

WORK, ENERGY, AND POWER

CHAPTER 10



STANDARDS

- SP3. Students will evaluate the forms and transformations of energy.
 - a. Analyze, evaluate, and apply the principle of conservation of energy and measure the components of work-energy theorem by describing total energy in a closed system.
 - identifying different types of potential energy.
 - calculating kinetic energy given mass and velocity.
 - relating transformations between potential and kinetic energy.
 - g. Analyze and measure power.

WHAT IS WORK?

- Simple form: work = force \times distance

$$W = \mathbf{F} \cdot \mathbf{d}$$

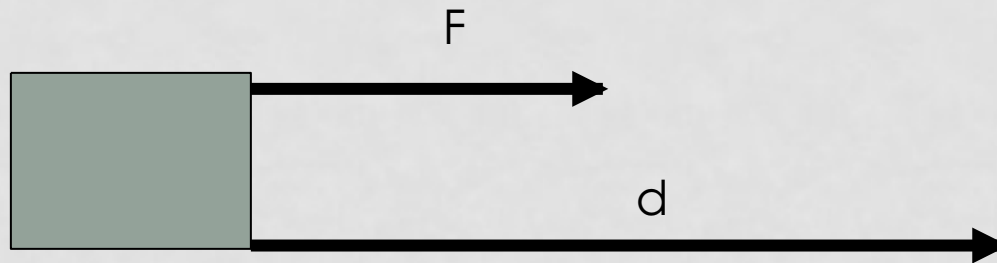
- Work can be done *by* you, as well as *on* you
 - Are you the *pusher* or the *pushee*?
- Work is a measure of expended energy
 - Work makes you tired
- Unit of work: Joules (j)
- Work is a *scalar* quantity

WORK DEPENDS ON

- The amount of force applied to the object.
- The distance that the object moves while the force is applied.
- The direction of the force with respect to the direction the object moves.

CALCULATING WORK

- If the force on the object is in the direction the object moves, the work done is:
- $W = f \times d$



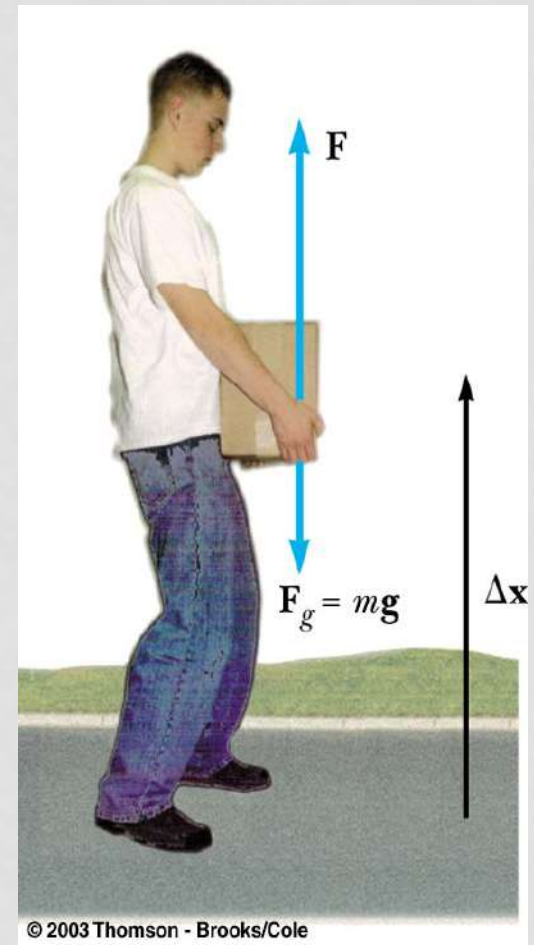
CALCULATING WORK

- If the direction of the force is **opposite** the direction the object moves, work is:
- $W = - f \times d$



CALCULATING WORK

- Work can be positive or negative
- Man does positive work lifting box
- Man does negative work lowering box
- Gravity does positive work when box lowers
- Gravity does negative work when box is raised



