| AP Statistics - 5.3 (part 2)                      | Name:          |  |  |
|---|----------------|--|--|
| Conditional Probability and Independence Activity | Date: 2018 KEY |  |  |

#### I. Disjoint vs. Independence

THINK ABOUT IT?: Can 2 mutually exclusive events ever be independent?

Why?

A MUTUALLY. EXCLUSIVE EVENTS

CAN NEVER BE INDEA EPENDENT.

HOW OUT COMES IN COMMON. IF ONE

FUENT OCCURS, THE OTHER EVENT

IS GUARANTEED NOT TO OCCUR

#### II. Conditional Probability Formula

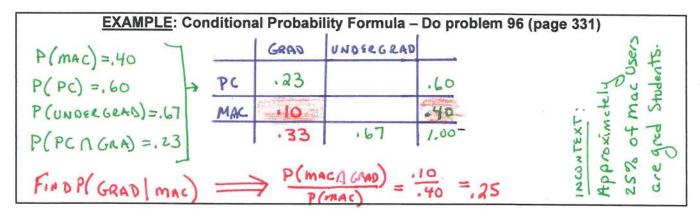
## <u>DEFINITION:</u> Conditional Probability Formula (p324)

Use the General Multiplication Rule: P(A ∩ B)= P(A)• P(B|A) to find this formula:

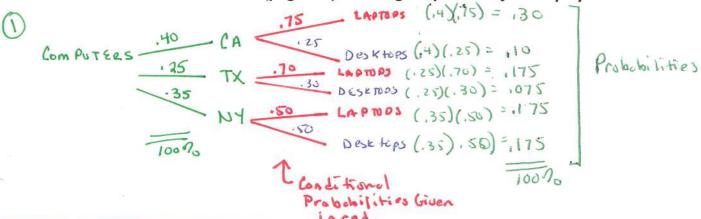
P(A) P(A)

P(BIA) = P(ANB) P(A)

Look at your green AP sheet and find this formula. Hence, you do not need to memorize the general multiplication rule. Why? No-USE YOUR ALGEBRA SKILLS



#### III. Review Tree Problems - CYU (page 321): Finding the probability of a laptops



Probability that the computer Ts a laptup = P(Laptup) = .30+.175 +.175 = .65

IN LONG HAND!

P(LAPTUP) = P(LAPTUP () A) + P(LAPTUP () TX) + P(LAPTUP () NY)

For men, binge drinking is defined as having five or more drinks in a row, and for women as having four or more drinks in a row. (The difference is because of the average difference in weight.) According to a study by the Harvard School of Public Health (H. Wechsler, G. W. Dowdall, A. Davenport, and W. DeJong, "Binge Drinking on Campus: Results of a National Study"), 44% of college students engage in binge drinking, 37% drink moderately, and 19% abstain entirely. Another study, published in the American Journal of Health Behavior, finds that among binge P(mob) = . 37 drinkers aged 21 to 34, 17% have been involved in an alcohol-related automobile accident, while among non-bingers of the same age, only 9% have been involved in such accidents. These are alcohol related accidents-

Given P(BINGE) = 44 P(ABSTAIN) = .19 P(ACC BINGE) = 17

What's the probability that a randomly selected college student will be a P(Acc | MOD) = .09 binge drinker who has had an alcohol-related car accident? P/ACC ABSTAIN = 0

1) Draw the tree diagram and answer the question. Show your work.

PLACE +AQ)=,44(.17) = .075 P(40)=82 P(BINGE+NO) =44 (.83) = ,365 Q (ma) = 09 = P(MOD + Acc) = 137 (.09) = 1033 DRINKING P(MOD + NO) =, 37 (.91) = 337 P(ABSTAIN)=19 P(NO) = 1.0 . P(ABSTANN + NO) = 119 (1) = . 190 CONDITIONAL THESE ALE PROBABLLITIES MARGINAL PROBABLITIES

| be  | easy<br>toble | to   | was ld<br>create<br>uprefe | a)    |
|-----|---------------|------|----------------------------|-------|
|     | BINGE         | GoM  | ABSTAIN                    | 1     |
| ACL | ,তাऽ          | .633 | ٥                          | ,108  |
| NO  | ,365          | ,337 | .190                       | . 892 |
|     | . 44          | .37  | .190                       | 1.00  |

To aswer all these

- What is the probability an accident given a binge drinker? PLACE BINGE)
  - 3) What is the probability an accident given the student drinks moderately? 09
- 4) What is the probability an accident given the student abstains from drinking? 0
- 5) What is the probability of binge drinker? (. 4 4

