

# 8th Grade Math

## Guided Notes

### Solutions to Equations in One Variable

#### One Solution, Infinite Many Solutions, No Solution

Two Guided Color-coded  
Interactive Math Notebook Pages

**Solutions to Linear Equations in One Variable**

The solution of an equation is the value(s) of the variable(s) that make the equation a true statement.

Equations in one variable can have one solution, infinite solutions or no solution.

	One Solution	Infinite Solutions	No Solution
<b>Reasoning:</b> What the type of solution means.	Only <u>one</u> value will make the equation <u>true</u> . • <u>One Number</u>	<u>Any</u> value will make the equation <u>true</u> . • <u>Any Number</u>	<u>No</u> values will make the equation <u>true</u> . • <u>No Number</u>
<b>True Solution?</b> Always, Sometimes, Never	<u>Sometimes</u> A conditional equation is true for <u>some</u> values of $x$ . <u>Only true one time</u>	<u>Always</u> An identity is <u>always</u> true for any value of $x$ . <u>True every time</u>	<u>Never</u> A contradiction is <u>never</u> true for any value of $x$ . <u>Not ever true</u>
<b>Example:</b>	$4x + 6 = 18 - 6$ $4x = 12$ $x = 3$ • <u>3</u> is the only number that makes the equation <u>true</u> .	$5x + 15 = 5x + 15$ $15 = 15$ <u>True</u> • <u>Any Number</u> for $x$ will make the equation <u>true</u> .	$4x + 8 = 4x + 3$ $8 \neq 3$ <u>False</u> • <u>No Number</u> for $x$ will make the equation <u>true</u> .
<b>Hints:</b> Look at both sides of the equation.	End result still has a <u>variable</u> and a <u>solution</u> .	Variables cancel each other out and both sides of the equation <u>look equal</u> .	Variables cancel each other out and both sides of the equation <u>do not look equal</u> .


**Determining the Type of Solution**

Simplified Equation	One Solution	Infinite Many Solutions	No Solution
$5x - 8 = 3x + 3$	Variable terms are <u>different</u>	Variable terms are the <u>same</u>	Variable terms are the <u>same</u>
$2 + 6x = 6x + 2$	Both sides are <u>not equal</u>	Both sides are <u>equal</u>	Both sides are <u>not equal</u>

**Example One:**  
 $2(4x + 3) = 5(2x + 2)$   
 $8x + 6 = 10x + 10$   
 $-10x$   
 $-2x = 4$   
 $x = -2$   
 The equation has one solution.  
 The solution means that -2 will make the equation true.

**Example Two:**  
 $4(-1) = 4x + 3(2x - 1)$   
 $-4 = 4x + 6x - 3$   
 $-4 = 10x - 3$   
 $-1 = 10x$   
 $x = -\frac{1}{10}$   
 The equation has one solution.  
 The solution means that -1/10 will make the equation true.

**Example Three:**  
 $2x + 1 = 3x$   
 $-x + 1 = 0$   
 $-x = -1$   
 $x = 1$   
 The equation has one solution.  
 The solution means that 1 will make the equation true.



★ Roxygirl Teacher ★

# Solutions to Linear Equations in One Variable

The \_\_\_\_\_ of an equation is the value(s) of the variable(s) that make the equation a **true statement**.

- Equations in **one variable** can have \_\_\_\_\_ solution, \_\_\_\_\_ solutions or \_\_\_\_\_ solution.

	One Solution	Infinite Solutions	No Solution
<b>Reasoning:</b> <i>What the type of solution means.</i>	Only _____ value will make the equation <b>true</b> .  ★ _____	_____ value will make the equation <b>true</b> .  ★ _____	_____ values will make the equation <b>true</b> .  ★ _____
<b>True Solution?</b> <i>Always, Sometimes, Never</i>	_____ A conditional equation is true for <b>some</b> values of $x$ . _____ _____	_____ An identity is <b>always</b> true, for any value of $x$ . _____ _____	_____ A contradiction is <b>never</b> true for any value of $x$ . _____ _____
<b>Example:</b>  .	$4x + 6 = 18$  _____  _____  ★ _____ is the only number that makes the equation <b>true</b> .	$5x + 15 = 5x + 15$  _____  _____  ★ _____ for $x$ will make the equation <b>true</b> .	$4x + 8 = 4x + 3$  _____  _____  ★ _____ for $x$ will make the equation true.
<b>Hints:</b> <i>Look at both sides of the equation.</i>	End result still has a _____ and a _____.	Variables cancel each other out and <b>both sides</b> of the equation _____.	Variables cancel each other out and <b>both sides</b> of the equation _____.

