

ROBBINSVILLE PUBLIC SCHOOLS

OFFICE OF CURRICULUM AND INSTRUCTION

Mathematics Department

PreCalculus Honors

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Course Philosophy

The New Jersey Core Curriculum Content Standards for Mathematics set a lofty goal for the mathematics curriculum when they state “all of our children, as well as our state and our nation, will be better served by higher expectations, by curricula that go far beyond basic skills and include a variety of mathematical models, and by programs which devote a greater percentage of instructional time to problem-solving learning.” The *Common Core Standards* seek to narrow the focus and foster a coherent progression of skills and concepts across grade levels. In addition, the *Common Core Standards* require both mastery of conceptual understanding and procedural fluency. We seek to adopt these practices and share the nation’s goal to enrich mathematics education.

It is our belief that the content of a mathematics course is brought to life for the student when it involves the student in investigating real-world applications using inductive and deductive reasoning while working cooperatively with others and communicating mathematically. This is reinforced by the use of technology and the use of real world data. In order to be competitive in today’s global, information-based economy, students’ mathematics experience must go beyond computation so that they are able to solve real problems, reason effectively, make logical connections, and think mathematically.

The Principles and Standards for School Mathematics published by the National Council of Teachers of Mathematics is a guiding document in the development and articulation of mathematics programs in Robbinsville. A central theme of this document is connections. According to *Principles and Standards*, “Students develop a much richer understanding of mathematics and its applications when they can view the same phenomena from multiple mathematical perspectives. One way to have students see mathematics in this way is to use instructional materials that are intentionally designed to weave together different content strands. Another means of achieving content integration is to make sure that courses oriented toward any particular content area (such as algebra or geometry) contain many integrative problems—problems that draw on a variety of aspects of mathematics, that are solvable using a variety of methods, and that students can access in different ways.” (NCTM)

Through engagement in mathematics learning outlined in this curriculum, the students of Robbinsville Public Schools will acquire the mathematical skills, understandings and reasoning to be successful citizens of the world.

Course Description

Pre-Calculus Honors

Grade: 10-12

5 Credits Year

Prerequisite(s): Algebra II Honors

Students intending to study mathematical and scientific related fields during their college experience should elect Pre-Calculus Honors. Functions (trigonometric, exponential, logarithmic, circular, linear, polynomial, rational), inverse functions, identities, equations (trigonometric, polar, linear, and quadratic), Cartesian and polar graphing, solutions of triangles and application problems will be studied. This course is designed to prepare students to take Calculus.

Core and Supplemental Instructional Materials

Core Materials	Supplemental Materials
<ul style="list-style-type: none"> Textbook 	<ul style="list-style-type: none"> Graphing websites (geogebra.com, desmos.com, etc.) Graphing calculator Online Resources Guided Notes Mimeo

Social Emotional Learning Connections

Below are the five core SEL Competencies as outlined by CASEL, and examples of how each may be addressed within this curriculum

Self-awareness: The ability to accurately recognize one’s emotions and thoughts and their influence on behavior. This includes accurately assessing one’s strengths and limitations and possessing a well-grounded sense of confidence and optimism.

Example 1: Students will discuss “what went well” at the end of class to assess their own understanding.

Example 2: Students will analyze their own errors and determine *why* they made a mistake so they can determine their level of understanding, strengths, and areas that need improvement in the unit.

Self-management: The ability to regulate one’s emotions, thoughts, and behaviors effectively in different situations. This includes managing stress, controlling impulses, motivating oneself, and setting and working toward achieving personal and academic goals.

Example 1: Students will have projects that will require steps and checkpoints. Completing the steps on time and remaining on task will require both self-motivation and regulation.

Example 2: Students will be given ample time in class to complete independent and group work. They must manage their time appropriately in order to keep up with the pace of the class.

Social awareness: The ability to take the perspective of and empathize with others from diverse backgrounds and cultures, to understand social and ethical norms for behavior, and to recognize family, school, and community resources and supports.

Example 1: Students will research other cultures and how different traditions and ways of life contribute to disease spread or population growth

Example 2: Students will learn about each other's diverse backgrounds and where to go at school and in the community if they need support.

Relationship skills: The ability to establish and maintain healthy and rewarding relationships with diverse individuals and groups. This includes communicating clearly, listening actively, cooperating, resisting inappropriate social pressure, negotiating conflict constructively, and seeking and offering help when needed.

Example 1: Instruct students how to effectively communicate with the teacher when conflicts arise. For example, if there is a conflict with academics and extracurricular activities, they will learn to be proactive and discuss how to resolve the conflict with the teacher.

Example 2: Students will work side by side with one another in order to discover theorems and solve problems

Responsible decision-making: The ability to make constructive and respectful choices about personal behavior and social interactions based on consideration of ethical standards, safety concerns, social norms, the realistic evaluation of consequences of various actions, and the well-being of self and others.

Example 1: Instruct students to embrace mistakes and not to criticize others when taking risks with new material

Example 2: Teach students that every action, whether intentional or not, has consequences, and that they should be mindful of what they say and how they act around others

Integration of 21st Century Themes and Skills

Educational Technology

Standards(8.1.12.A.2, 8.1.12.A.5, 8.1.12.C.1, 8.1.12.F.1)

- **8.1.12.A.2 Select and use applications effectively and productively.** Produce and edit a multi-page digital document for a commercial or professional audience and present it to peers and/or professionals in that related area for review.
- **8.1.12.A.5 Select and use applications effectively and productively.** Create a report from a relational database consisting of at least two tables, describe the process, and explain the report results.
 - Example: Students can electronically submit a slide presentation on a research topic of their choosing and present it to their peers and teachers. They must include at least two tables and three graphs in their presentation and use them to help explain their results.
- **8.1.12.C.1 Contribute to project teams to produce original works or solve problems** Develop an innovative solution to a real world problem or issue in collaboration with peers and experts, and present ideas for feedback through social media or in an online community
 - Example: Students discuss how disease can spread and how exponential growth is found in a real world setting. Students will research ways to reduce rates of infection and present ideas to the class.
- **8.1.12.F.1 Plan and manage activities to develop a solution or complete a project.** Evaluate the strengths and limitations of emerging technologies and their impact on educational, career, personal and/or social needs.
 - Example: Students can use online graphing tools to explore trigonometric, exponential, and logarithmic graphs. They can use these resources to transform parent functions and draw conclusions about the graphs and trends.

Career Ready Practices

Standards: (CRP1, CRP2, CRP4, CRP8, CRP11)

CRP1. Act as a responsible and contributing citizen and employee Career-ready individuals understand the obligations and responsibilities of being a member of a community, and they demonstrate this understanding every day through their interactions with others. They are conscientious of the impacts of their decisions on others and the environment around them. They think about the near-term and long-term consequences of their actions and seek to act in ways that contribute to the betterment of their teams, families, community and workplace. They are reliable and consistent in going beyond the minimum expectation and in participating in activities that serve the greater good.

Example: Students will demonstrate the responsibilities associated with being a member of a community when engaging collaboratively during sharing in pairs/trios, and participating in whole group discussions. Examples may include jigsaw and fishbowl activities.

CRP2. Apply appropriate academic and technical skills.

Example: Students will demonstrate the skills learned in PreCalculus when engaging collaboratively during sharing in pairs/trios and participating in whole group discussions. Examples may include jigsaw and fishbowl activities, as well as projects and formal assessments.

CRP4. Communicate clearly and effectively and with reason. Communication is a key factor in PreCalculus. Students are aware that their words and techniques they use to convey their thoughts are crucial to audience understanding.

Example: Students will demonstrate clear and effective communication through written and oral assignments and assessments.

CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.

Example: Students will demonstrate critical thinking as they determine the best methods to solve free response and multiple choice problems.

CRP11. Use technology to enhance productivity.

Example: Students will use technology to enhance productivity on a regular basis as they use graphing calculators and other graphing software to complete calculus problems.

Robbinsville Ready 21st Century Skill Integration

The following skills will be embedded throughout the curriculum and instruction of this course.

Collaborative Team Member: Robbinsville students will learn more by working together than in isolation. As educational theorist Lev Vygotsky advocated, learning is a social process. Many workplaces today encourage employees to work in teams to solicit diverse perspectives, brainstorm new ideas and/or products, and solve problems. Further, collaboration fosters interpersonal relationships, self-management skills, cooperation, and a sense of collective responsibility. Collaborative team members are able to work with diverse groups of people who hold a variety of perspectives.

Effective Communicator: Robbinsville students must be able to clearly articulate their ideas orally, in writing, and across various media in order to successfully connect to the world around them. As the world becomes increasingly globalized, communication is more than just sharing one's ideas. Effective communicators are able to communicate their convictions, actively listen and analyze others' work to identify perspective and/or potential bias.

Emotionally Intelligent Learner: Robbinsville students who are emotionally intelligent learn to be empathetic, demonstrate integrity and ethical behavior, are kind, are self-aware, willing to change, and practice self-care. They are better able to cope with the demands of the 21st century digital society and workplace because they are reliable, responsible, form stable and healthy relationships, and seek to grow personally and professionally. Emotionally intelligent people are able to manage their emotions, work effectively on teams and are leaders who can grow and help to develop others.

