) = 6x = 189 = (943)

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	Nous-constant			,				1		
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Example: "National Hockey League's Goals" (continued)

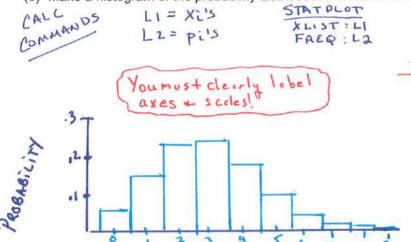
	Goals:	0	1	2	3	4	5	6	7	8	9
	Probability:	0.061	0.154	0.228	0.229	0.173	0.094	0.041	0.015	0.004	0.001
11=	A. A.		154	115/	161	197	1170	244	105	633	.009
CHA	XL. PL	0	-154	.456	-687	-647	-470	246	.105	,032	.009

ALWAYS DEFINE RV-> X = number of goals scored by a randomly selected team in a randomly selected game

(b) Make a histogram of the probability distribution. Describe the distribution in context.

STATPLOT

XLIST : LI



LI = Xi's

GOALS SCORED

- WINDOW: XMIN=-1 YMIN = -1 X MAX = 10 1MAX= . 3 x SCL = 1
- Remember Cuss AND BS · THE DISTRIBUTION OF GOALS SLORED IS SKEWED RIGHT MEANIN THE NUM BER OF GOALS SLORED IS RELATIVELY SMALL.
 - THE CENTER APPEARS TO BE 2 TO 3 GOALS. WITH THE SPREAD OF GUALS IS O TO 9 GUALS WITH THE MAJURITY OF GUALS BETWEEN 1 - 4 SLOREN
- (c) What is the probability that the number of goals scored by a randomly selected team in a randomly selected game is at least 6 ?

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CONTEXT THE PROBABILITY THAT A RANDOMLY SELECTED TEAM IN A RANDONLY SELECTED GAME WILL SCORE 6 OR MORE GOALS IS ABOUT 6%.

(d) Compute the mean of the random variable X by hand, clearly show work, and interpret this value in context.

CONTEXT: THE MEAN NUMBER OF GOALS FOR A RANDOMLY SELECTED TEAM IN A RANDOMLY SELECTED GAME IS 2.851, [THAT IS ... IF YOU WERE TO REPEAT THE RANDOM SAMPLING PROCESS OVER AND OVER AGAIN, THE MEAN HOF GOALS SCURED WOULD BE

ABOUT 2.851 IN THE LONG RUN.

Example: "National Hockey League's Goals" (continued) 11.

Probability: 0.061 0.154 0.228 0.229 0.173 0.094 0.041 0.015 0.004	
	0.001
17) 14 12 1101 535 115 735 1134 HOZ 258 106 -	0.38

ALWAYS DEFINE RV -> X = number of goals scored by a randomly selected team in a randomly selected game

(e) Compute the standard deviation of the random variable X by hand, clearly show work, and interpret this

VAR(X) = 6x = 2(x1-4x)2. Pi = (0-2.851)2.(.061) + ... + (9-2.851)2.(.001) must show this work

VAR(x) = 6x2 = Q.66) The verience

SD(x) = Gx = J2.66 = [1.63]

USE CALC FOR Mean + S. D of RV'S

1 VAR STAT (STAT) (CALC) LIST: L1 Xi's FREQ LIST: ILZ

Ru's are population

CONTEXT: ON AVERAGE, A RANDOMLY SELECTED TEAM'S NUMBER OF GOALS IN A RANDONLY SELECTED GAME WILL

DIFFER FROM THE MEAN (2.851) BY ABOUT 1.63 GOALS.

Technology Corner (page 348) 111.

Example: "Apgar Scores (example on page 343)"

APGAR SCORE OF A RANDOMLY a) Define the Random Variable → X= 1 HG SELECTED BABY.

- b) Explain that the probability distribution for X is legitimate.
 - Fill in table and place data in calculator lists (L1-L2)
 - Using 1-VarStats to determine if probability distribution for X is legitimate. EXPLAIN:

Xi	pi
0	,001
1	.006
2	, 00 7
3	1008
4	.012
5	1020
6	1038
7	.099
8	1319
9	.437
10	1053
Totals	1.00

X is alegitimate probability distribution because () all the individual probabilities are between

2 the sum of the probabilities is 1.

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3 | Page

(continued) III. Technology Corner: "Apgar Scores" Example

c) (step 2 from the "Technology Corner") Make a histogram of the probability distribution.

CALCOMMONS L1=xi'> La = Pi's



SETWINDOW

XMIN=-1 YMIN=-1 XMAX=11 YMAX= 5 X SCL= 1 YSCL= 1





Describe the distribution in context.

THE DISTRIBUTION OF APCAR SCORES IS HEAVILY SKEWED TO THE LEFT WITH AN EXPECTED SCORE AROUND 9 FOR A NORMAL BABY WITH MUST SCORES FALLING BETWEEN 7 and 9.

d) (step 3 from the "Technology Corner") Compute the mean of the random variable X, clearly show work, and interpret this value in context.

