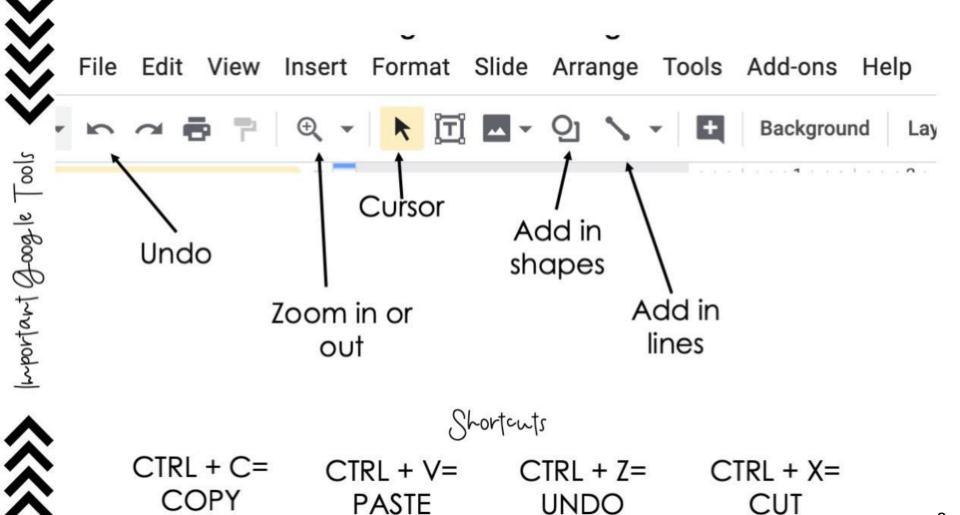
## Unit 3: Measuring Circles

Type name here

Math - Ms. Yonash



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Quiz

**Exploring Circumference** 

**Applying Circumference** 

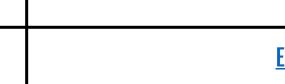
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**Resources for Review** 

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Resources



# Lesson 1: How well can you measure?

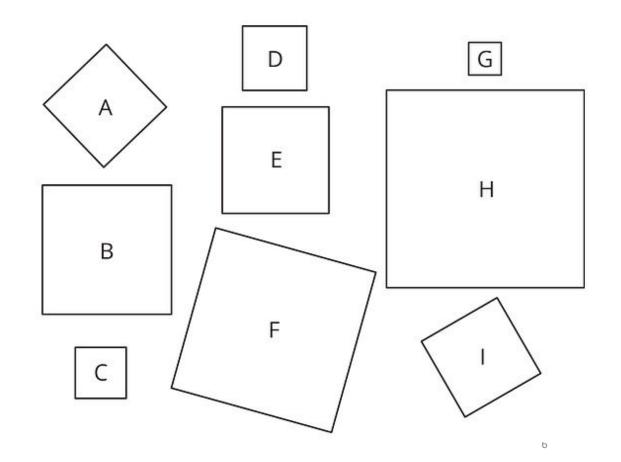
#### **Learning Goals**

I understand that it can be difficult to measure the quantities in a proportional relationship accurately.

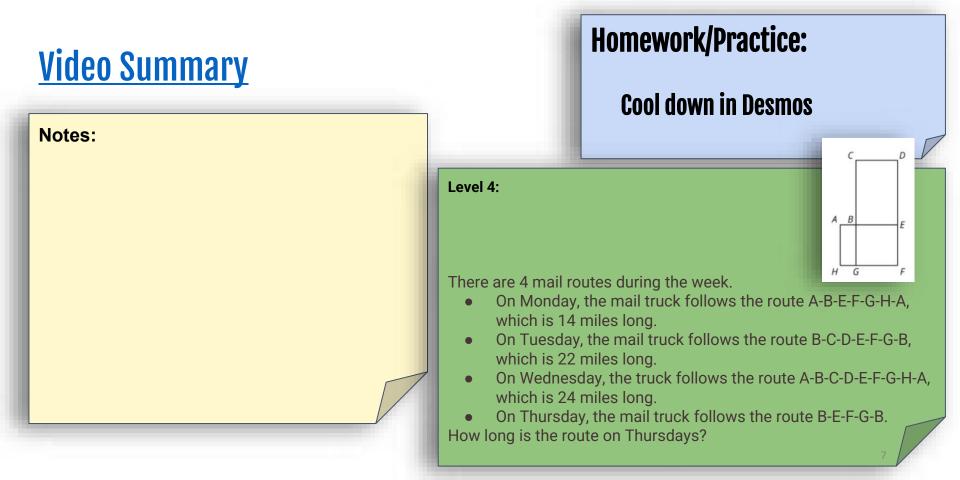
I can examine quotients and use a graph to decide whether two associated quantities are in a proportional relationship.