Informed and Involved Citizen: Robbinsville students need to be digital citizens who are civically and globally aware. The concept of what it means to be "literate" has evolved along with 21st century technological and cultural shifts. Our progressive vision of literacy entails having our students explore real world problems in the classroom. Informed and involved citizens are able to safely and accurately communicate with people all around the world and are financially, environmentally and informationally literate.

Innovative Thinker: Robbinsville students must encompass innovative thinking skills in order to be successful lifelong learners in the 21st century world. As stated by Karl Fisch and Scott McLeod in the short film Shift Happens, "We are currently preparing students for jobs that don't yet exist . . . using technologies that haven't been invented . . . in order to solve problems we don't even know are problems yet." Innovative thinkers are able to think analytically, solve problems critically, creatively engage in curiosity and tinkering, and demonstrate originality.

Resilient and Self-Directed Learner: Robbinsville students need to take risks and ultimately make independent and informed decisions in an ever-changing world. Author of *Life, the Truth, and Being Free*, Steve Maraboli stated, “Life doesn’t get easier or more forgiving, we get stronger and more resilient.” Self-directed scholars of the 21st century are able to set goals, initiate resolutions by seeking creative approaches, and adjust their thinking in light of difficult situations. Resilient students are able to take risks without fear of failure and overcome setbacks by utilizing experiences to confront new challenges. Resilient and self directed scholars will consistently embrace opportunities to initiate solutions and overcome obstacles.

Robbinsville Public Schools
Scope, Sequence, Pacing and Assessment

PreCalculus Honors

Unit Title	Unit Understandings and Goals	Recommended Duration/ Pacing	Assessments			
			Formative	Summative	Common Benchmark Assessments (mid-course and end of course <u>only</u>)	Alternative Assessments (projects, etc. when appropriate)
Unit 1: Functions and Their Graphs	<ul style="list-style-type: none"> The domain of a function impacts the properties of functions when they are manipulated. Relations and functions can be represented algebraically, numerically, and graphically. All graphical properties of functions can be established with algebraic work. The properties of functions and function operations are used to model and analyze real-world applications and quantitative relationships. 	6 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

Unit 2: Polynomials, Quadratics, and Rational Functions	<ul style="list-style-type: none"> There is a direct relationship between the graphs of polynomial and rational functions in terms of algebraically solving their equations when equal to zero. Technology allows us to approximate solutions easily, whereas solving for solutions algebraic gives us exact answers. We need to know when the difference between the two is relevant in a problem. 	7 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge
Unit 3: Exponential and Logarithmic Functions	<ul style="list-style-type: none"> Data that multiplies by a constant factor increases and decreases rapidly over time is represented by an exponential equation All exponential and logarithmic functions can be written in either exponential or logarithmic form Predictions for population, carbon dating, compound interest, and cooling are all examples of how exponential and logarithmic models are used to interpret real world data 	8 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

			Chapter Test			
Unit 4: Trigonometric Functions	<ul style="list-style-type: none"> Periodic behavior is behavior that repeats over intervals of equal length. The measure of an angle is the input for two important functions called sine and cosine. You can translate periodic functions in the same way that you translate other functions. Sine, cosine, and tangent have reciprocals. 	6 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge
Unit 5: Analytic Trigonometry	<ul style="list-style-type: none"> Given the relationships between the six basic trigonometric functions, it is possible to simplify the trigonometric expressions, making it easier to work with for mathematical application. Mathematics is a study of patterns, and the goal of algebra and trigonometry is to simplify complex patterns into easy forms that are more manageable. Trigonometric identities are just an extension of this basic mathematical skill. 	7 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

			Chapter Test			
Unit 6: Additional Topics in Trigonometry: Law of Sines/Law of Cosines	<ul style="list-style-type: none"> Trigonometry goes beyond the right triangle. Sides and angles of all triangles can be found, providing solutions to real-world problems. 	4 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge
Unit 7: Additional Topics in Trigonometry: Vectors	<ul style="list-style-type: none"> Trigonometry can be extended beyond geometric applications into a variety of areas, such as physics and the complex number system. Trigonometry can also be used to help develop non-rectangular or function graphing systems. 	5 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

			Quizzes			
			Chapter Test			
Unit 8: Additional Topics in Trigonometry: Trig Form of Complex Numbers and Polars	<ul style="list-style-type: none"> Complex numbers can be represented using trigonometry. Trigonometric representations of complex numbers simplify computations. 	8 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge
Unit 9: Matrices	<ul style="list-style-type: none"> We can use algebraic techniques to break down a complicated expression into smaller and more manageable parts. Knowing how to use matrices in the calculator can support algebraic techniques and make solving problems simpler. 	4 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

			Quizzes			
			Chapter Test			
Unit 10: Conic Sections	<ul style="list-style-type: none"> Conic Sections are formed when a plane intersects a cone. There are four types of curves known as conic sections: parabolas, circles, ellipses, and hyperbolas. Each curve has its own distinct shape and properties. Conic Sections reflect real-world phenomena. 	6 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge
Unit 11: Sequences, Series, and Probability	<ul style="list-style-type: none"> Sequences and series lead to the foundations of calculus and are an important part of higher levels of mathematics. Patterns in mathematics lead to more efficient ways of solving problems. 	9 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

			Exit Slips Quizzes Chapter Test			
Unit 12: Limits	<ul style="list-style-type: none"> The concept of a limit is one of the foundations of calculus. The limit of a function is the value approached by $f(x)$ as x approaches a given value. 	10 blocks	Unit Quizzes Open-Ended Questions Class Discussion In-class Assignments: (Group-work, Mini-Projects, Practice Material) Observations Exit Slips Quizzes Chapter Test	Unit Test with Varying Types of Questions Projects Authentic Assessments Core Assessments	Cumulative Exam Final Exam	Application Projects Graphing explorations Anticipatory Set/Warm Up Homework Quizzes Open-Ended Leading Questions Highlighting Prior Knowledge

Robbinsville Public Schools

Unit #1: Functions and Their Graphs

<p>Enduring Understandings:</p> <ul style="list-style-type: none"> • The domain of a function impacts the properties of functions when they are manipulated. • Relations and functions can be represented algebraically, numerically, and graphically. All graphical properties of functions can be established with algebraic work. • The properties of functions and function operations are used to model and analyze real-world applications and quantitative relationships. 	<p>Essential Questions:</p> <ul style="list-style-type: none"> • How is the domain affected when an equation is algebraically manipulated? • What characteristics of a function are based on its domain? • How is algebra used to determine characteristics of functions?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Literacy SL.9-10.1.B Collaborate with peers to set rules for discussions (e.g. informal consensus, taking votes on key issues, presentation of alternate views); develop clear goals and assessment criteria (e.g. student developed rubric) and assign individual roles as needed. Example: Students, when preparing and conducting peer and class error analysis, assign roles and set group norms for conducting respectful and constructive feedback.</p> <p>9.4.12.CT.2: Explain the potential benefits of collaborating to enhance critical thinking and problem solving <i>Example:</i> Students will work together to review prerequisite problems from the summer packet</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Functions are found all over the real world, anywhere there is an input and an output. Some examples include: A circle's circumference is a function of its diameter, the length of a person's shadow along the floor is a function of their height, and when driving a car, location is a function of time. Students will create functions based on real world quantitative relationships and examine their inverse relationships.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
A-REI.D.11	<p>How can we use the graphing calculator to solve problems and determine features of graphs?</p> <p>What characteristics of a graph should we be able to visually identify?</p>	<p>Use a graphing calculator to find a regression equation.</p> <p>Use a graphing calculator to determine characteristics of a graph: maximum, minimum zeros.</p>	<p>Administer pre-test and reflection.</p> <p>Give a station activity in which students check answers to their packet and work on additional problems in their weak areas.</p>	<p>Pre-test and reflection.</p> <p>Summer packet answer key.</p> <p>Videos.</p>	<p>Written test/quiz</p> <p>Cooperative activities (rubrics)</p> <p>Notebooks</p> <p>Class participation</p>

A-REI. B.4b	What are the similarities and differences between the parent functions?	Use the intersect feature on a graphing calculator to solve equations.	Provide videos for students to look up similar problems.	Additional practice problems and homework.	Homework/written assignments
F-IF.B .4	How do the parameters a, b, c and d affect the graph of a function?	Graph transformations of the parent functions including quadratic, square root, cubic, cube root, absolute value, greatest integer and reciprocal functions.	Pair up students to work together and guide each other.		Response to discussion questions
F-BF. B.3	How can one function be created from several functions on a specified domain?	Graph piecewise functions.	Work with small groups as needed.		Anticipatory Sets/Do Now Problems
F-IF.C .7a,b	How can we simplify rational and radical expressions?	Write the equation of a parent and piecewise functions based on a given graph.			Diagnostic Assessments to determine readiness
F-BF. A.1b		Perform operations with rational and radical expressions.			Closure question/ Exit Slips
F-BF. A.1c	When two or more functions are combined, how does the domain of the combined function change from the domain of the individual functions?	Combine and compose functions algebraically and for a specified value.			Oral presentations
F-BF. B.4a		Find the inverse of a function algebraically.			Special projects
F-BF. B.4b	What is the relationship between a function and its inverse?	Prove functions are inverses using compositions.			
A-AP R.D.6	How can we use factoring to simplify polynomials and rational expressions?	Factor algebraic expressions.			
A-AP R.D.7	How can we write the equation of line in point-slope and slope-intercept form?	Solve for the zeros of a function algebraically.			
A-CED .A.1		Write linear equations in point-slope and slope-intercept form.			

