

Unit IX: Worksheet 1

1. Two objects, A & B, have identical velocities. Object A has 3 times the mass of object B. Compare the momentum of each object. Justify your answer.

$$\begin{aligned}\rho &= m \cdot v \\ \rho_a &= 3m_b \cdot v \\ \rho_b &= m_b \cdot v \\ \rho_b &= \rho_a/3\end{aligned}$$

2. Two other objects, C and D, have identical masses. Object C has twice the velocity of object D. Compare the momentum of each object. Justify your answer.

$$\begin{aligned}m_c &= m_d \\ \rho_c &= m_c \cdot 2v_d \\ \rho_d &= m_d \cdot v_d \\ \rho_d &= \rho_c/2\end{aligned}$$

3. While being thrown, a net force of 132 N acts on a baseball (mass = 140g) for a period of 4.5×10^{-2} sec. What is the magnitude of the change in momentum of the ball?

$$\begin{aligned}F\Delta t &= \text{impulse} = \text{momentum} = m\Delta v \\ 132\text{N} \cdot (4.5 \times 10^{-2} \text{ s}) &= 5.94 \text{ N}\cdot\text{s}\end{aligned}$$

4. If the initial speed of the baseball in question 3 is $v_0 = 0.0$ m/s, what will its speed be when it leaves the pitcher's hand?

$$\begin{aligned}F\Delta t &= \text{impulse} = \text{momentum} = m\Delta v \\ 132\text{N} \cdot (4.5 \times 10^{-2} \text{ s}) &= 5.94 \text{ N}\cdot\text{s} = (0.140\text{kg})\Delta v \\ \Delta v &= 42.4 \text{ m/s}\end{aligned}$$

5. When the batter hits the ball, a net force of 1320 N, opposite to the direction of the ball's initial motion, acts on the ball for 9.0×10^{-3} s during the hit. What is the change in momentum of the ball? What is the final velocity of the ball? (use initial velocity from #4)

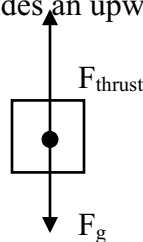
$$\begin{aligned}F\Delta t &= \text{impulse} = \text{momentum} = m\Delta v \\ 1320\text{N} \cdot (9.0 \times 10^{-3} \text{ s}) &= 11.88 \text{ N}\cdot\text{s} = (0.140\text{kg})\Delta v \\ \Delta v &= 84.9 \text{ m/s} = v_f - v_i = 84.9\text{m/s} = v_f - (-42.4\text{m/s}) = +42.5 \text{ m/s}\end{aligned}$$

6. What force does the ball exert on the bat in the question above? Explain.

Newton's 3rd Law: $F_{\text{bat on ball}} = -F_{\text{ball on bat}} = 1320\text{N} = -(-1320\text{N})$

7. A rocket, weighing $4.36 \times 10^4 \text{ N}$, has an engine that provides an upward force of $8.90 \times 10^5 \text{ N}$. It reaches a maximum speed of 860 m/s .

- a. Draw a force diagram for the rocket.



- b. How long must the engine burn in order to reach this speed?

$$\begin{aligned} F\Delta t &= m\Delta v \\ (8.90 \times 10^5 \text{ N} - 4.36 \times 10^4 \text{ N}) \Delta t &= 4.36 \times 10^3 \text{ N} \cdot 860 \text{ m/s} \\ \Delta t &= 4.43 \text{ s} \end{aligned}$$

8. A golf ball that weighs 0.45 N is dropped from a height of 1.0 m . Assume that the golf ball has a perfectly elastic collision with the floor.

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- a. In the margin, construct a motion map for the golf ball from the time it is dropped until it reaches its highest point of rebound.
- b. Determine the time required for the ball to reach the floor.

$$\begin{aligned} \Delta x &= \frac{1}{2}(10 \text{ m/s}^2)t^2 = 1.0 \text{ m} \\ t^2 &= 0.2 \text{ s}^2 \\ t &= 0.45 \text{ s} \end{aligned}$$

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- c. What will the instantaneous momentum of the golf ball be immediately *before* it strikes the floor?

$$\begin{aligned} v_f &= at + v_i \\ v_f &= 10 \text{ m/s}^2 \cdot 0.45 \text{ s} = 4.47 \text{ m/s} \\ 0.045 \text{ kg}(4.47 \text{ m/s}) &= 0.20 \text{ kg}\cdot\text{m/s} \end{aligned}$$

- d. What will be the change in momentum, (Δp) from the instant before the ball collides with the floor until the instant after it rebounds from the floor? (Illustrate with a vector diagram.)

$$\Delta p = (0.045 \text{ kg})(4.47 \text{ m/s} - (-4.47 \text{ m/s})) = 0.4023 \text{ kg}\cdot\text{m/s}$$

- e. Suppose that the golf ball was in contact with the floor for $4.0 \times 10^{-4} \text{ s}$. What was the average force on the ball while it was in contact with the floor?

$$\begin{aligned} F\Delta t &= m\Delta v \\ F &= (m\Delta v) / \Delta t \\ (0.045 \text{ kg})(8.94 \text{ m/s}) / (4.0 \times 10^{-4} \text{ s}) &= 1005.8 \text{ N} \end{aligned}$$