FORCE AND WORK

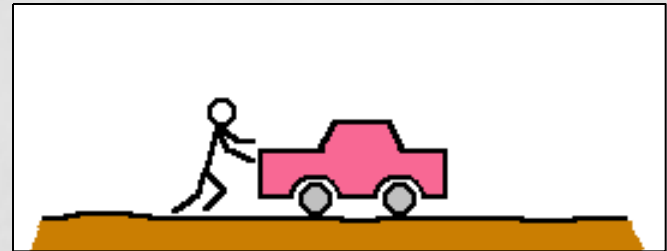
- Force and Work do not mean the same thing
- If the force is **perpendicular** to the direction the object moves, the work done is **0**.
- If the object **doesn't move**, the work done is **0**.
- $W = 0$



EXAMPLE

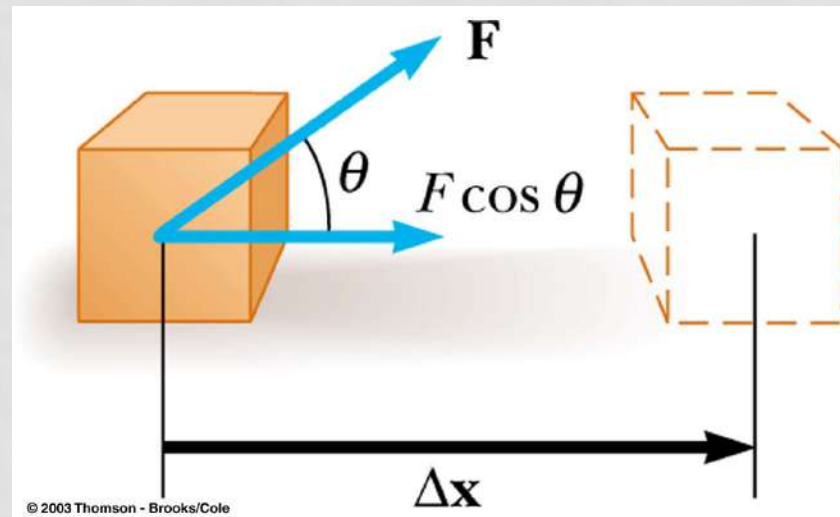
- A person pushes a car with a 110 N force for a distance of 30 m. How much work was done?

- $W = f \times d$
- $W = 110 \text{ N} \times 30\text{m}$
- $W = 3300 \text{ Nm}$ or 3300 J



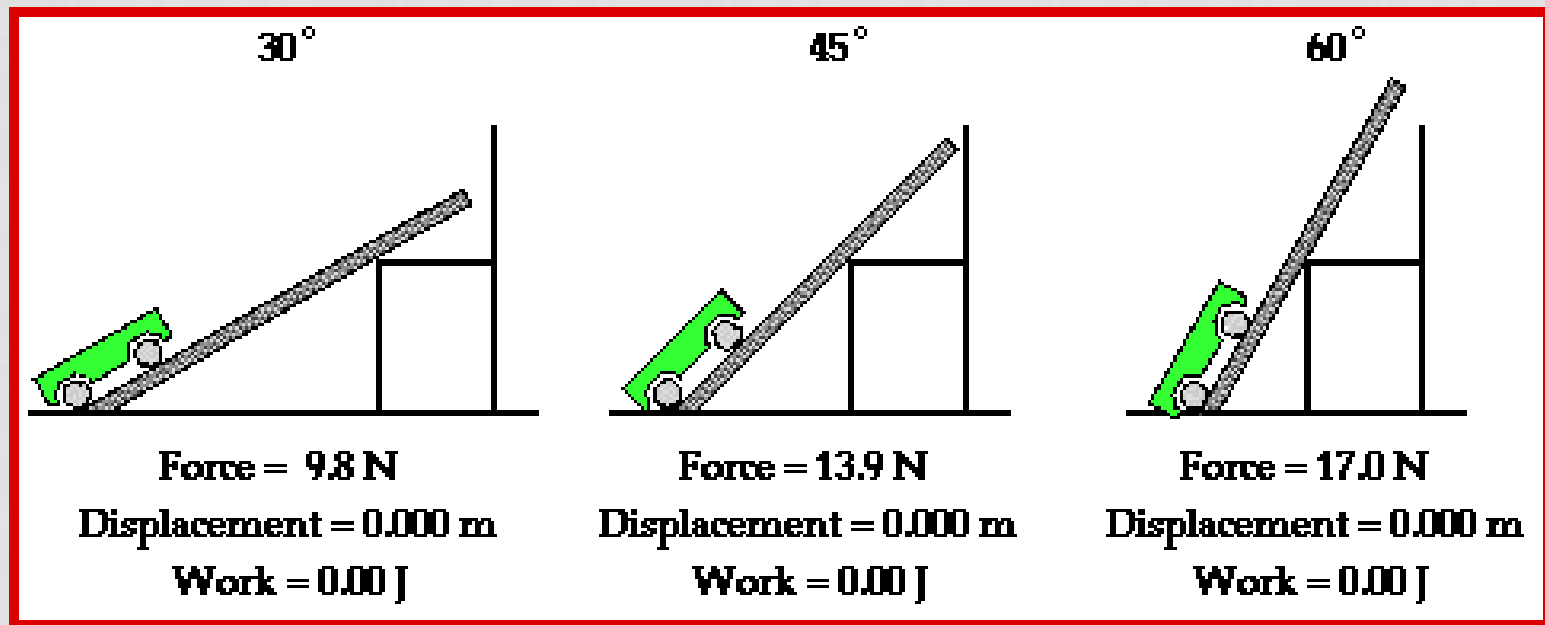
WHAT IF THERE IS AN ANGLE?