F-IF.A .1	How can you find the domain of a function based on its algebraic properties? What types of symmetries exist within functions? How is algebra used to determine the symmetry of a function?	Determine the domain of a function algebraically. Determine the symmetry of a function algebraically.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	
F-IF.A .2			Use guided and independent practice activities		
F-IF.B .4			Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	Mimeo lessons www.desmos.com	
F-IF.B .5			Use cooperative learning activities Use discovery based learning activities that require students to make conjectures and investigate patterns Use whiteboards to show immediate feedback on questions Discover the symmetry rules with a partner. Matching card game between domain and equation. Emphasize notation using both interval and set notation. Include examples in which cases for domain overlap.	www.ixl.com Geometer's Sketchpad GeoGebra TI Smart View with TI 84 Graphing Calculators	
F-IF.B .4	What are the types of discontinuities that occur in functions? How are they related to the algebraic equation of a function?	Describe types of discontinuities in functions.	Same as above	Same as above	
F-IF.C .9		Determine the discontinuity of a function based on its algebraic equation.	Group work activity – create a function given characteristics. Swap and check with another group.		

	Can one always create a function that has given characteristics?	<p>Define boundedness and apply the term to the graph of a function.</p> <p>Create the graph and algebraic equation of functions given characteristics such as: domain, symmetry, boundedness, continuity, domain, range, increasing interval, decreasing interval, constant interval, x-intercepts, y-intercept, maximum, and minimum.</p>	Emphasize vocabulary – utilize see it, say it, write it.		
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Robbinsville Public Schools

Unit #2: Polynomial, Quadratic, and Rational Function

Enduring Understandings: <ul style="list-style-type: none"> There is a direct relationship between the graphs of polynomial and rational functions in terms of algebraically solving their equations when equal to zero. Technology allows us to approximate solutions easily, whereas solving for solutions algebraic gives us exact answers. We need to know when the difference between the two is relevant in a problem. 	Essential Questions: <ul style="list-style-type: none"> How are the techniques for solving a quadratic applied to solving polynomial or rational function? What are the relationships between the graphs of different polynomial and rational functions?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Tech 8.2.12.A.3 The relationships among technologies and the connections between technology and other fields of study <i>Example:</i> Students will use technology to graph multiple function types and analyze, compare and contrast the graphs</p> <p>9.3.12.BM-MGT.2 Access, evaluate, and disseminate information for business decision making. <i>Example:</i> Students will access, evaluate, and disseminate information given by polynomials to optimize profit for businesses</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Since polynomials are used to describe curves of various types, people use them in the real world to graph curves. For example, roller coaster designers may use polynomials to describe the curves in their rides. Additionally, polynomials are used in physics to describe the trajectory of projectiles. Rational functions can represent direct, inverse, and joint variation in the real world. From anesthesia to economics, rational functions are used in multiple areas of study to help predict outcomes.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
A-AP R.B.2	How can you use the Zero Product Property to find solutions of quadratic equations?	Find the zeros of quadratics by factoring, completing the square or using the quadratic formula.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
A-AP R.B.3	What methods are necessary to completely factor a higher order polynomial function?	Find the zeros of polynomials algebraically, by factoring or using synthetic or long division.	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics)
A-REI. B.4		Apply the Upper and Lower Bound Theorems, Descartes Rule of Signs,	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts		Notebooks
					Class participation
					Homework/written assignments

<p>A-SSE.B.3a</p> <p>F-IF.C.7c</p> <p>F-IF.C.8a</p> <p>N-CN.C.7</p> <p>N-CN.C.9</p>	<p>How many solutions can a quadratic equation have? What type are they?</p> <p>What patterns emerge when determining complex roots of a polynomial?</p> <p>How does the degree and leading coefficient of a polynomial affect the shape of the graph of the function?</p> <p>How does the multiplicity of the zeros or factors of a function affect the graph of the function?</p>	<p>Rational Root Theorem on polynomials to find zeros algebraically</p> <p>Apply the Fundamental Theorem of Algebra to graph and write equations of polynomials</p> <p>Find imaginary zeros of a polynomial or quadratic.</p> <p>Use the complex conjugate theorem to find remaining zeros of polynomials.</p> <p>Find the x intercept(s), y intercept, and end behavior of polynomials.</p> <p>Graph polynomials.</p> <p>Write equations of polynomials based on a graph or given characteristics.</p>	<p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Provide a template to assist with organization.</p>	<p>Teacher created worksheets</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
<p>A-REI.D.11</p> <p>A-REI.A.2</p> <p>F-IF.C.7d</p>	<p>What are the six characteristics of rational functions that help us to create their graphs? How are they found?</p> <p>What real world scenarios represent asymptotes in word problems?</p>	<p>Determine vertical, asymptotes, horizontal or slant asymptotes, zero(s), y intercept, and removable discontinuities of rational functions.</p> <p>Graph rational functions.</p> <p>Write equations of rational functions based on a graph or given characteristics.</p> <p>Solve word problems that are modeled by rational functions.</p> <p>Use the calculator to solve rational and polynomial word problems using the intersect, zero, max/min, and value feature.</p>	<p>Same as above</p> <p>Use prompts as to what criteria needs to be found for rational functions.</p> <p>Create flashcards with instructions on how to find each characteristic of a rational function and use them to quiz each other.</p> <p>Provide a template to assist with organization.</p>	<p>Same as above</p>	

F-IF.C .7d	<p>How can an inequality be used to graph a function?</p> <p>What different ways can both polynomial and rational inequalities be solved?</p> <p>Are there certain methods that work better for solving different types of inequalities?</p>	<p>Sketch the graph of a polynomial using inequalities.</p> <p>Use different methods to algebraically solve polynomial and rational inequalities.</p> <p>Use a graphing calculator to solve inequalities graphically.</p> <p>Solve inequalities involving radicals and absolute values.</p>	Same as above	Same as above	

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Unit #3: Exponential and Logarithmic Functions

Enduring Understandings: <ul style="list-style-type: none"> • Data that multiplies by a constant factor increases and decreases rapidly over time is represented by an exponential equation • All exponential and logarithmic functions can be written in either exponential or logarithmic form • Predictions for population, carbon dating, compound interest, and cooling are all examples of how exponential and logarithmic models are used to interpret real world data 	Essential Questions <ul style="list-style-type: none"> • What are the characteristics of exponential and logarithmic models? • How can you tell if the exponential or logarithmic form of a function is needed to solve a problem? • When and how are exponential and logarithmic models used in everyday life?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Tech HS-ETS1-4. Use a computer simulation to model the impact of proposed solutions to a complex real-world problem with numerous criteria and constraints on interactions within and between systems relevant to the problem. <i>Example:</i> Students will graph exponential functions and discuss the real world factors that affect rate of growth or decay</p> <p>Science HS-ESS3-6 Use a computational representation to illustrate the relationships among Earth systems and how those relationships are being modified due to human activity (i.e., climate change). <i>Example:</i> Students will study the spread of disease to a population as exponential growth, and how human activity can affect spread</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Coronavirus is a global pandemic that exemplifies exponential growth. Human behavior, among other factors, can affect the rate of infection. Students can study different states and countries to see how their behavior changed the course of the virus</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
F-BF.B.3 A-SSE.B.3c F-IF.C.7e	<p>What is the difference between the graphs of exponential growth and decay? What graphical properties do both exponential growth and exponential decay share?</p> <p>How do the transformation rules affect</p>	<p>Graph transformations of exponential functions.</p> <p>Graph transformations of logarithmic functions.</p> <p>Find the intercepts and other characteristics of exponential and logarithmic functions.</p>	<p>Anticipatory sets to measure background knowledge and engage students</p> <p>Use guided and independent practice activities</p> <p>Use the Mimeo, whiteboard, and worksheets to reinforce the concepts</p>	<p>Worksheets and sample problems to analyze step-by-step solutions of the problems</p> <p>Textbook & associated materials</p>	<p>Written test/quiz</p> <p>Cooperative activities (rubrics)</p> <p>Notebooks</p> <p>Class participation</p> <p>Homework/written assignments</p>

