AP Statistics – 6.1	Name: KEY
Goal: Understanding Discrete and Continuous Random Variables	Date:
I. Warm Up CYU (page 349): Discrete RV's	FIXED SET OF POSSIBLE VALUES (SECTIO)
 Calculate the mean of X by hand and interpret in context 	HOUR OF BUSINESS ANDOMLY SELECTED FRIDAY.
GREEN SHEET [CALC] E(x) = Ux = 0(.3) +	1(.4) + 2(2) + 3(.1) = +.4 +.3 = (1-1)
E(X) = \mathcal{M}_X = [CONTEXT] THE LONG-RUN ZXIPI = FRIDAY MURNINGS, W Calculate the standard deviation of X by hand and interpret in context	TILL BE ABOUT 1.1 Cars
GREEN SHEET (2-1.1)2	$(.2) + (3-1.1)^{2}(.1) = (.89)$
Z (X; -Mx)Pi CONTEXT) ON AVECAGE, THE	
DIFFER FROM THE MEAN	
II. <u>Discrete Random Variables</u> <u>Example</u> : "National I	Hockey League's Goals" SOLO.

In 2010, there were 1319 games played in the regular NHL season. Imagine selecting one of these games at random and then randomly selecting one of the two teams that played in the game. Define the random variable X = number of goals scored by a randomly selected team in a randomly selected game. The table below gives the probability distribution of X:

Goals:	0	1	2	3	4	5	6	7	8	9
Probability:	0.061	0.154	0.228	0.229	0.173	0.094	0.041	0.015	0.004	0.001

1ST ALWAYS STATE THE RV→ X= # of goals scored by a randomly selected Heam
in a randomly selected game.

(a) Explain that the probability distribution for X is legitimate.

① ALL THE PROBABILITIES (Pi) IS A NUMBER BETWEEN O AND 1.

② THE SUM OF THE PROBABILITIES IS 1 (Z Pi=1)

Revised 2015

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Example: "National Hockey League's Goals" (continued)

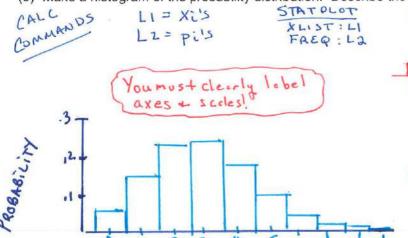
	Goals:	0	1	2	3	4	5	6	7	8	9
Ì	Probability:	0.061	0.154	0.228	0.229	0.173	0.094	0.041	0.015	0.004	0.001
E(A)=	xi- Pi	0	121,	.456	.687	.692	.470	.246	.105	.032	,009

ALWAYS DEFINE RV -> X = number of goals scored by a randomly selected team in a randomly selected game

(b) Make a histogram of the probability distribution. Describe the distribution in context.

STATPLOT

XLIST: LI



LI = Xi's

GOALS SCORED

WINDOW: XMIN=-1 X MAX = 10

Remember Cuss AND BS O THE DISTRIBUTION OF GOALS SLORED IS SKEWED RIGHT MEANING THE NUM BER OF GOALS GLORED IS RELATIVELY SMALL.

* THE CENTER APPEALS TO BE 2 TO 3 GOALS. WITH THE SPREAD OF GUALS 15 0 TO 1 GUALS WITH THE MAJURITY OF GUALS BETWEEN 1-4 SCORED.

(c) What is the probability that the number of goals scored by a randomly selected team in a randomly selected game is at least 6 ?

CONTEXT THE PROBABILITY THAT A RANDOMLY SELECTED TEAM IN A RANDOMLY SELECTED GAME WILL SCORE 6 OR MORE GOALS TS ABOUT 6%

(d) Compute the mean of the random variable X by hand, clearly show work, and interpret this value in context.