- Sometimes there is an angle between force and displacement
- The equation becomes:
- $W = f \times d \times \cos\theta$



ANGLE AND WORK

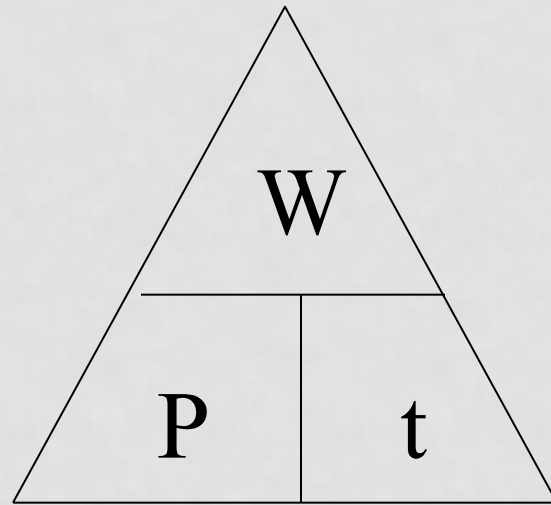
- Same amount of work, however the force needed is greater



WHAT IS POWER?

- Power is energy exchanged per unit of time
 - How fast you get work done
- Power = work over time

$$P = \frac{W}{t}$$



UNITS OF POWER

- Units of power: 1 Joule/sec = 1 **Watt**
- 1000 Watts = 1 **kilowatt**
- Power is a **scalar** quantity.
- 1 horsepower = 746 watts

EXAMPLE

- The minimum work required to raise a 800 N person up 10 m, is:
 - $W = F \times d$
 - $W = (800 \text{ N}) (10 \text{ m}) = 8000 \text{ J}$
- If this work is done in 60 sec, then what is the power?

$$P = \frac{W}{t} = \frac{8000 \text{ J}}{60 \text{ sec}} = 133 \frac{\text{J}}{\text{sec}} = 133 \text{ watts}$$

EXAMPLE

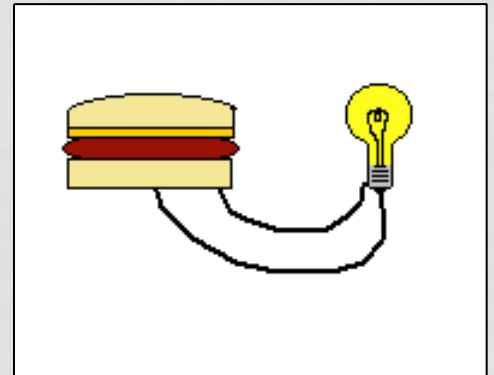
- A 'Big Mac' contains about 2,000,000 J of chemical energy. If all this energy could be used to power a 60 watt light bulb, how long could it run?

$$P = \frac{E}{t}$$

$$t = \frac{E}{P} = \frac{2,000,000 \text{ J}}{60 \text{ watt}}$$

$$t = 33,000 \frac{\text{J}}{\text{J/sec}}$$

$$t = 33,000 \text{ sec} \quad (\sim 9 \text{ hr})$$



WHAT IS ENERGY?