#### **Lesson 1: Desmos - Activity 1**

## Desmos lesson and cool down!



#### Lesson 1: How well can you measure? - SUMMARY



## **Lesson 2: Exploring Circles**

#### **Learning Goals**

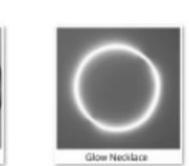
I can identify the diameter, center, radius, and circumference of a circle.

I can describe the characteristics that make a shape a circle.

#### **Lesson 2: Sorting Round Objects-- Activity 2**

#### **Sorting Round Objects Card Sort**





fan cover

Fan Cover



boiled egg

glow necklace



Center Pivot Irrigation

grill

#### **Lesson 2: Measuring Circles – Activity 3**

Priya, Han, and Mai each measured one of the circular objects from earlier.

- Priya says that the bike wheel is 24 inches.
- Han says that the yo-yo trick is 24 inches.
- Mai says that the glow necklace is 24 inches.

- 1. Do you think that all these circles are the same size? Answer here
- 1. What part of the circle did each person measure? Explain your reasoning here

#### Lesson 2: Drawing Circles - Activity 4 Optional

# Practice drawing circles in the <u>applet</u>

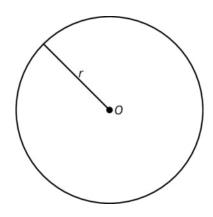
#### Draw:

- Circle A with a diameter of 6
- Circle B with a radius of 5cm



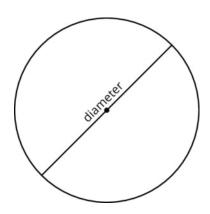
### **Radius**

The distance from the center of a circle to any point on the circle. Also the corresponding line segment from the center to a point on the circle.



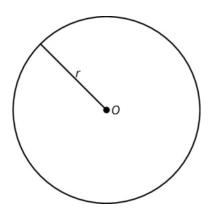
### **Diameter**

A line segment that has endpoints on a circle and passes through the center is called a diameter of the circle. The length of this segment is also called the diameter.



### Circumference

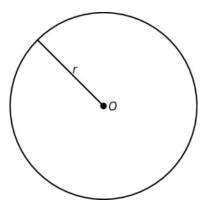
The circumference of a circle is the distance around the circle. If you imagine the circle as a piece of string, it is the length of the string. If the circle has radius r then the circumference is  $2\pi r$ .



### Circle

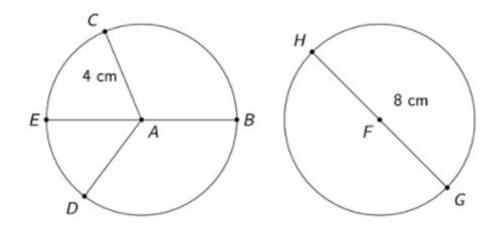
A circle of radius r with center O is the set of all points that are a distance r units from O.

To draw a circle of radius 3 and center O, use a compass to draw all the points at a distance 3 from O.



#### **Lesson 2: Comparing Circles- Cool Down**

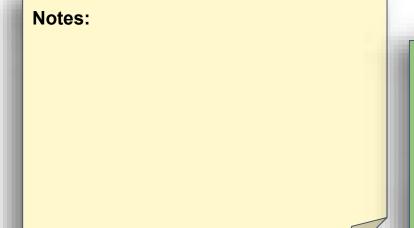
Here are two circles. Their centers are A and F.