F-LE. A.3	<p>the graphs of exponential and logarithmic functions?</p> <p>How is a logarithmic graph related to an exponential graph?</p>		<p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Compare and contrast summary of exponential versus logarithmic graphs and their characteristics.</p> <p>Introduce growth and decay using real world scenarios.</p>	<p>Teacher created worksheets</p> <p>www.desmos.com</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
A-SSE .B.3c F-BF. B.5	<p>How are exponential functions written in logarithmic form and vice versa?</p> <p>How are the properties of logarithmic functions related to the properties of exponents?</p>	<p>Convert between exponential and logarithmic form.</p> <p>Evaluate logarithms without a calculator.</p> <p>Condense and expand logarithms using their properties.</p>	<p>Same as above</p> <p>Split up the class into groups based on readiness. Work with a small group while the other group works with each other.</p> <p>Emphasize how to recognize when a calculator is not necessary.</p> <p>Reference the exponent rules when showing the logarithm rules.</p>	<p>Same as above</p> <p>SAT 2 property problems</p>	
F-LE. A.4	<p>What are the different ways of solving exponential and logarithmic equations?</p>	<p>Solve exponential and logarithmic equations.</p> <p>Apply algebraic techniques to solving exponential and logarithmic problems.</p>	<p>Same as above</p> <p>Classify types of exponential and logarithmic solving problems by solving technique.</p>	<p>Same as above</p>	

	How can you use the form of an exponential or logarithmic equation to determine the algebraic solving strategy?				
A-REI.D.11 F-IF.C.8b A-CE.D.A.1 F-BF.A.1b F-LE.B.5	<p>Given a set of data, how can you represent the data with a mathematical model both algebraically and using technology?</p> <p>How can you create exponential or logarithmic models from word problems? How can you use solving techniques to solve for the missing variable in the problem?</p> <p>How can you verify algebraic techniques for solving exponential equations using technology?</p>	<p>Interpret an exponential model through the context of a word problem.</p> <p>Create exponential models (growth and decay) and logarithmic models for real world applications and use them to solve problems.</p> <p>Solve exponential and logarithmic word problems as a system of equations using technology to find the point of intersection.</p>	<p>Same as above</p> <p>Use expert jigsaw to have groups solve a word problem and teach another group their solution.</p>	Same as above	
S-ID.B.6a S-ID.C.8 F-IF.B.6	<p>What determines if a mathematical model should be linear, quadratic, or exponential?</p> <p>What is another word for average rate of change?</p> <p>How and why is the average rate of change different based on the</p>	<p>Compare and contrast linear models, quadratic, and exponential models.</p> <p>Find and interpret the average rate of change in the context of a real world problem using linear, quadratic, and exponential models.</p>	<p>Same as above</p> <p>Analyze the difference between average rates of change on all three models with the same intervals. Create a visual for each.</p>	Same as above	

	model chosen and the parameters used?				
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Unit #4: Trigonometric Functions

Enduring Understandings: <ul style="list-style-type: none"> • Periodic behavior is behavior that repeats over intervals of equal length. • The measure of an angle is the input for two important functions called sine and cosine. • You can translate periodic functions in the same way that you translate other functions. • Sine, cosine, and tangent have reciprocals. 	Essential Questions <ul style="list-style-type: none"> • How can the unit circle be used to calculate the six trigonometric functions? • How can you model periodic behavior? • What information does a trigonometric function provide of its graph? • If you know the value of sin, how can you find the values of all of the other trigonometric functions at that same angle?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Tech HS-ETS1-4. Use a computer simulation to model the impact of proposed solutions to a complex real-world problem with numerous criteria and constraints on interactions within and between systems relevant to the problem. <i>Example:</i> Students will graph trigonometric functions on the computer</p> <p>9.3.12.ED.2 Demonstrate effective oral, written, and multimedia communication in multiple formats and contexts. <i>Example:</i> Students will derive special trig values a number of ways, including using special right triangles, the unit circle, and several shortcuts</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Trigonometry is used in oceanography in calculating the height of tides in oceans. The sine and cosine functions are fundamental to the theory of periodic functions, those that describe the sound and light waves. Jobs that may use trigonometry are navigation, land surveying, mathematics, science, engineering, architecture, cartography, computer graphics, machining, meteorology, music theory, oceanography, phonetics, seismology, and statistics.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
F-TF. A.1	What is a radian measure?	Convert between degree and radian measure.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
F-TF. A.2	How do you convert between degrees and radians?	Use angles to model and solve real world problems.	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics) Notebooks
F-TF. A.3	How do trigonometric functions relate to right angles?	Evaluate trigonometric functions of acute angles.	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts		Class participation Homework/written assignments

F-TF. A.4 G-SR T.C.6 G-SR T.C.8	<p>What is special about the trigonometric functions of 30, 45, and 60-degree angles?</p> <p>How does each trigonometric function relate to the others?</p> <p>What is a unit circle?</p> <p>How do special right triangles help determine measures on the unit circle?</p> <p>How does the unit circle make it easier to determine values of trigonometric functions?</p> <p>In what way do the coordinates on the unit circle differ based on which quadrant they are in?</p> <p>Can the coordinates in each quadrant determine how each trigonometric function is affected between different angles?</p>	<p>Use a calculator to evaluate trigonometric functions.</p> <p>Use the fundamental trigonometric identities.</p> <p>Solve real-world problems using trigonometric functions.</p> <p>Identify a unit circle and describe its relationship to real numbers.</p> <p>Create a unit circle.</p> <p>Use special right triangles to determine values of trigonometric functions on the unit circle.</p> <p>Evaluate trigonometric functions using the unit circle.</p> <p>Determine which trigonometric functions are negative in each quadrant.</p> <p>Evaluate trigonometric functions of any angle.</p> <p>Find reference angles.</p>	<p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Compare and contrast summary of exponential versus logarithmic graphs and their characteristics.</p> <p>Introduce growth and decay using real world scenarios.</p> <p>Give students blank unit circles to fill out as Do Nows.</p> <p>Partner practice activities on evaluating trigonometric functions.</p> <p>Emphasize connections between items on the unit circle to minimize memorization.</p>	<p>Teacher created worksheets</p> <p>www.desmos.com</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
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F-TF. B.5	<p>How can the sine, cosine, cosecant, secant, tangent, and cotangent functions be graphed using the unit circle?</p> <p>What does it mean for a function to have continuous cycles?</p> <p>How do the constants in trigonometric equations affect what the graph looks like?</p> <p>How many ways can trigonometric graphs be translated?</p> <p>How are each of the trigonometric graphs related?</p> <p>What real world applications do trigonometric functions have?</p> <p>What differences do the tangent and cotangents graphs have to the other trigonometric functions?</p>	<p>Sketch the parent graphs of all trigonometric functions.</p> <p>Use amplitude and period to sketch graphs of trigonometric functions.</p> <p>Graph reflections, midline, and phase shift translations of trigonometric functions.</p> <p>Solve real-life problems involving directional bearings.</p> <p>Solve real-life problems involving harmonic motion.</p>	<p>Same as above</p> <p>Provide a template for critical information.</p> <p>Display parent graphs on a word wall.</p> <p>Give stations with leveled difficulty of problems.</p> <p>Describe characteristics of the graphs in real world language (uphill, downhill, flipped out, etc.)</p>	Same as above	
F-TF. B.7	<p>How can trigonometric functions be inverted?</p>	<p>Evaluate and graph inverse trigonometric functions.</p> <p>Solve real world problems using inverse trigonometric functions.</p>	<p>Same as above</p> <p>Construct a chart of which quadrant applies to which inverse trigonometric function.</p>	Same as above	

	What does an inverse trigonometric function help you find?	Evaluate compositions of trigonometric functions.	Relate the graph of the inverse function to the quadrants you are using.		
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Honors Pre-Calculus
Unit 5: Analytic Trigonometry

Enduring Understandings: <ul style="list-style-type: none"> Given the relationships between the six basic trigonometric functions, it is possible to simplify the trigonometric expressions, making it easier to work with for mathematical application. Mathematics is a study of patterns, and the goal of algebra and trigonometry is to simplify complex patterns into easy forms that are more manageable. Trigonometric identities are just an extension of this basic mathematical skill. 	Essential Questions: <ul style="list-style-type: none"> How can you identify and model periodic behavior? How can you verify a trigonometric functions as an identity? How are trigonometric identities used to solve equations?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>ELA NJSLA.SL2. Integrate and evaluate information presented in diverse media and formats, including visually, quantitatively, and orally. <i>Example:</i> Students will use previously learned identities to solve problems presented in new ways.</p> <p>ELA NJSLA.SL3. Evaluate a speaker's point of view, reasoning, and use of evidence and rhetoric. <i>Example:</i> Students will discuss different ways to solve the same problem, and determine the best method when appropriate</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Students will have to use problem solving skills in this unit while collaborating with classmates. They will have to determine the most efficient method for solving and reason with their peers about each method. These are skills that they will need in any future job when working with coworkers.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
A-SSE .A.1a	What is a trigonometric identity?	Simplify trigonometric expressions using trigonometric identities.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
A-SSE .A.1b	How can we use problem solving skills to transform trigonometric expressions using identities?	Apply algebraic techniques to trigonometric expressions.	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics)
A-SSE .A.2		Describe the trigonometric identities.	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	www.ixl.com	Notebooks
F-TF. C.8		Verify trigonometric identities.			Class participation