- *Energy is the capacity to do work*
- Two main categories of energy
 - Kinetic Energy: Energy of motion
 - Potential Energy: Stored (latent) capacity to do work
- *Energy can be converted between types*

KINETIC ENERGY

- Energy of motion
- An object's **kinetic energy** depends on:
 - the object's **mass**.
 - Kinetic energy is **directly proportional** to mass.
 - the object's **speed**.
 - Kinetic energy is **directly proportional** to the **square** of the object's speed.

$$KE = \frac{1}{2}mv^2$$

WORK-ENERGY THEOREM

- Work is equal to the change in kinetic energy.

$$W = \Delta KE$$

KINETIC ENERGY

- Kinetic energy is a ***scalar*** quantity.
- Common units of kinetic energy:
Joules

EXAMPLE

What is the KE of 100 kg of water moving at 1.2 m/sec?

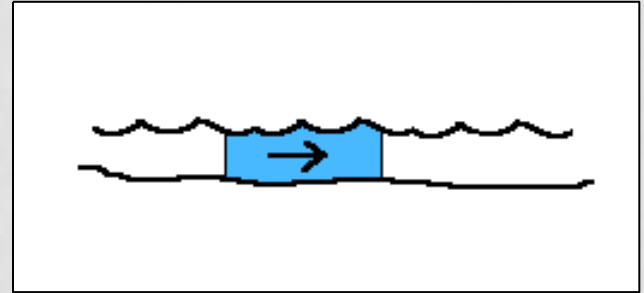
$$E_K = \frac{1}{2} mv^2$$

$$E_K = \frac{1}{2} (100 \text{ kg}) (1.2 \text{ m/s})^2$$

$$E_K = \frac{1}{2} (100 \text{ kg}) (1.44 \text{ m}^2/\text{s}^2)$$

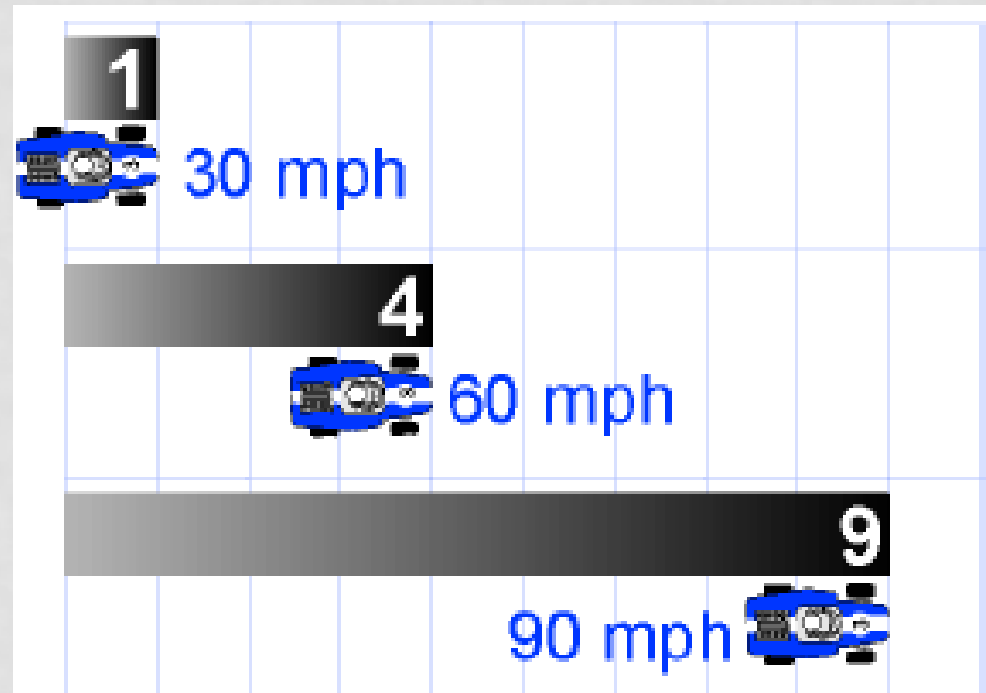
$$E_K = 72 (\text{ kg m}^2)/\text{s}^2$$