- 1. What is the same about the two circles? Answer here
- 1. What is different about the two circles? Answer here
- 1. What is the length of segment AD? How do you know? Answer here
- 1. On the first circle, what segment is a diameter? How long is it? Answer here

#### **Lesson 2: Exploring Circles – SUMMARY**

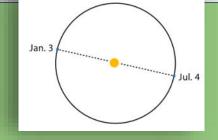
### **Video Summary**



#### **Homework/Practice:**

Cool down on the previous slide

Level 4:



On January 3rd, the Earth is 147,500,000 kilometers away from the Sun. On July 4th, the Earth is 152,500,000 kilometers away from the Sun. The sun has a radius of about 865,000 kilometers.

Could the Earth's orbit be a circle with some point in the Sun as its center? Explain your reasoning.

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# Lesson 3: Exploring Circumference

**Learning Goals** 

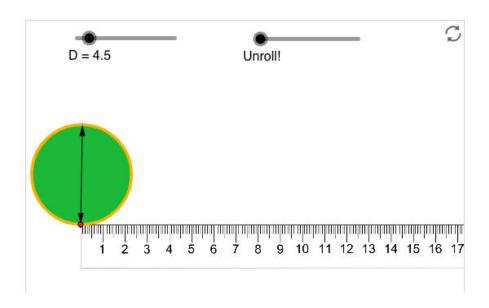
I can describe the relationship between circumference and diameter of any circle.

I can explain what  $\pi$  means.



#### **Lesson 3:** Measuring Circumference and Diameter and Calculating Circumference and Diameter -- Activity 2 and 3

## Measuring Circumference and Diameter Desmos



#### Lesson 3: Identifying Circumference and Diameter-- Cool Down Assignment

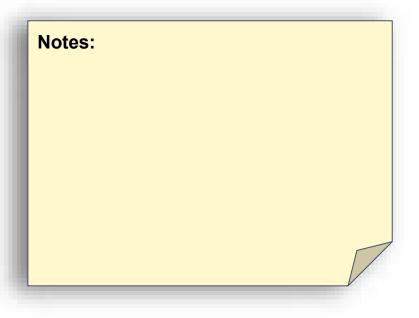
# Video showing the constant of proportionality between the diameter and circumference

Highlight all the pairs that could be reasonable approximations for the diameter and circumference of a circle. Explain your reasoning.

- A. 5 meters and 22 meters.
- B. 19 inches and 60 inches.
- C. 33 centimeters and 80 centimeters.

#### **Lesson 3: Exploring Circumference- SUMMARY**

#### **Video Summary**



#### Homework/Practice:

- -Cool down on previous slide
- -Finish Desmos

#### Level 4:

Suppose you had another circular object with a diameter that is half as long as the diameter of your largest circle. What would its circumference be?



# Lesson 4: Applying Circumference

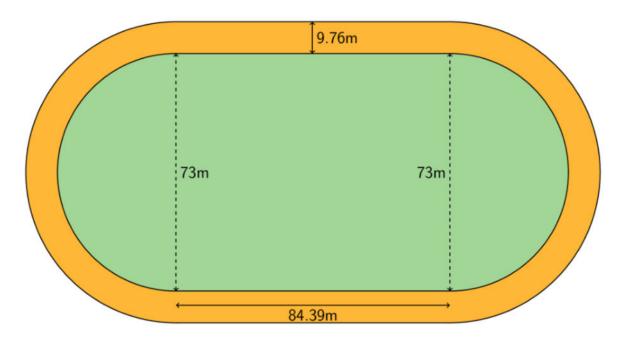
#### **Learning Goals**

I can choose an approximation for  $\pi$  based on the situation or problem.

If I know the radius, diameter, or circumference of a circle, I can find the other two.