CONTEXT: THE MEAN NUMBER OF GOALS FUR A RANDOMY SELECTED TEAM IN A RANDOMLY SELECTED GAME IS 2.851. [THAT IS ... IF YOU WERE TO REPEAT THE RANDOM SAMPLING PROCESS OVER AND OVER AGAIN, THE MEAN HOF GOALS SCUEED WOULD BE ABOUT 2.851 IN THE LONG RUN. Revised 2015

II. Example: "National Hockey League's Goals" (continued)

	Goals:	0	1	2	3	4	5	6	7	8	9
	Probability:	0.061	0.154	0.228	0.229	0.173	0.094	0.041	0.015	0.004	0.001
VARLE)	(Xi-4) Pi	.496	.528	.165	.005	.228	,434	.407	. 258	.106	.038

ALWAYS DEFINE RV -> X = number of goals scored by a randomly selected team in a randomly selected game

(e) Compute the standard deviation of the random variable X by hand, clearly show work, and interpret this value in context

value in context. $VAR(x) = 6x^2 = \sum (x_1 - \mu_x)^2 \cdot p_1 = (0 - 2.851)^2 \cdot (.061) + ... + (9 - 2.851)^2 \cdot (.001)$

VAR(x) = 6x2 = Q.66) The variance

SD(x) = Gx = \[\lambda 2.66 = \left[1.63 \right]

USE CALC FOR Mean + S. D of RV'S

STAT CALC 1 VAR STAT

FREQ LIST: LZ Pis

Ru's are population

NOT Sample

X + Never say X!

Ex = 8.128 + EX

Sx = NOT a Sample s

(the above table has the numbers)

ONTEXT:

ON AVERAGE, A RANDOMLY

SELECTED TEAM'S NUMBER OF

GOALS IN A RANDOMLY

SELECTED GAME WILL

DIFFER FROM THE

MEAN (2.851) BY ABOUT 1.63 GOALS.

III. Technology Corner (page 348)

Example: "Apgar Scores (example on page 343)"

- a) Define the Random Variable -> X= THE APGAR SCORE OF A RANDOMLY SELECTED BABY.
- b) Explain that the probability distribution for X is legitimate.
 - Fill in table and place data in calculator lists (L1-L2)

Using 1-VarStats to determine if probability distribution for X is legitimate.

EXPLAIN:

See 808

Χį	pi
0	,001
1	.006
2	,007
3	8001
4	.012
5	1020
6	1038
7	,099
8	1319
9	.437
10	,053
Totals	1.00

X is alegitimate probability distribution because

(i) all the individual probabilities are between

2) the sum of the probabilities is 1.

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7x=1

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(continued) III. Technology Corner: "Apgar Scores" Example

c) (step 2 from the "Technology Corner") Make a histogram of the probability distribution.

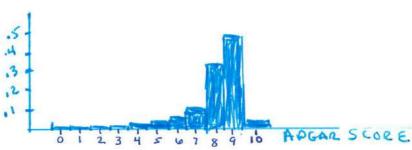
CALCAMOS

L1=xi'> La = Pi's

STATOLOF XLIST= L1

SETWINDOW FREQ = L2

XMIN=-1 YMIN=-1 XmAX=11 YMAX= 5 X SLL= 1 YSCL= 1



Describe the distribution in context.

THE DISTRIBUTION OF APGAR SCORES IS HEAVILY SKEWED TO THE LEFT WITH AN EXPECTED SCORE AROUND 9 FOR A NORMAL BABY WITH MUST SCURES FALLING BETWEEN 7 and 9.

d) (step 3 from the "Technology Corner") Compute the mean of the random variable X, clearly show work, and interpret this value in context.

E(x) = 0(.001) + ... + 10(.053) = (8.128

CALC Comminds

the wor

CONTEXT:

THE MEAN APGAR SCORE OF A RANDOMLY SELECTED NEWBORN IS 8,128, THIS IS THE LONG-RUN AUGRAGE APGAR SCORE OF MANY, MANY, MANY randomly chosen babies.

e) (step 3 from the "Technology Corner") Compute the standard deviation of the random variable X, clearly show work, and interpret this value in context.

VAR(x) = (0-8.128)2(.001)+... + (10-8.128)2(.053) =

SD (x) = \(VAR(x) = | 1.437 | +

this is

CONTEXT:

ON AVERAGE, A RANDOMLY SELECTED BABY'S APGAR SCURE WILL DIFFER FROM THE MEAN (8.128) BY ABOUT 1.4 UNITS,

IV	"DISCRETE Random Variable" VOCABULARY You need to understand these definitions for this
	chapter. See my web site for these definitions. Here is space for you to take your own notes:

. Random Variable (p313) TAKES NUM ERICAL VALUES THAT DESCRIBE
THE OUTCOMES OF SOME CHANCE PROCESS.
* RU'S ARE DENOTED WITH CAPITAL LETTERS (X)
. Probability Distribution OF A RANGOM UARIABLE GIVES ITS POSSIBLE
VALUES AND THEIR PROBABILITIES. THIS IS A DISTRIBUTION
LIKE IN EARLIER CHAPTER. Remember to graph and
DESRIBE WITH "CUSS and BS".
Discrete Random Variable and Their Probability Distribution (p313)
DISCRETE RV'S (X) takes a fixed set of possible
* GAPS MAY OCCUR
* PROBABILITY X all possible outcomes
DISTRIBUTION: Value X, to Xi
Probabilities PI to Pi
The probabilities must satisfy 2 requirements
1) Pi's are betweel o and 1
2) The som of probabilities is 1 2 pi = 1
2) The som of probabilities is 1 Z pi = 1 To find the probability of an EVENT, add the pi's
for the Xi'S IN THE EVENT.
Expected Value of a Discrete Random Variable (p345)
The EXPECTED VALUE is the mean of a RV.
X
$M_{x} = E(x) = Z \times i Pi$
X
CONTEXT: IF YOU WERE TO REPEAT THE RANDOM SAMPLING !! PROCESS OVER AND OVER AGAIN, THE MEAN VALUE WOUld NO!! (random variable have population means. NEVER USE X.
(random variable have population means. NEVER USE X.
Standard Deviation of a Discrete Random Variable(p347)
To find the SD(x), you must first find the variance:
$G_{x}^{2} = VAR(x) = \sum (Xi - \mu_{x})^{2} Pi$
CONTEXT OF SD
ON AVERAGE, A RANDOMLY SELECTED PROCESS WILL
DIFFER FROM THE MEAN BY ABOUT
* The formulas are on Your AP GREEN SHEET

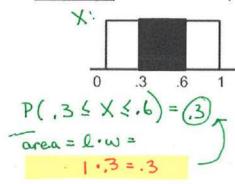
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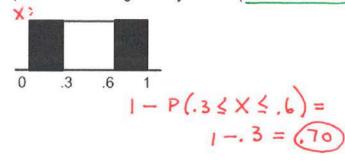
V. Continuous Random Variables

A. VOCABULARY (IMPORTANT) -- "CONTINUOUS Random Variable"

- Continuous Probability Distribution: described by the area under a density curve
- A <u>CONTINUOUS</u> probability distribution differs from a <u>DISCRETE</u> probability distribution in several ways:
 - 1. The probability that a continuous random variable will assume an exact value is zero.
 - 2. As a result, a continuous probability distribution cannot be expressed in tabular form.
 - 3. Instead, an equation or formula is used to describe a continuous probability distribution.
 - 4. We assign probabilities to **intervals** of outcomes rather than to individual outcomes.

EXAMPLE: Find the areas (shaded region) for the following density curves (uniform distribution).





Continuous Random Variables (p350) SEE ABOUE NOTES. Your Notes:

IN MANY CASES ... DISCRETE RANDOM VARIABLES aRISE FROM COUNTING Something

CONTINUOUS RU'S arise From MEASURING SOMETHING

NOTE: P(-1 < x < 2) is really the same as P(-1 < X < 2) SINCE THERE IS NO AREA DIRECTLY ABOVE -1 OR 2

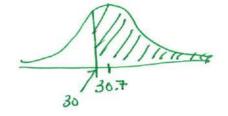
Example: "Weights of Three-Year-Old Females"

The weights of three-year-old females closely follow a Normal distribution with a mean of μ = 30.7 pounds and a standard deviation of 3.6 pounds. Randomly choose one three-year-old female and call her weight X. Find the probability that the randomly selected three-year-old female weighs at least 30 pounds.

- X = THE WEIGHT OF A RANDOMLY CHUSEN BYEAROLD FEMALE 3 MITS (1) Ru :

- STATE DISTRIBUTION: N (30.7, 3.6)

 STATE PROBABILITY OF INTEREST: P(X>,30)
- DRAW A PICTURE AND STAND ARDIZE THE WEIGHT TO FIND PROBABILITY



(5) CONCLUDE : THERE IS ABOUT A 58% CHANCE THAT THE RANDOMLY SELECTED 3 YEAR OLD FEMALE WILL AT LEAST 30 painds 6 | Page