

Basic Algebra Review

Name: Key

Period: _____

Before diving in to problem solving with physical applications, let's review the necessary elements of algebra that you will need in this course.

Show all your work!!!

1. $2x+6=0$

$$\begin{array}{r} -6 \quad -6 \\ \hline 2x = -6 \\ \hline x = -3 \end{array}$$

2. $x-6=4$

$$\begin{array}{r} +6 \quad +6 \\ \hline x = 10 \end{array}$$

3. $y+8=12$

$$\begin{array}{r} -8 \quad -8 \\ \hline y = 4 \end{array}$$

4. $3y+1=16$

$$\begin{array}{r} -1 \quad -1 \\ \hline 3y = 15 \\ \hline y = 5 \end{array}$$

5. $6y=24$

$$\begin{array}{r} \div 6 \quad \div 6 \\ \hline y = 4 \end{array}$$

6. $\frac{y}{8} = 2$

$$y = 16$$

7. $\frac{z}{12} = 1$

$$z = 12$$

8. $\frac{10}{x} = 5$

$$\begin{array}{r} 10 \\ 5 = x \\ \hline x = 2 \end{array}$$

★ if x in denominator, you can switch with what is on other side of "="

9. $\frac{39}{x} = 3$

$$\begin{array}{r} 39 \\ 3 = x \\ \hline 13 = x \end{array}$$

switch!

if not, then long way:

- ① ~~$\frac{39}{x} = 3$~~
- ② $\frac{39}{3} = \frac{39}{3}$
- ③ $x = 13$

10. $x^2 = 16$

$$x = 4$$

$$11. x^2 = 16 + 9$$

$$\sqrt{x^2} = \sqrt{25}$$

$$\boxed{x = 5}$$

$$12. x^2 + 5 = 41$$

$$x = 5$$

$$\sqrt{x^2} = \sqrt{36}$$

$$\boxed{x = 6}$$

$$13. \frac{x^2}{4} = 4$$

$$\sqrt{16} = \sqrt{x^2}$$

$$\boxed{x = 4}$$

$$14. \frac{x^2}{9} = 27$$

$$\sqrt{x^2} = \sqrt{81}$$

$$\boxed{x = 9}$$

$$15. \frac{40}{x^2} = 10$$

* can switch b/c
x in denominator
(even x^2 !)

$$\frac{40}{10} = x^2$$

$$\sqrt{4} = \sqrt{x^2}$$

$$\boxed{x = 2}$$

$$16. \frac{27}{x^2} = 3$$

* switch!

$$\frac{27}{3} = x^2$$

$$9 = x^2$$

$$\boxed{x = 3}$$

$$17. 10 = 4 + 3x$$

$$-4$$

$$\frac{6}{3} = \frac{3x}{3}$$

$$\boxed{2 = x}$$

$$18. 8 = \frac{1}{2}x^2$$

2 options

double both sides

$$2 \cdot 8 = \frac{1}{2}x^2(2)$$

$$\sqrt{16} = \sqrt{x^2}$$

$$\boxed{4 = x}$$

divide by $\frac{1}{2}$

$$\frac{8}{\frac{1}{2}} = \frac{\frac{1}{2}x^2}{\frac{1}{2}}$$

$$\sqrt{16} = \sqrt{x^2}$$

$$\boxed{4 = x}$$

$$19. 18 = \frac{1}{2}x^2 \cdot 2$$

$$\sqrt{36} = \sqrt{x^2}$$

$$\boxed{6 = x}$$

$$20. 32 = \frac{1}{2}y(4^2)$$

do first

$$32 = (\frac{1}{2}y)(16)$$

$$\frac{32}{8} = \frac{8y}{8}$$

$$\boxed{4 = y}$$

$$21. z^2 = 3^2 + (2)(8)$$

$$z^2 = 9 + 16$$

$$\sqrt{z^2} = \sqrt{25}$$

$$\boxed{z = 5}$$

$$22. 12^2 = x^2 + 23$$

$$144 = x^2 + 23$$

$$-23$$

$$\sqrt{121} = \sqrt{x^2}$$

$$\boxed{x = 11}$$