#### Lesson 4: What Do We Know?, Using Pi, and Running Around The Track-- Activity 1-3

#### **Lesson 4 Desmos**



#### **Lesson 4: -- Cool Down Assignment**

$$C = 3.14d$$

Circle A has a diameter of 9 cm. Circle B has a radius of 5 cm.

- 1. Which circle has the larger circumference? Answer here
- 1. About how many centimeters larger is it? Answer here

#### **Lesson 4: Applying Circumference – SUMMARY**

### **Video Summary**

**Homework/Practice:** 

Cool down on previous slide

#### Notes:

#### Level 4:

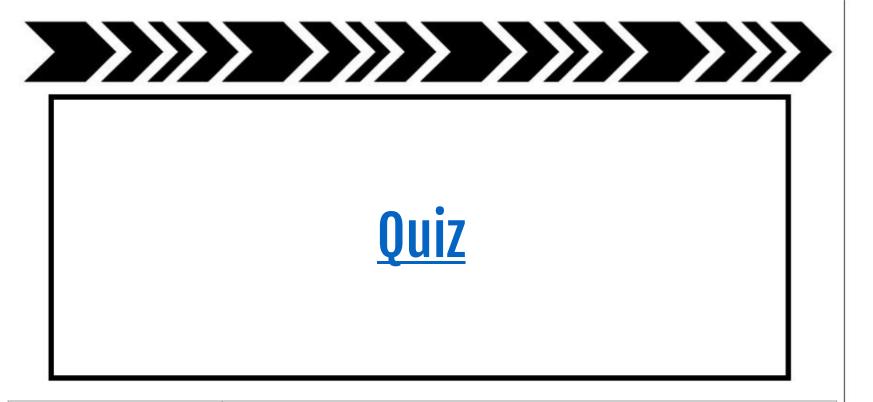
This size running track is usually called a 400-meter track. However, if a person ran as close to the "inside" as possible on the track, they would run less than 400 meters in one lap. How far away from the inside border would someone have to run to make one lap equal exactly 400 meters?



## **Note Sheet**

**Learning Goals** 

I can take notes on circles and circumference



**Learning Goals** 

I can solve my knowledge of circle concepts from lessons 1-4



# Lesson 5: Circumference and Wheels Optional

**Learning Goals** 

If I know the radius or diameter of a wheel, I can find the distance the wheel travels in some number of revolutions.

#### **Lesson 5: Optional Rotations and Distance-- Activity 3**

- A car wheel has a diameter of 20.8 inches.
  - a. About how far does the car wheel travel in:
    - 1 rotation? Answer here
    - 5 rotations? Answer here
    - 30 rotations? Answer here
  - a. Write an equation relating the distance the car travels in inches, *c*, to the number of wheel rotations, *x*. Answer here
  - a. About how many rotations does the car wheel make when the car travels 1 mile?
    Explain or show your reasoning here

#### Lesson 5: Optional Rotations and Distance-- Activity 3 Continued

- A bike wheel has a radius of 13 inches.
  - a. About how far does the bike wheel travel in
    - 1 rotation? Answer here
    - 5 rotations? Answer here
    - 30 rotations? Answer here
  - a. Write an equation relating the distance the bike travels in inches, *b*, to the number of wheel rotations, *x*. Answer here
  - a. About how many rotations does the bike wheel make when the bike travels 1 mile? Explain or show your reasoning here.

#### **Lesson 5: Optional-- Cool Down Assignment**

The wheels on Noah's bike have a circumference of about 5 feet.

- 1. How far does the bike travel as the wheel makes 15 complete rotations? Answer here
- 2. How many times do the wheels rotate if Noah rides 40 feet? Answer here

#### Lesson 5: Circumference and Wheels Optional – SUMMARY

#### **Video Summary**



#### **Homework/Practice:**

Cool down on previous page Optional Khan Quiz

#### Level 4:



If you could stretch out the spring completely straight, how long would it be? Explain or show your reasoning.

