## Mini Choice Board: GPS Honors Pre Calculus - Trigonometric Identities

Name

Directions: Complete three activities from this 3x3 grid in a tic-tac-toe arrangement (vertically, horizontally, or diagonally). Show all work on separate paper. You may work by yourself or with one partner. Each box is worth 33 points for a total of 99 points (rounded to 100). The center box is worth 15 additional bonus points.

- 1. **Simplify** the following two trig expressions to a single term or number. Show all work.
- $\csc x \sin x$ CSC X
- $\frac{\sin^3 x}{\cos x} + \sin x \cos x$
- 2. **Analyze** the following problem and student work. Find the error(s) made by the student. **Explain** the error(s) made. Support your explanation by including the correct simplification.

$$\frac{\sin x}{\cos x} + \frac{\cos x}{1 + \sin x}$$

$$= \sin x (1 + \sin x) + \cos x \cdot \cos x$$
$$= \sin x + \sin^2 x + \cos^2 x$$
$$= \sin x$$

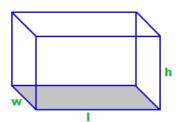
- 3. **Verify** 10 trig identities from the (1 - 31) HANDOUT given that accompanies this project.
  - You MUST choose 4 from the left column.
  - You MUST choose 6 from the right column.
  - Show all steps linearly.
  - Don't skip any steps.

- 4. **Verify** 10 trig identities from the (1-31) HANDOUT given that accompanies this project.
  - You MUST choose 3 from the left column.
  - You must choose 7 from the right column.
  - Show all steps linearly.
  - Don't skip any steps.

- 5. Compose three different, original, trigonometric expressions that meet the following criteria:
  - Starts with at least two different trig functions (i.e.  $\sin \theta$ ,  $\cos \theta$ , etc.)
  - Simplifies to a single trig function
  - Simplifies in 3 or four steps.

THEN, simplify these expressions, showing all interim steps.

6. **Write** an expression for the volume of the rectangular prism below. Simplify your expression to a single trig expression or single number.



$$l = \csc \theta \qquad w = \cot \theta$$
$$h = \sec^2 \theta - 1$$

- 7. On notebook sheet of paper, illustrate how to verify the following expression to its answer. Show all work, and describe, in words, what you did to simplify each step in a paragraph.
- \*  $(1 tanx)(1 cotx) = 2 \sec x \csc x$
- $*\frac{\sin 2x}{1+\cos 2x} = \tan x$ \*  $\sin(x+y)\sin(x-y) = \sin^2 x - \sin^2 y$
- 8. **Solve** the following trig equations. Show all steps. All answers are contained  $(0, 2\pi)$ 
  - $2\sin^2 x 5\sin x + 2 = 0$
  - sinx = cos2x
  - $cos2xcsc^2x = 2 cos 2x$
- 9. **Review.** Solve the problem below. Sketch a picture and label. Show all steps and formulas used to obtain all of your answers:
- \*Two tugboats that are 120 ft apart, pull a barge. If the length of one cable is 212 ft. and the length of the other is 230 ft...
- a) find the angle formed by the two cables.
- b) find the remaining angles.
- c) how much area (body of water) is contained between everything?