# Determining the Type of Solution

	One Solution	Infinite Many Solutions	No Solution
Simplified Equation	$3x - 5 = 7x + 3$	$2 + 4x = 4x + 2$	$8x + 9 = 8x - 5$
Look at the Variable Terms.	The variable terms are _____.	Variable terms are the _____. Both sides _____.	Variable terms are the _____. Both sides _____.

## Example One:

$$2(4x + 5) = 5(2x + 4)$$

\_\_\_\_\_

\_\_\_\_\_ both sides of the equation.

← **Variable terms** are \_\_\_\_\_.

★ Equation can be \_\_\_\_\_. ★

The equation has \_\_\_\_\_. The solution means \_\_\_\_\_.

\_\_\_\_\_.

## Example Two:

$$2(5x + 4) - 11 = 4x + 3(2x - 1)$$

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_ both sides of the equation.

← **Variable terms** are \_\_\_\_\_.

and both sides are \_\_\_\_\_.

The equation has \_\_\_\_\_. The solution means \_\_\_\_\_.

\_\_\_\_\_.

## Example Three:

$$-4x + 3(5x + 6) = 7(2x + 1) - 3x$$

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_ both sides of the equation.

← **Variable terms** are \_\_\_\_\_.

and both sides are \_\_\_\_\_.

The equation has \_\_\_\_\_. The solution means \_\_\_\_\_.

\_\_\_\_\_.

# Solutions to Linear Equations in One Variable

The Solution of an equation is the value(s) of the variable(s) that make the equation a true statement.

- Equations in one variable can have one solution, infinite solutions or no solution.

	One Solution	Infinite Solutions	No Solution
<b>Reasoning:</b> <i>What the type of solution means.</i>	Only <u>one</u> value will make the equation <u>true</u> . ★ <u>One Number</u>	<u>Any</u> value will make the equation <u>true</u> . ★ <u>Any Number</u>	<u>No</u> values will make the equation <u>true</u> . ★ <u>No Number</u>
<b>True Solution?</b> <i>Always, Sometimes, Never</i>	<u>Sometimes</u> A conditional equation is true for <u>some</u> values of $x$ . <u>Only true one time.</u>	<u>Always</u> An identity is <u>always</u> true, for any value of $x$ . <u>True every time</u>	<u>Never</u> A contradiction is <u>never</u> true for any value of $x$ . <u>Not ever true.</u>
<b>Example:</b>	$4x + 6 = 18 - 6$ $\frac{4x}{4} = \frac{12}{4}$ $x = 3$ ★ <u>3</u> is the only number that makes the equation <u>true</u> .	$5x + 15 = 5x + 15$ $15 = 15$ <u>true</u> ★ <u>Any Number</u> for $x$ will make the equation <u>true</u> .	$4x + 8 = 4x + 3$ $8 \neq 3$ <u>False</u> ★ <u>No Number</u> for $x$ will make the equation true.
<b>Hints:</b> <i>Look at both sides of the equation.</i>	End result still has a <u>variable</u> and a <u>solution</u> .	Variables cancel each other out and <u>both sides</u> of the equation <u>look equal</u> .	Variables cancel each other out and <u>both sides</u> of the equation <u>do not look equal</u> .



# Determining the Type of Solution

	One Solution	Infinite Many Solutions	No Solution
Simplified Equation	$3x - 5 = 7x + 3$	$2 + 4x = 4x + 2$	$8x + 9 = 8x - 5$
Look at the Variable Terms.	The Variable terms are <u>different</u> .	Variable terms are the <u>same</u> . Both sides <u>are equal</u> .	Variable terms are the <u>same</u> . Both sides <u>are not equal</u> .

## Example One:

$$2(4x + 5) = 5(2x + 4)$$

$$8x + 10 = 10x + 20$$

$$\begin{array}{r} -10x \\ -10x \end{array}$$

$$\begin{array}{r} -2x = 10 \\ -2 \quad -2 \end{array} \quad \boxed{x = -5}$$

Simplify both sides of the equation.

← Variable terms are different.

★ Equation can be solved. ★

The equation has one solution. The solution means that -5 is the only value for x that will make the equation true.

## Example Two:

$$2(5x + 4) - 11 = 4x + 3(2x - 1)$$

$$10x + 8 - 11 = 4x + 6x - 3$$

$$10x - 3 = 10x - 3$$

True

Simplify both sides of the equation.

← Variable terms are the same.

and both sides are equal.

The equation has infinite many solutions. The solution means that any value for x will make the equation true.

## Example Three:

$$-4x + 3(5x + 6) = 7(2x + 1) - 3x$$

$$-4x + 15x + 18 = 14x + 7 - 3x$$

$$11x + 18 \neq 11x + 7$$

False

Simplify both sides of the equation.

← Variable terms are the same.

and both sides are not equal.

The equation has no solution. The solution means that no value for x will make the equation true.



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