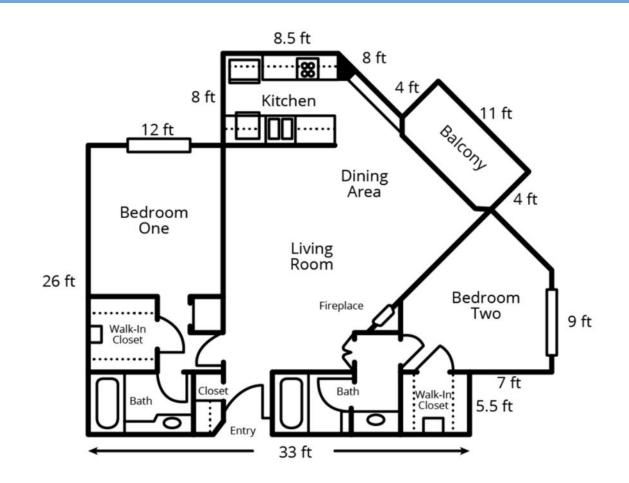
## Lesson 6: Estimating Area

**Learning Goals** 

I can calculate the area of a complicated shape by breaking it into shapes whose area I know how to calculate.

#### **Lesson 6: House Floor Plan-- Activity 2**

Kami activity (find the link posted in Google Classroom today)



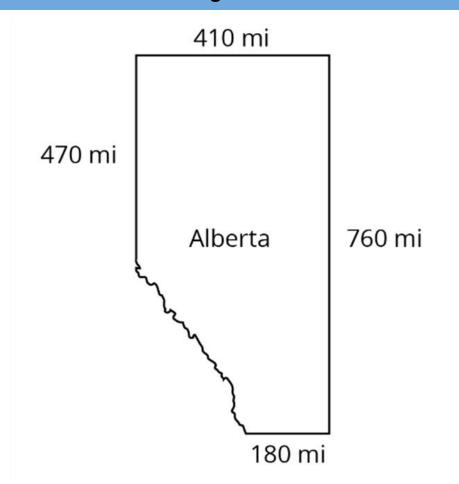
#### Lesson 6: Area of Nevada -- Activity 3

Estimate the area of Nevada in square miles. Explain or show your reasoning here



#### Lesson 6: The Area of Alberta -- Cool Down Assignment

Estimate the area of Alberta in square miles. Explain or show your reasoning here

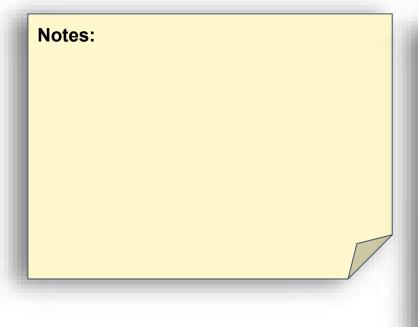


#### **Lesson 6: Estimating Area-SUMMARY**

### **Video Summary**

Homework/Practice:

Cool down on previous slide



Level 4:

The two triangles are equilateral, and the three pink regions are identical. The blue equilateral triangle has the same area as the three pink regions taken together. What is the ratio of the sides of the two equilateral triangles?



# Lesson 7: Exploring the Area of a Circle

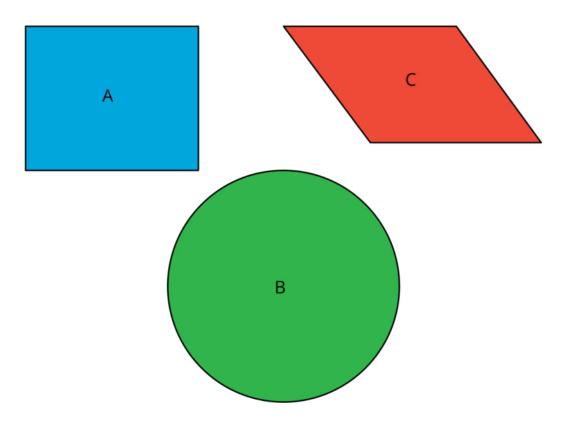
**Learning Goals** 

If I know a circle's radius or diameter, I can find an approximation for its area.