$$E_K = 72 \text{ J}$$



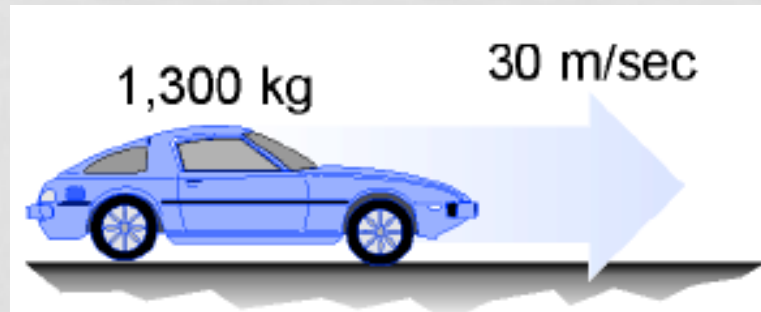
STOPPING DISTANCE

- Kinetic energy becomes important in calculating braking distance.



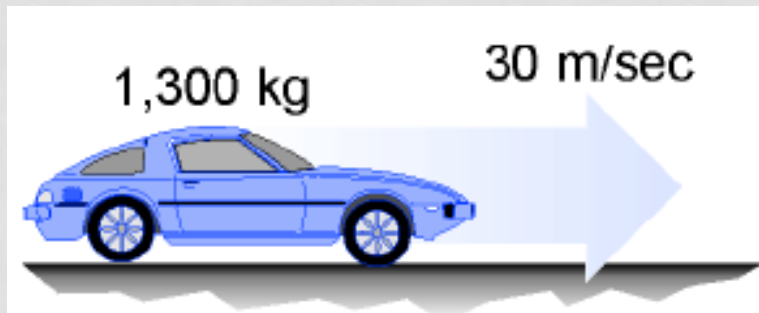
EXAMPLE

- A car with a mass of 1,300 kg is going straight ahead at a speed of 30 m/sec (67 mph).
- The brakes can supply a force of 9,500 N.
- Calculate:
 - a) The kinetic energy of the car.
 - b) The distance it takes to stop.



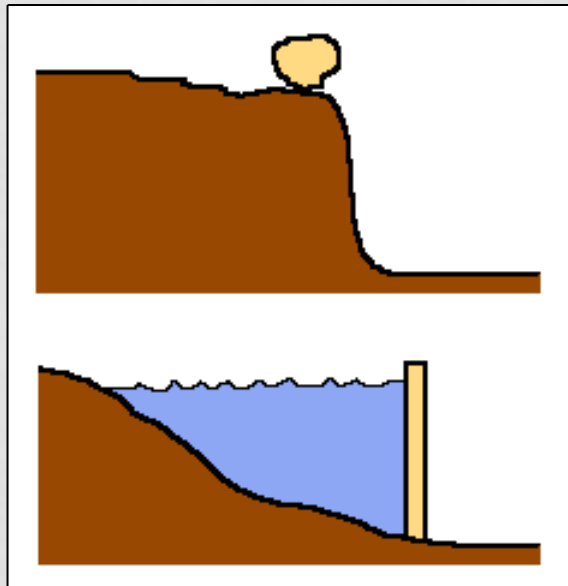
EXAMPLE

- Kinetic energy $KE = 1/2 mv^2$
- $KE = (1/2)(1,300 \text{ kg})(30 \text{ m/sec})^2$
- $KE = 585,000 \text{ J}$
- To stop the car, the kinetic energy must be reduced to zero by work done by the brakes.
- Work, $W = Fd$
- $585,000 \text{ J} = (9,500 \text{ N}) \times d$
- $d = 62 \text{ meters}$