			<p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Administer puzzle proofs.</p> <p>Have students see, say, and write the trigonometric identities to memorize them.</p> <p>Create a checklist of simplifying strategies on a word wall</p> <p>Show multiple ways to simplify or verify the same problem and have students compare them</p>	<p>Teacher created worksheets</p> <p>Mimeo lessons</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Homework/written assignments</p> <p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
<p>A-SSE .A.2</p> <p>F-TF. B.7</p> <p>F-TF. C.9</p>	<p>How can we use sum and difference identities, double angle identities, half angle identities, and power reducing identities to evaluate trigonometric functions that are not on the unit circle?</p>	<p>Apply the sum and difference identities, double angle identities, half angle identities, and power reducing identities to simplifying and verifying problems.</p> <p>Evaluate trigonometric expressions numerically using sum and difference identities, double angle identities, half angle identities, and power reducing identities.</p>	<p>Same as above.</p> <p>Administer a matching game between the problem and solution to sum and difference problems</p> <p>Discuss when using an identity is necessary and which identity is easier.</p> <p>Analyze how to recognize when drawing a right triangle is critical to solving a problem.</p>	<p>Same as above.</p> <p>Matching Game</p>	

A-SSE .A.1a A-SSE .A.1b A-SSE .A.2 F-TF. B.7	<p>How can we use properties of inverse trigonometric functions and the unit circle to determine the angles that satisfy the trigonometric equations?</p> <p>Can there be more than one solution to trigonometric equations?</p> <p>What are the strategies for solving trigonometric equations?</p> <p>How are trigonometric identities used to simplify and solve equations?</p>	<p>Solve trigonometric equations over a general and specified interval.</p> <p>Solve trigonometric equations with a multiple angle as an input.</p> <p>Apply algebraic techniques to solving trigonometric equations.</p> <p>Use inverses to solve trigonometric equations for values that are not defined on the unit circle.</p> <p>Use identities to simplify solving trigonometric equation problems.</p>	<p>Same as above.</p> <p>Use a send a problem partner activity</p> <p>Show how the algebraic solution to equations is represented graphically</p>	<p>Same as above.</p> <p>Send a Problem</p>	
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Unit #6: Additional Topics in Trigonometry: Law of Sines/Law of Cosines

Enduring Understandings: <ul style="list-style-type: none"> • Trigonometry goes beyond the right triangle. • Sides and angles of all triangles can be found, providing solutions to real-world problems. 	Essential Questions <ul style="list-style-type: none"> • How are oblique triangles solved using law of sines and law of cosines? • In real world situation, how can the law of sines and law of cosines be used?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>9.4.12.CT.1: Identify problem-solving strategies used in the development of an innovative product or practice <i>Example:</i> Students will have to determine how to solve the ambiguous case and how many triangles are possible</p> <p>RST.11-12.7 Integrate and evaluate multiple sources of information presented in diverse formats and media (e.g., quantitative data, video, multimedia) in order to address</p>	

a question or solve a problem.

Example: Many mathematical applications of Law of Sines and Law of Cosines are given in word problem form and students must interpret the writing assign variables, and then solv

Career/Real World Connections

Example: Many real-world applications involve oblique triangles, where the Law of Sines and Cosines can be used to find certain measurements. The Law of Cosines is used to find a side, given an angle between the other two sides, or to find an angle given all three sides. For all other questions, the Law of Sines can be used.

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
G-SR T.D.11	What is an oblique triangle?	Use the law of sines to solve oblique triangles (AAS or ASA).	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
	How can we solve missing sides and angles of an oblique triangle?	Use the law of sines to solve oblique triangles (SSA).	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics)
	How can a triangle have no solution?	Use the law of sines to solve real world problems, including problems with bearings.	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	Teacher created worksheets	Notebooks
	How can a triangle have two solutions?	Find the area of an oblique triangle using law of sines.	Use cooperative learning activities	www.ixl.com	Class participation
			Use discovery based learning activities that require students to make conjectures and investigate patterns	Mimeo lessons	Homework/written assignments
			Use whiteboards to show immediate feedback on questions	Geometer's Sketchpad	Response to discussion questions
			Create a chart of all possible triangles and the strategy to solve them.	GeoGebra	Anticipatory Sets/Do Now Problems
				TI Smart View with TI 84 Graphing Calculators	Diagnostic Assessments to determine readiness
					Closure question/ Exit Slips
					Oral presentations
					Special projects

			Create leveled stations on solving word problems.		
G-SR T.D.11	How can we find angles of a triangle using only its side lengths? How can the law of cosines be used to find the area of a triangle?	Use the law of cosines to solve oblique triangles (SSS or SAS). Use the law of cosines to solve real-world problems. Use Heron's Area Formula to find areas of triangles.	Same as above	Same as above	

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Unit 7: Additional Topics in Trigonometry: Vectors

Enduring Understandings: <ul style="list-style-type: none"> Trigonometry can be extended beyond geometric applications into a variety of areas, such as physics and the complex number system. Trigonometry can also be used to help develop non-rectangular or function graphing systems. 	Essential Questions <ul style="list-style-type: none"> How is trigonometry used in other fields of math and science?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Sci HS-PS2-1. Analyze data to support the claim that Newton's second law of motion describes the mathematical relationship among the net force on a macroscopic object, its mass, and its acceleration. <i>Example:</i> Students will use vectors to model motion of an object</p> <p>Science HS-ESS2-3 Develop a model based on evidence of Earth's interior to describe the cycling of matter by thermal convection. <i>Example:</i> Students will use vectors to show flow of materials such as lava, water, or weather patterns</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Vectors are used to show both magnitude and direction in the real world and are often used to graphically represent weather patterns</p>	

Guiding / Topical Questions with Specific Standards	Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
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N-VM. A.1	What are the characteristics of vectors?	Sketch a vector on the coordinate plane.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
N-VM. A.2	How is a vector represented graphically?	Write a vector in component form given the initial and terminal point or a graph.	Use guided and independent practice activities		Cooperative activities (rubrics)
N-VM. B.4a	How can vectors be represented in different ways?	Find the magnitude of vectors.	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	Textbook & associated materials	Notebooks
N-VM. B.4b	In what ways are unit vectors similar to the unit circle?	Find the direction angle of a vector.	Use cooperative learning activities	Teacher created worksheets	Class participation
N-VM. B.4c	How can vectors be added and subtracted graphically?	Apply the arithmetic of vectors as related to trigonometry, both graphically and numerically	Use discovery based learning activities that require students to make conjectures and investigate patterns	www.ixl.com	Homework/written assignments
N-VM. B.5a		Determine the unit vector of a vector	Use whiteboards to show immediate feedback on questions	Mimeo lessons	Response to discussion questions
N-VM. B.5b		Write vectors as linear combinations	Show what is a vector video clip from Despicable Me	Geometer's Sketchpad	Anticipatory Sets/Do Now Problems
		Perform scalar multiplication of vectors, both graphically and numerically	Give guided reading homework on vocabulary from the unit	GeoGebra	Diagnostic Assessments to determine readiness
			Create a word wall of important vocabulary and how it affects the questions	TI Smart View with TI 84 Graphing Calculators	Closure question/ Exit Slips
			Create a word wall of formulas	http://illuminations.nctm.org/Activity.aspx?id=3536	Oral presentations
N-VM. B.4a	How can we use the dot product to determine the relationship between two vectors?	Find the Dot Product of two vectors	Same as above	Same as above	Special projects
		Find the angle between two vectors, using the dot product formula	Compare and contrast the dot product to scalar multiplication		

N-VM. B.4b N-VM. B.4c					
N-VM. A.3	How are vectors used to represent real world situations?	Solve application problems involving velocity using vectors.	Same as above Model a problem in depth. Show students a general formula for what types of vectors to add to calculate velocity.	Same as above	
A-CE D.A.2 A-RE I.C.6 N-VM. A.3	What are the benefits of graphing in parametric form? How do the parameters affect the graph of the same parametric equation? What does it mean to eliminate the parameter? How are vectors used to model the parametrization for the equation of a line between two points?	Graph parametric equations both by hand and using the calculator Eliminate the parameter to write equations in rectangular form Write the parameterization between two given points Solve word problems involving simultaneous motion and velocity using parametric equations	Same as above Use printed copies of notes for students. Compare graphs of the same equation with different parameters. Split up the classroom so some students receive guided practice while others work independently.	Same as above	

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Unit 8: Additional Topics in Trigonometry: Trig Form of a Complex Number and Polars