I know whether or not the relationship between the diameter and area of a circle is proportional and can explain how I know.

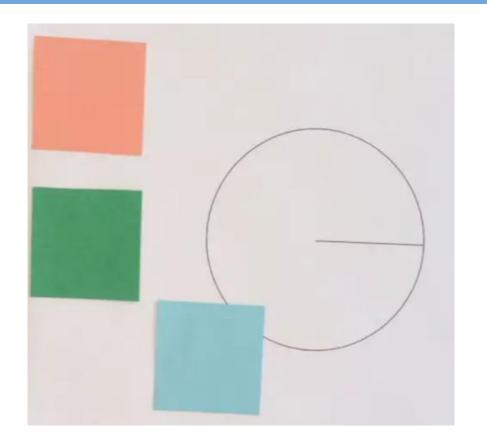
#### **Lesson 7: Estimating Areas of Circles - Activity 2**

**Estimating area of circles Desmos** 



#### **Lesson 7: Covering a Circle- Activity 3**

Click on the image to view a video on covering a circle to find the area.



#### **AREA OF A CIRCLE**

$$A = \pi r^2$$

#### Lesson 7: Area of Two Circles -- Cool Down Assignment

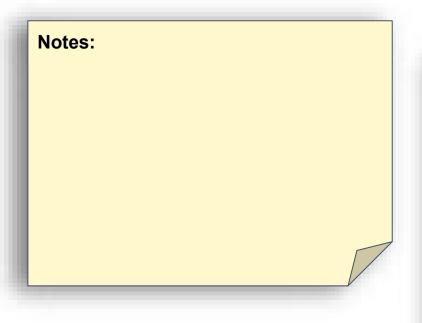
- Circle A has a diameter of approximately 20 inches and an area of approximately 300 in<sup>2</sup>.
- Circle B has a diameter of approximately 60 inches.

Highlight which of these could be the area of Circle B? Explain your reasoning here

- A. About 100 in<sup>2</sup>
- B. About 300 in<sup>2</sup>
- C. About 900 in<sup>2</sup>
- D. About 2,700 in<sup>2</sup>

#### **Lesson 7: Exploring Area of a Circle-SUMMARY**

#### <u>Video Summary</u>



#### **Homework/Practice:**

**Cool Down on previous slide** 

#### Level 4:

- 1. How many circles of radius 1 unit can you fit inside a circle of radius 2 units so that they do not overlap?
- 2. How many circles of radius 1 unit can you fit inside a circle of radius 3 units so that they do not overlap?
- 3. How many circles of radius 1 unit can you fit inside a circle of radius 4 units so that they do not overlap?

If you get stuck, consider using coins or other circular objects.



# Lesson 8: Relating Area to Circumference

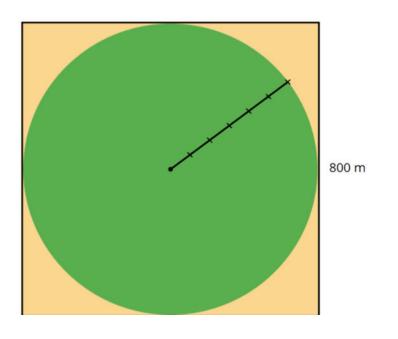
**Learning Goals** 

I can explain how the area of a circle and its circumference are related to each other.

I know the formula for area of a circle.

#### Lesson 8 Activity 1: Irrigating a Field

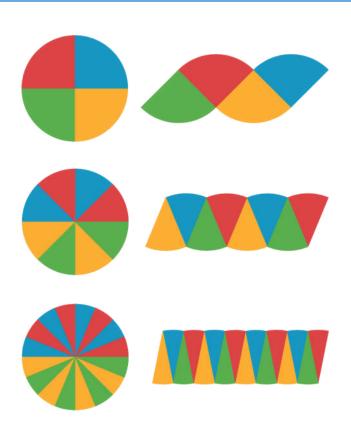
A circular field is set into a square with an 800m side length. Estimate the field's area (highlight).