E(x) = 0(.001) + ... + 10(.053) = (8.128)

eace commends



CONTEXT:

THE MEAN APGAR SCORE OF A RANDOMLY SELECTED NEWBORN IS 8,128, THIS IS THE LONG-RUN AUERAGE AFGAR SCORE OF many, many, many randomly chosen babies.

e) (step 3 from the "Technology Corner") Compute the standard deviation of the random variable X, clearly show work, and interpret this value in context.

VAQ(x) = (0-8.128)2(.001)+...+ (10-8.128)2(.053) =

CONTEXT:

ON AVERAGE, A RANDOMLY SELECTED BABY'S APGAR SCORE WILL DIFFER FROM THE MEAN (8.128) BY ABOUT 1.4 UNITS,

IV	"DISCRETE Random Variable" VOCABULARY You need to understand these definitions for thi
	chapter. See my web site for these definitions. Here is space for you to take your own notes:

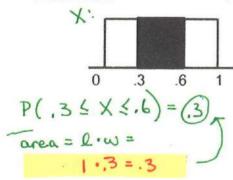
apter. See my web site for these definitions. There is space for you to take your own house.
. Random Variable (p313) TAKES NUM ERICAL VALUES THAT DESCRIBE
THE ORGANICE OF STATE AND PROCESS
* RU'S ARE DENOTED WITH CAPITAL LETTERS (X)
· Probability Distribution OF A RANGOM UARIABLE GIVES ITS POSSIBLE
VALUES AND THEIR PROBABILITIES. THIS IS A DISTRIBUTION
LIKE IN EARLIER CHAPTER. Remember to graph and
DESRIBE WITH "CUSS and BS.
Discrete Random Variable and Their Probability Distribution (p313)
DISCRETE RV'S (X) takes a fixed set of possible Values.
* GAPS MAY OCCUR
* PROBABILITY X all possible outcomes
DISTRIBUTION: Value X, to Xi
Probabilities PI to Pi
The much oblitics asset satisfic 2 as a viscous assets
The probabilities must satisfy 2 requirements 1)pi's are betwee\ o and 1
2) The som of probabilities is 1 2 pi = 1. To find the probability of an EVENT, add the pi's
for the Xi'S IN THE EVENT.
Expected Value of a Discrete Random Variable (p345)
The EXPECTED VALUE is the mean of a RV.
*
$M_X = E(x) = Z \times i Pi$
CONTEXT: IF YOU WERE TO REPEAT THE RANDOM SAMPLING !! PROCESS OVER AND OVER AGAIN, THE MEAN VALUE WOOLD !!
(rendom veriable have population means. NEVER USE X.
Standard Deviation of a Discrete Random Variable(p347)
To find the SD(x), you must first find the variance:
$G_{x}^{2} = VAR(x) = \sum (x_{i} - \mu_{x})^{2} P_{i}$
CONTEXT OF SD
ON AVERAGE, A RANDOMLY SELECTED PROCESS WILL
DIFFER FROM THE MEAN BY ABOUT

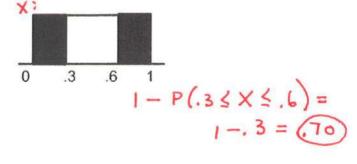
V. Continuous Random Variables

A. VOCABULARY (IMPORTANT)-- "CONTINUOUS Random Variable"

- Continuous Probability Distribution: described by the area under a density curve
- A CONTINUOUS probability distribution differs from a DISCRETE probability distribution in several ways:
 - The probability that a continuous random variable will assume an exact value is zero.
 - As a result, a continuous probability distribution cannot be expressed in tabular form.
 - Instead, an equation or formula is used to describe a continuous probability distribution.
 - We assign probabilities to **intervals** of outcomes rather than to individual outcomes.

EXAMPLE: Find the areas (shaded region) for the following density curves (*uniform distribution*).





SEE ABOVE NOTES. Your Notes: Continuous Random Variables (p350)

IN MANY CASES ... DISCRETE RANDOM VARIABLES aRISE FROM COUNTING

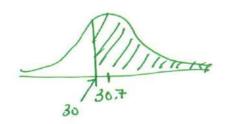
CONTINUOUS RU'S arise FROM M EASURING SOMETHING

P(-1 < x < 2) is really the same as P(-1 < x < 2) SINCE THERE IS NO AREA DIRECTLY ABOVE -1

Example: "Weights of Three-Year-Old Females"

The weights of three-year-old females closely follow a Normal distribution with a mean of μ = 30.7 pounds and a standard deviation of 3.6 pounds. Randomly choose one three-year-old female and call her weight X. Find the probability that the randomly selected three-year-old female weighs at least 30 pounds.

- RU: X = THE WEIGHT OF A RANDOMLY CHUSEN BYEARDLD FEMALE
- STATE DISTRIBUTION: N (30.7, 3.6) P(X >, 30)
- STATE PROBABILITY OF INTEREST;
- DRAW A PICTURE AND STAND ARDIZE THE WEIGHT TO FIND PROBABILITY



WILLNAT LEAST 30 Pands 6 | Page