COME

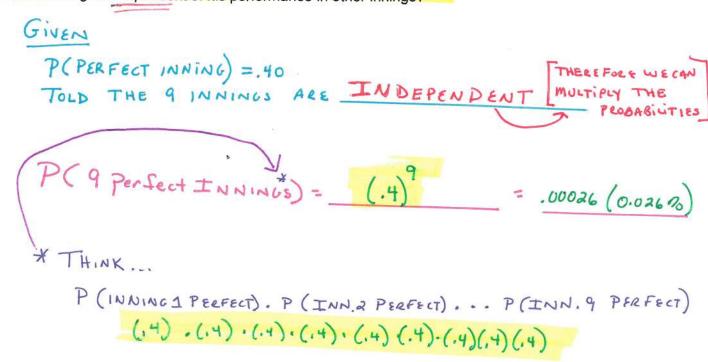
directly

6) What is the probability of having an accident?

- 7) What is the probability of not having an accident? p (NOT ACCIDENT) = 1-.11 (~89%)
- 8) What is the probability of binge drinking and having an accident? N 7.5% 9) What is the probability a student has an accident is a binge drinker?
- P(BINGE | ACCIDENT) = P(BINGE | ACCIDENT) = .0748

(N693

V. "Independence: A Special Multiplication Rule" [TIP reference page 321] EXAMPLE: Perfect Games
In baseball, a perfect game is when a pitcher doesn't allow any hitters to reach base in all nine innings.
Historically, pitchers throw a perfect inning—an inning where no hitters reach base—about 40% of the time. So, to throw a perfect game, a pitcher needs to have nine perfect innings in a row. Problem: What is the probability that a pitcher throws nine perfect innings in a row, assuming the pitcher's performance in an inning is independent of his performance in other innings?



VI. Finding the probability of "at least one" [TIP reference page 322] Example: First Trimester Screen

The First Trimester Screen is a non-invasive test given during the first trimester of pregnancy to
determine if there are specific chromosomal abnormalities in the fetus. According to a study published in
the New England Journal of Medicine in November 2005, approximately 5% of normal pregnancies will
receive a positive result. Among 100 women with normal pregnancies, what is the probability that there
will be at least one false positive?

GIVEN

P(NOrmal pregnancy) = .05

IT IS REASONABLE THAT THE WOMEN'S TESTS ARE INDEASONENT.

P(FALSE POSITIVE) = .05

P(ATLEAST 1 POSITIVE TEST OUT OF 100 WOMEN) =

I - P(NO POSITIVE RESULTS FOR 100 WOMEN) =

[HINK | 1- (.95) = 1-.0059 = 1.9941

CONCLUDE: THERE IS OVER A 99 % PROBABILITY THAT AT LEAST 1 OF THE 100 WOMEN WITH NORMAL PREGNANCY WILL RECEIVE A FALSE POSITIVE TEST FOR DEFECT.

# VII. Compare using trees and tables [TIP reference page 326] EXAMPLE: False Positives & Drug Testing

Many employers require prospective employees to take a drug test. A positive result on this test indicates that the prospective employee uses illegal drugs. However, not all people who test positive actually use drugs. Suppose that 4% of prospective employees use drugs, the false positive rate is 5% and the false negative rate is 10%.

# PROBLEM: What % OF PEOPLE WHO TEST POSITIVE A CTUALLY USE ILLEGAL DRUGS?

## GIVEN INFO

OPT

| SON A USE Z | Test Result  | PROBABILITIES:                    |
|-------------|--|-----------------------------------|
| TREET       | .90 +  | (.04) (90) = ,036                 |
| PRUSPECTIV  |  | (10) (10) = (004)                 |
| EMPLOYE     | DRICS 195 + (FALSE POSITIVE)                       | (.96)(.os) = ,048                 |
|             | //3 -  | (.96) (.95) = -912                |
| P(Took D    | RUGS   Positive TEST) = P(TOOK DEUGS AND POSITIVE) | 1.000<br>- 036<br>1036+,048 - 036 |

There is about 43% OF THE PROSPECTIVE = .429
EMPLOYEES WHO TEST POSITIVE POSITIVELY ACTUALLY TOOK DRUGS

TABLE :

| TEST     | PosiTive NEGATIVE |    | GATIVE  | MULTIPLY BY 1000 |     |          |          |       |
|----------|-------------------|----|---------|------------------|-----|----------|----------|-------|
| DRUGS    | .90               | 36 | .10     | NEGATIVE H       | .04 | 40       |          |       |
| NO DRUCS | FALSE POFITY      | 48 | .95 912 | .96 9            | 960 | P(b1+) = | 36 = 479 |       |
|          | ४न                |    | 4       | 916              |     | 1.00     | , 62     | 84 11 |