Enduring Understandings: <ul style="list-style-type: none"> Complex numbers can be represented using trigonometry. 	Essential Questions <ul style="list-style-type: none"> How do we represent complex numbers using trigonometry?
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<ul style="list-style-type: none"> • Trigonometric representations of complex numbers simplify computations 	<ul style="list-style-type: none"> • How does representing complex numbers in polar form simplify computations? • What are the differences between polar and rectangular coordinates?
<p align="center">Interdisciplinary Connections</p> <p>9.3.12.ED.2 Demonstrate effective oral, written, and multimedia communication in multiple formats and contexts. <i>Example:</i> Students will clearly show how to move from one number system to another and explain why the number system should be used.</p> <p>ELA NJSLA.SL2. Integrate and evaluate information presented in diverse media and formats, including visually, quantitatively, and orally. <i>Example:</i> Students will use previously learned identities to solve problems presented in new ways.</p>	
<p align="center">Career/Real World Connections</p> <p>Example: Polar coordinates are very useful in many “real life” applications where one moves from one point to another along an unimpeded vector, such as in the navigation of a plane, a ship, or a rocket. They are also used in calculating the equations of motion from a lot of mechanical systems such as electric fields, magnetic fields, and temperature fields.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
N-CN. A.1	What are complex numbers and how are they used in solving polynomial equations?	The complex numbers are an extension of the real number system and have many useful applications.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
N-CN. A.2			Use guided and independent practice activities		Cooperative activities (rubrics)
N-CN. A.3	How do you represent and operate using complex numbers?	The discriminant of a quadratic equation determines whether the equation has two real roots, one real root, or two complex conjugate roots.	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	Textbook & associated materials	Notebooks
N-CN. B.4	What is the imaginary axis?	Plot complex numbers in the complex plane and find absolute values of a complex number.	Use cooperative learning activities	Teacher created worksheets	Class participation
N-CN. B.5	How can you graph something that isn't real?	Convert complex numbers between standard and trigonometric form.	Use discovery based learning activities that require students to make conjectures and investigate patterns	www.ixl.com	Homework/written assignments
N-CN. B.6	How can there be an absolute value of a complex number?		Use whiteboards to show immediate feedback on questions	Mimeo lessons	Response to discussion questions
				Geometer's Sketchpad	Anticipatory Sets/Do Now Problems
				GeoGebra	Diagnostic Assessments to determine readiness

	How can you write a standard complex number in trigonometric form?		<p>Have students investigate which mathematical and scientific fields use complex numbers</p> <p>Guided examples with formulas highlighted.</p> <p>Create a word wall of important conversion formulas.</p> <p>Make a matching card game between forms.</p>	TI Smart View with TI 84 Graphing Calculators	<p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
N-CN. B.4	Can complex numbers be multiplied or divided?	Multiply and divide complex numbers written in trigonometric form.	Same as above	Same as above	
N-CN. B.5	What happens when a complex number is taken to a power?	Use DeMoivre's Theorem to find powers of complex numbers.			
N-CN. B.6	Can you root a complex number?	Find nth roots of complex numbers.			
N-CN. B.4	<p>What is a polar coordinate?</p> <p>What is a polar equation?</p> <p>How do polar points and equations relate to rectangular points and equations?</p>	<p>Plot polar points.</p> <p>Convert points and equations from polar to rectangular coordinates and vice versa.</p>	<p>Same as above</p> <p>Polar graph paper worksheets.</p>	Same as above	

N-CN. B.4	What do graphs of polar equations look like?	Graph polar equations and determine the symmetry of polar graphs.	Same as above	Same as above	
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Unit #9: Matrices

Enduring Understandings: <ul style="list-style-type: none"> We can use algebraic techniques to break down a complicated expression into smaller and more manageable parts. Knowing how to use matrices in the calculator can support algebraic techniques and make solving problems simpler. 	Essential Questions <ul style="list-style-type: none"> How can we use matrices to solve real world problems? What are the pros and cons of using matrices to solve problems?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>Tech 8.1.12.E.1 Evaluate and select information sources and digital tools based on the appropriateness for specific tasks. <i>Example:</i> Students will use technology to set up and solve matrices when appropriate</p> <p>ELA NJSLA.SL4. Present information, findings, and supporting evidence such that listeners can follow the line of reasoning and the organization, development, and style are appropriate to task, purpose, and audience <i>Example:</i> Students will determine when systems of equations should be solved graphically, algebraically, or using matrices</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Systems of equations in the real world (such as business or science) are often so complicated and full of variables that they cannot be solved by hand. So, students will learn to use matrices to solve such systems.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
A-REI .C.8	How can we perform matrix operations by hand and using the calculator?	Add, subtract, and perform scalar multiplication on matrices	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
A-REI .C.9	How are matrices used to organize information?	Represent data using a matrix	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics)
		Solve scalar word problems using matrices			Notebooks
		Multiply matrices using the calculator			Class participation

N-VM. C.6	When can matrices be multiplied?	Find the inverse of matrix using the calculator	Use the Mimeo, whiteboard, and worksheets to reinforce the concepts	Teacher created worksheets	Homework/written assignments
N-VM. C.8	What properties of real numbers are maintained through matrix operations?	Determine which algebraic properties hold true for matrix operations	Use cooperative learning activities	www.ixl.com	Response to discussion questions
N-VM. C.9			Use discovery based learning activities that require students to make conjectures and investigate patterns	Mimeo lessons	Anticipatory Sets/Do Now Problems
N-VM. C.10			Use whiteboards to show immediate feedback on questions	Geometer's Sketchpad	Diagnostic Assessments to determine readiness
			Have students self discover which matrices can be multiplied using examples	GeoGebra	Closure question/ Exit Slips
			Have students discover and/or prove which properties are true	TI Smart View with TI 84 Graphing Calculators	Oral presentations
					Special projects
A-SSE .A.2	What is partial fraction decomposition?	Write the partial fraction form for the decomposition of a rational function	Same as above	Same as above	
		Solve for the constants using matrices in partial fraction decomposition	Match the decomposition to the original problem		
			Emphasize vocabulary to review the rules		
			Show both algebraic and technological ways of solving		
			Show students how to check solutions		

			Students can add two rational functions and have their partner decompose it		
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Unit #10: Conic Sections

Enduring Understandings: <ul style="list-style-type: none"> Conic Sections are formed when a plane intersects a cone. There are four types of curves known as conic sections: parabolas, circles, ellipses, and hyperbolas. Each curve has its own distinct shape and properties. Conic Sections reflect real-world phenomena. 	Essential Questions <ul style="list-style-type: none"> How is each conic section related to a cone? What properties does an equation have to graph a circle, ellipse, parabola, and hyperbola? What applications can be drawn for the analysis of conic graphs?
Interdisciplinary Connections NJSLSA.SL2. Integrate and evaluate information presented in diverse media and formats, including visually, quantitatively, and orally. <i>Example:</i> Students will graph and/or describe conic sections given an equation, description, or graph. Tech 8.2.12.A.3 The relationships among technologies and the connections between technology and other fields of study <i>Example:</i> Students will use technology to graph multiple conic functions function types and analyze, compare and contrast the graphs given the equations	
Career/Real World Connections Example: The paths of the planets around the sun are ellipses with the sun at one focus. Parabolic mirrors are used to converge light beams at the focus of the parabola. Hyperbolic as well as parabolic mirrors and lenses are used in systems of telescopes.	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
G-.GP E.A.1	What are the characteristics of a circle? An ellipse?	Recognize a conic as the intersection of a plane and a double-mapped cone.	Anticipatory sets to measure background knowledge and engage students	Worksheets and sample problems to analyze step-by-step solutions of the problems	Written test/quiz
G-.GP E.A.3	How can we identify an equation as a circle equation?	Write equations of circles and ellipses in standard form given characteristics of the circle.	Use guided and independent practice activities	Textbook & associated materials	Cooperative activities (rubrics) Notebooks Class participation

	<p>How do we find the center and radius of a circle?</p> <p>How can we identify an equation as an ellipse equation?</p> <p>How do we find the center, foci, and axes of an ellipse?</p>	<p>Complete the square in quadratic equations to write the equation of the ellipse from general to standard form.</p> <p>Sketch circles and ellipses using their equations.</p> <p>Complete the square to write the equation of a circle from general to standard form.</p> <p>Find eccentricity of an ellipse.</p> <p>Model and solve real world situations using circle and elliptical equations.</p>	<p>Use the Mimeo, whiteboard, and worksheets to reinforce the concepts</p> <p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Review completing the square on prior homework.</p> <p>Video on all four types of conic sections.</p> <p>Give partner practice on ellipse and circle problems in which each partner has the other's answers.</p> <p>Create an ellipse using a string.</p>	<p>Teacher created worksheets</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Homework/written assignments</p> <p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
G-.GP E.A.2	<p>What are the characteristics of a hyperbola?</p> <p>How can we identify an equation as an ellipse equation?</p> <p>What are the similarities and differences between a hyperbola and an ellipse?</p>	<p>Write equations of hyperbolas in standard form given its characteristics.</p> <p>Complete the square on quadratic equations to write the equation of the hyperbola from general to standard form.</p> <p>Find the asymptotes of a hyperbola.</p> <p>Sketch a hyperbola using its equation.</p> <p>Find eccentricity of a hyperbola.</p>	<p>Same as above</p> <p>Give partner practice on ellipse and circle problems in which each partner has the other's answers.</p> <p>Compare and contrast the ellipse and hyperbola formulas and characteristics.</p>	<p>Same as above</p>	

	How do we find the center, foci, and axes of a hyperbola?	Model and solve real world situations using hyperbolic equations.			
G-.GP E.A.2	<p>What are the characteristics of a parabola?</p> <p>How can we identify an equation as a parabola equation?</p> <p>How do we find the vertex, directrix, and axis of a parabola?</p>	<p>Write equations of parabolas in standard form given its characteristics.</p> <p>Complete the square on quadratic equations to write the equation of the parabola from general to standard form.</p> <p>Sketch a parabola using its equation.</p> <p>Find the tangent line at a point on a parabola.</p> <p>Model and solve real world situations using parabolic equations.</p>	<p>Same as above</p> <p>Match the parabola to its graph.</p>	Same as above	