- A. About 5,000 m<sup>2</sup>
- B. About 50,000 m<sup>2</sup>
- C. About 500,000 m<sup>2</sup>
- D. About 5,000,000 m<sup>2</sup>
- E. About 50,000,000 m<sup>2</sup>

#### **Lesson 8: - Activity 2**

Click on the picture to go to the applet that shows you one way to find the area formula of a circle.



#### **Lesson 8: - Activity 3**

Click on the picture to go to the video that shows you another way to find the area formula of a circle, but this time using a triangle.

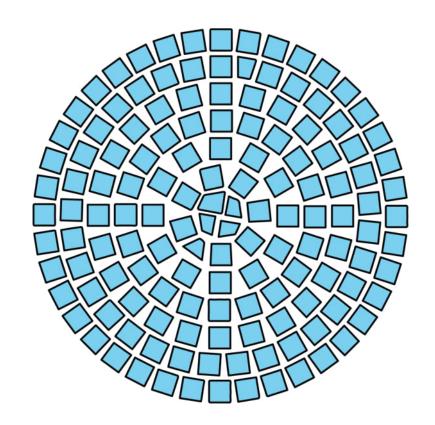
- Area =  $\frac{1}{2}$  · base · height
- Area =  $\frac{1}{2}$  · circumference · radius
- Area =  $\frac{1}{2} \cdot (\pi d) \cdot r$
- Area =  $\pi r \cdot r$
- Area =  $\pi r^2$



#### Lesson 8: Tiling a Table -- Activity 4

Elena wants to tile the top of a circular table. The diameter of the table top is 28 inches.

What is its area? Answer here



#### **Lesson 8: - SUMMARY**

### **Video Summary**

Homework/Practice:

Cool Down on the previous slide

#### Notes:

#### Level 4:

A box contains 20 square tiles that are 2 inches on each side. How many boxes of tiles will Elena need to tile the table?

## Lesson 9: Applying Area of Circles

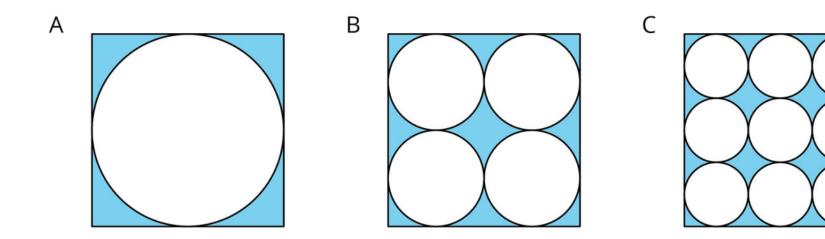
#### **Learning Goals**

I can write exact answers in terms of  $\pi$ .

I can calculate the area of more complicated shapes that include fractions of circles.

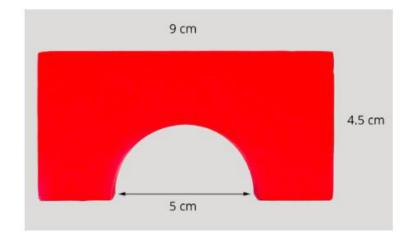
#### Lesson 9: Applying Area – Activity 1–3

#### **Lesson 9 Desmos**



#### Lesson 9: Applying Area - Activity 1-3

Here is a picture that shows one side of a child's wooden block with a semicircle cut out at the bottom.



Find the area of the side. Explain or show your reasoning here.

#### **Lesson 9: Applying Area of Circles-SUMMARY**



Notes:

Homework/Practice:

Cool Down on previous slide



Which figure in Activity 2 has a longer perimeter, Figure D or Figure E? How much longer?

## **Unit 3: Circles Resources**

- Area of Parallelograms
- Area of Triangles
- How well can you measure?: Lesson 1 <u>Video</u> Summary
- Exploring Circumference Lesson 3 Video Summary
- Applying Circumference: Lesson 4 <u>Video</u> Summary
- Estimating Area: Lesson 6 Video Summary

# **Khan Academy Practice Test**

**Kahoot Review Game** 

Study Guide Paper Packet