POTENTIAL ENERGY

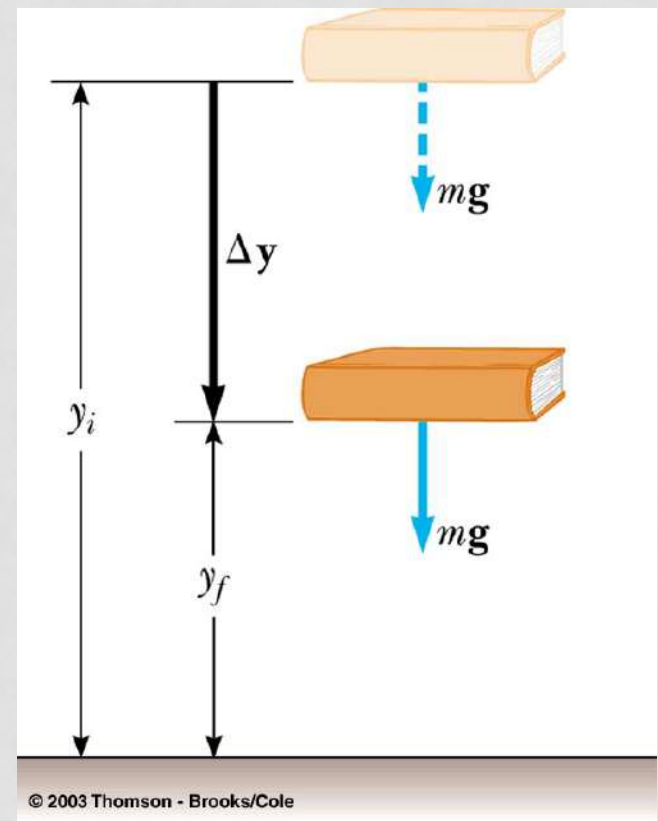
- Sometimes work is **not** converted directly into kinetic energy. Instead it is “stored”, or “hidden”.
- **Potential energy** is **stored energy** or **stored work**.
- **Potential energy** is energy that an object (system) has due to its **position** or **arrangement**.



GRAVITATIONAL POTENTIAL ENERGY

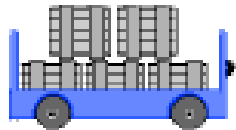
- Potential energy that is dependent on mass, height, and acceleration due to gravity
- Essentially this is work done against gravity

$$\text{GPE} = mgh$$

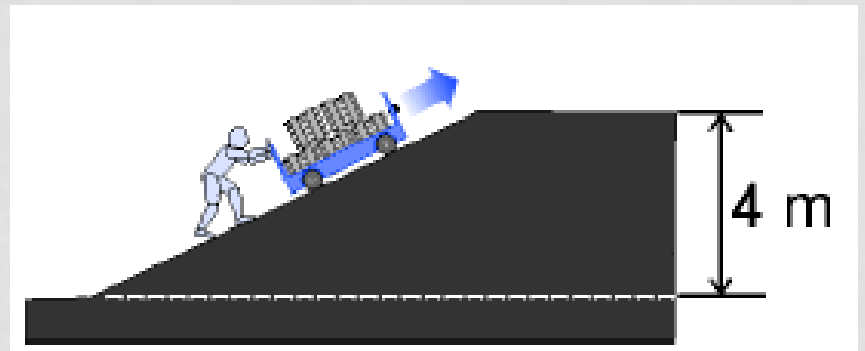


EXAMPLE

- A cart with a mass of 102 kg is pushed up a ramp.
- The top of the ramp is 4 meters higher than the bottom.
- How much potential energy is gained by the cart?
- If an average student can do 50 joules of work each second, how much time does it take to get up the ramp?

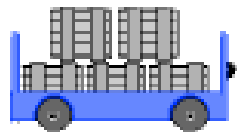


102 kg

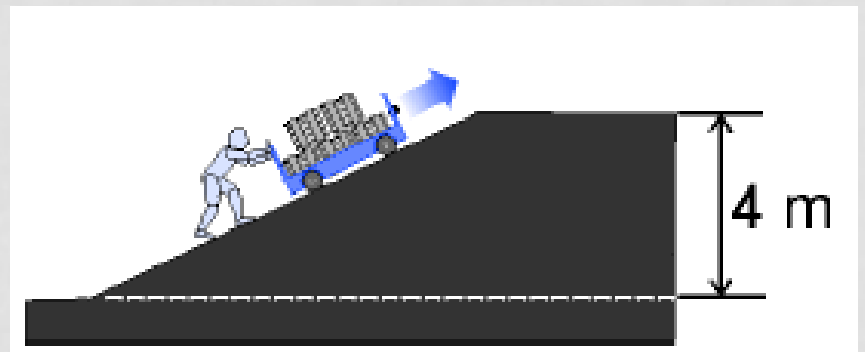


EXAMPLE, CONT

- Use the formula for potential energy $PE = mgh$.
- $PE = (102 \text{ kg})(9.8 \text{ N/kg})(4 \text{ m})$
- $PE = 3,998 \text{ J}$
- At a rate of 50 J/sec , it takes:
- $3,998 \div 50$
- 80 seconds to push the cart up the ramp.



102 kg



RELATIONSHIP OF PE AND KE