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Unit #11: Sequences, Series, and Probability

Enduring Understandings: <ul style="list-style-type: none"> Sequences and series lead to the foundations of calculus and are an important part of higher levels of mathematics. Patterns in mathematics lead to more efficient ways of solving problems. 	Essential Questions <ul style="list-style-type: none"> How are numeric patterns represented algebraically? What are the different algebraic ways of generating a sequence? What are the pros and cons of each?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>ELA NJSLA.SL3. Evaluate a speaker's point of view, reasoning, and use of evidence and rhetoric. <i>Example:</i> Students will discuss different ways to evaluate probability, and determine the best method when appropriate</p> <p>Tech HS-ETS1-4. Use a computer simulation to model the impact of proposed solutions to a complex real-world problem with numerous criteria and constraints on interactions within and between systems relevant to the problem. <i>Example:</i> Students will use technology to determine trends of infinite series and draw conclusions about different types of series</p>	
<p style="text-align: center;">Career/Real World Connections</p>	

Example: Geometric series can be used to calculate the amount of money in an account or the amount of medicine in a person's body at a given time. Infinite series have applications in engineering, physics, computer science, finance, and mathematics. In engineering, they are used for analysis of current flow and sound waves. In physics, infinite series can be used to find the time it takes a bouncing ball to come to rest or the swing of a pendulum to stop. Probability is used everyday in decision making. Meteorologists, for instance, use weather patterns to predict the probability of rain. In epidemiology, probability theory is used to understand the relationship between exposures and the risk of health effects.

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
F-BF. A.2 F-BF. B.3 F-LE. A.2	<p>What is the difference between explicit and recursive formulas?</p> <p>How is the notation used for explicit and recursive formulas similar? Different?</p> <p>What patterns help us to generate explicit formulas?</p> <p>What are the pros and cons of working with sequences in explicit or recursive form?</p>	<p>Compare and contrast explicit and recursive formulas</p> <p>Write an explicit and recursive formula for sequences</p> <p>Find terms of a given explicit formula</p> <p>Find terms of a given recursive formula</p>	<p>Anticipatory sets to measure background knowledge and engage students</p> <p>Use guided and independent practice activities</p> <p>Use the Mimeo, whiteboard, and worksheets to reinforce the concepts</p> <p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p> <p>Use tower of Hanoi activity as an introduction</p> <p>Write recursive patterns using sentences in order to write the formula</p>	<p>Worksheets and sample problems to analyze step-by-step solutions of the problems</p> <p>Textbook & associated materials</p> <p>Teacher created worksheets</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Written test/quiz</p> <p>Cooperative activities (rubrics)</p> <p>Notebooks</p> <p>Class participation</p> <p>Homework/written assignments</p> <p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>

			Create a table comparing the term of the sequence to the position in order to write the explicit formula		
F-BF. A.2	What is the pattern in an arithmetic sequence? A geometric sequence?	Define an arithmetic and geometric sequence	Same as above	Same as above	
F-LE. A.2	What real world problems represent arithmetic sequences? Geometric sequences?	Write explicit and recursive formulas for arithmetic sequences	Have students discover the formulas for each		
	How are arithmetic and geometric sequences represented graphically, algebraically, and numerically?	Write explicit and recursive formulas for geometric sequences	Interpret vocabulary for real world scenarios to distinguish between initial terms		
		Find the n th term in a geometric or arithmetic sequence			
		Solve word problems using sequences that are arithmetic or geometric			
A-SSE .B.4	What is the difference between a sequence and a series?	Expand and evaluate a series in summation notation	Same as above	Same as above	
F-BF. A.2	How can a series be represented most efficiently?	Write a series using summation notation	Review calculator shortcuts for evaluating a series		
F-LE. A.2	What real world problems represent arithmetic series? Geometric series?	Use the arithmetic and geometric series formulas to find the sum of finite series	Discover the pattern for infinite geometric series using examples		
	How can an infinite series have a sum?	Apply the arithmetic and geometric series formulas to word problems			
		Find the sum of an infinite geometric series			
		Determine if an infinite geometric series converges or diverges			

<p>S-CP. A.1</p> <p>S-CP. B.9</p>	<p>What is the difference between a permutation and a combination? How does that difference affect the factorial formula?</p>	<p>Solve counting problems using the Fundamental Counting Principle</p> <p>Differentiate between permutations or combinations</p> <p>Solve combination and permutation problems, both using the calculator and the factorial formula</p>	<p>Same as above</p> <p>Show a list or tree of possibilities before reviewing the formula</p> <p>Analyze the vocabulary associated with permutations or combinations</p> <p>Snap or clap to determine if a scenario is a permutation or combination</p>	<p>Same as above</p>	
<p>A-AP R.C.5</p>	<p>How are combinations used in expanded polynomials?</p> <p>How can a binomial be expanded most efficiently?</p> <p>What are the patterns in Pascal's Triangle?</p>	<p>Expand a binomial by applying the binomial theorem</p> <p>Determine a specific term in an expanded binomial</p> <p>Solve combination problems using Pascal's Triangle</p>	<p>Same as above</p> <p>Use an expert jigsaw to explore the four concepts of the binomial theorem</p> <p>Expand a binomial by multiplying factors (the long way)</p> <p>Review the general formula for one term in the expanded polynomial</p>	<p>Same as above</p> <p>http://mathcoachblog.com/2013/05/28/the-binomial-theorem-jigsaw/</p>	
<p>S-CP. A.2</p> <p>S-CP. A.3</p> <p>S-CP. A.4</p> <p>S-CP. A.5</p> <p>S-CP. B.6</p> <p>S-CP. B.7</p>	<p>When do we add probabilities together?</p> <p>When do we multiply probabilities?</p> <p>How and when are combinations used in probability questions?</p> <p>How do dependent events change probabilities?</p>	<p>Determine the probability of simple and compound events</p> <p>Distinguish between theoretical and experimental probability</p> <p>Distinguish between the probability of independent and dependent events</p> <p>Determine conditional probabilities, numerically and using frequency tables</p>	<p>Same as above</p> <p>Analyze the vocabulary associated with multiple or singular events</p> <p>Use kahoot practice game</p> <p>Review the cards in a standard deck</p>	<p>Same as above</p> <p>https://create.kahoot.it/#quiz/7bb2b141-a738-499b-ab0f-826c9b3040b6</p>	

S-CP. B.8	How does vocabulary affect our interpretation of conditional events?	Apply combinations and permutations to probability questions			
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Unit #12: Limits

Enduring Understandings: <ul style="list-style-type: none"> The concept of a limit is one of the foundations of calculus. The limit of a function is the value approached by $f(x)$ as x approaches a given value. 	Essential Questions <ul style="list-style-type: none"> What determines if a function is continuous? What strategies can be applied to determine the limit of a polynomial?
<p style="text-align: center;">Interdisciplinary Connections</p> <p>ELA NJSLSA.SL3. Evaluate a speaker's point of view, reasoning, and use of evidence and rhetoric. <i>Example:</i> Students will discuss different ways to solve the same problem, and determine the best method when appropriate</p> <p>Sci HS-PS2-1. Analyze data to support the claim that Newton's second law of motion describes the mathematical relationship among the net force on a macroscopic object, its mass, and its acceleration. <i>Example:</i> Students will use derivatives to model the rate of change of an object</p>	
<p style="text-align: center;">Career/Real World Connections</p> <p>Example: Among the disciplines that utilize calculus include physics, engineering, economics, statistics, and medicine. It is used to create mathematical models in order to arrive into an optimal solution.</p>	

Guiding / Topical Questions with Specific Standards		Content, Themes, Concepts, and Skills	Teaching Strategies	Instructional Resources and Materials	Assessment Strategies
A-SSE .A.1b A-SSE .A.22	What is a limit? How can we find a limit? How can a limit not exist?	Estimate a limit using a numerical or graphical approach. Use the formal definition of limit. Determine if a limit does not exist.	Anticipatory sets to measure background knowledge and engage students Use guided and independent practice activities	Worksheets and sample problems to analyze step-by-step solutions of the problems Textbook & associated materials	Written test/quiz Cooperative activities (rubrics) Notebooks Class participation

			<p>Use the Mimeo, whiteboard, and worksheets to reinforce the concepts</p> <p>Use cooperative learning activities</p> <p>Use discovery based learning activities that require students to make conjectures and investigate patterns</p> <p>Use whiteboards to show immediate feedback on questions</p>	<p>Teacher created worksheets</p> <p>www.ixl.com</p> <p>Mimeo lessons</p> <p>Geometer's Sketchpad</p> <p>GeoGebra</p> <p>TI Smart View with TI 84 Graphing Calculators</p>	<p>Homework/written assignments</p> <p>Response to discussion questions</p> <p>Anticipatory Sets/Do Now Problems</p> <p>Diagnostic Assessments to determine readiness</p> <p>Closure question/ Exit Slips</p> <p>Oral presentations</p> <p>Special projects</p>
<p>A-SSE .A.1b</p> <p>A-SSE .A.2</p>	<p>What are the basic properties of limits?</p> <p>How do the basic limit properties relate to multiplicative properties?</p> <p>How do the properties allow us to break up limits?</p> <p>What can graphs be used for when finding limits?</p> <p>How can you make a complicated limit less complicated by factoring or rationalizing?</p>	<p>Evaluate a limit using properties of limits.</p> <p>Develop and use strategies for finding limits.</p> <p>Evaluate a limit using dividing out and rationalizing techniques.</p> <p>Evaluate a limit using the squeeze theorem.</p>	Same as above	Same as above	

	What is the squeeze theorem?				
A-SSE .A.1b A-SSE .A.2 F.IF.0 7.D	<p>Does a function have a limit if it infinitely increases or decreases?</p> <p>How do vertical asymptotes help define infinite limits?</p> <p>How can an infinite limit be determined algebraically?</p> <p>What properties do infinite limits have?</p>	<p>Determine infinite limits from the left and from the right.</p> <p>Find and sketch the vertical asymptotes of the graph of a function.</p>	Same as above	Same as above	
F.IF.0 4	<p>What does it mean for a function to be continuous?</p> <p>What are the qualifications for continuity?</p> <p>How can a closed interval affect the continuity of a function?</p> <p>What is the Intermediate Value Theorem and how does it assist in finding if a function is continuous?</p>	<p>Determine continuity at a point and continuity on an open interval.</p> <p>Determine one-sided limits and continuity on a closed interval.</p> <p>Use properties of continuity.</p> <p>Understand and use the Intermediate Value Theorem.</p>	Same as above	Same as above	

F.IF.0 6	<p>How is the tangent line of a curve connected to the limit of a curve?</p> <p>What is the derivative of a function?</p> <p>How can you use the tangent lines of a curve to determine the derivative of its function?</p>	<p>Find the slope of a tangent line to a curve of a point.</p> <p>Use the limit definition to find the derivative of a function.</p> <p>Understand the relationship between differentiability and continuity.</p>	Same as above .	Same as above	
F.IF.0 6	<p>Are there easier ways of finding the derivative of functions other than using tangent lines?</p>	<p>Find the derivative of a function using the Constant Rule, Power Rule, Constant Multiple Rule, and the Sum and Difference Rule.</p> <p>Use derivatives to find rate of change.</p>			

General Differentiated Instruction Strategies	
<ul style="list-style-type: none"> • Leveled texts • Chunking texts • Choice board • Socratic Seminar • Tiered Instruction • Small group instruction • Guided Reading • Sentence starters/frames • Writing scaffolds • Tangible items/pictures • Adjust length of assignment 	<ul style="list-style-type: none"> • Repeat, reword directions • Brain breaks and movement breaks • Brief and concrete directions • Checklists for tasks • Graphic organizers • Assistive technology (spell check, voice to type) • Study guides • Tiered learning stations • Tiered questioning • Data-driven student partnerships • Extra time

Possible Additional Strategies for Special Education Students, 504 Students, At-Risk Students, and English Language Learners (ELLs)			
Time/General	Processing	Comprehension	Recall
<ul style="list-style-type: none"> • Extra time for assigned tasks • Adjust length of assignment • Timeline with due dates for reports and projects • Communication system between home and school • Provide lecture notes/outline 	<ul style="list-style-type: none"> • Extra Response time • Have students verbalize steps • Repeat, clarify or reword directions • Mini-breaks between tasks • Provide a warning for transitions • Reading partners 	<ul style="list-style-type: none"> • Precise step-by-step directions • Short manageable tasks • Brief and concrete directions • Provide immediate feedback • Small group instruction • Emphasize multi-sensory learning 	<ul style="list-style-type: none"> • Teacher-made checklist • Use visual graphic organizers • Reference resources to promote independence • Visual and verbal reminders • Graphic organizers

Assistive Technology	Assessments and Grading	Behavior/Attention	Organization
<ul style="list-style-type: none"> ● Computer/whiteboard ● Tape recorder ● Spell-checker ● Audio-taped books 	<ul style="list-style-type: none"> ● Extended time ● Study guides ● Shortened tests ● Read directions aloud 	<ul style="list-style-type: none"> ● Consistent daily structured routine ● Simple and clear classroom rules ● Frequent feedback 	<ul style="list-style-type: none"> ● Individual daily planner ● Display a written agenda ● Note-taking assistance ● Color code materials

Enrichment

The goal of Enrichment is to provide learners with the opportunity to participate in extension activities that are differentiated and enhance the curriculum. All enrichment decisions will be based upon individual student needs.

- Show a high degree of intellectual, creative and/or artistic ability and demonstrate this ability in multiple ways.
- Pose questions and exhibit sincere curiosity about principles and how things work.
- The ability to grasp concepts and make real world and cross-curricular connections.
- Generate theories and hypotheses and pursue methods of inquiry.
- Produce products that express insight, creativity, and excellence.
- Possess exceptional leadership skills.
- Evaluate vocabulary
- Elevate Text Complexity
- Inquiry based assignments and projects
- Independent student options
- Tiered/Multi-level activities
- Purposeful Learning Center
- Open-ended activities and projects
- Form and build on learning communities
- Providing pupils with experiences outside the 'regular' curriculum
- Altering the pace the student uses to cover regular curriculum in order to explore topics of interest in greater depth/breadth within their own grade level
- A higher quality of work than the norm for the given age group.
- The promotion of a higher level of thinking and making connections.
- The inclusion of additional subject areas and/or activities (cross-curricular).

- Using supplementary materials in addition to the normal range of resources.

English Language Learner (ELL) Resources

- Learning style quiz for students- <http://www.educationplanner.org/students/self-assessments/learning-styles-quiz.shtml>
- “Word clouds” from text that you provide-<http://www.wordle.net/>
- Bilingual website for students, parents and educators: <http://www.colorincolorado.org/>
- Learn a language for FREE-www.Duolingo.com
- Time on task for students-<http://www.online-stopwatch.com/>
- Differentiation activities for students based on their Lexile-www.Mobymax.com
- WIDA-<http://www.wida.us/>
- Everything ESL - <http://www.everythingESL.net>
- ELL Tool Box Suggestion Site <http://www.wallwisher.com/wall/elltoolbox>
- Hope4Education - <http://www.hope4education.com>
- Learning the Language <http://blogs.edweek.org/edweek/learning-the-language/>
- FLENJ (Foreign Language Educators of NJ) 'E-Verse' wiki: <http://www.flenj.org/Publications/?page=135>
- OELA - <http://www.ed.gov/offices/OBEMLA>
- New Jersey Department of Education- Bilingual Education information <http://www.state.nj.us/education/bilingual/>

Special Education Resources

- Animoto -Animoto provides tools for making videos by using animation to pull together a series of images and combining with audio. Animoto videos or presentations are easy to publish and share. <https://animoto.com>
- Bookbuilder -Use this site to create, share, publish, and read digital books that engage and support diverse learners according to their individual needs, interests, and skills. <http://bookbuilder.cast.org/>
- CAST -CAST is a non-profit research and development organization dedicated to Universal Design for Learning (UDL). UDL research demonstrates that the challenge of diversity can and must be met by making curriculum flexible and responsive to learner differences. <http://www.cast.org>
- CoSketch -CoSketch is a multi-user online whiteboard designed to give you the ability to quickly visualize and share your ideas as images. <http://www.cosketch.com/>
- Crayon -The Crayon.net site offers an electronic template for students to create their own newspapers. The site allows you to bring multiple

sources together, thus creating an individualized and customized newspaper. <http://crayon.net/> Education Oasis -Education Oasis offers a collection of graphic organizers to help students organize and retain knowledge – cause and effect, character and story, compare and contrast, and more! <http://www.educationoasis.com/printables/graphic-organizers/>

- Edutopia -A comprehensive website and online community that increases knowledge, sharing, and adoption of what works in K-12 education. We emphasize core strategies: project-based learning, comprehensive assessment, integrated studies, social and emotional learning, educational leadership and teacher development, and technology integration. <http://www.edutopia.org/>
- Glogster -Glogster allows you to create "interactive posters" to communicate ideas. Students can embed media links, sound, and video, and then share their posters with friends. <http://edu.glogster.com/?ref=personal>
- Interactives – Elements of a Story -This interactive breaks down the important elements of a story. Students go through the series of steps for constructing a story including: Setting, Characters, Sequence, Exposition, Conflict, Climax, and Resolution. <http://www.learner.org/interactives/story/index.html>
- National Writing Project (NWP) -Unique in breadth and scale, the NWP is a network of sites anchored at colleges and universities and serving teachers across disciplines and at all levels, early childhood through university. We provide professional development, develop resources, generate research, and act on knowledge to improve the teaching of writing and learning in schools and communities. <http://www.nwp.org>
- Pacecar -Vocab Ahead offers videos that give an active demonstration of vocabulary with audio repeating the pronunciation, definition, various uses, and synonyms. Students can also go through flash cards which give a written definition and visual representation of the word. <http://pacecar.missingmethod.com/>