## **EXAMPLE 1** Grade 7 Unit 6: Expressions, Equations, and Inequalities Lessons 1–6: Representing Situations of the Form of px + q = r and p(x + q) = r

	<ul> <li>I can think of ways to solve some more constrained in the solution of the solution of</li></ul>	omplicated word problems. ents parts of a situation and relationships own amount in a situation. s that represent the same situation. iagram that shows the same relationship.
-	<ul> <li>Activity Suggestions:</li> <li>▶ Lesson 1: Focus on making diagrams or tables or reason in some other way. The main goal of this lesson is for students to realize different strategies for efficiently solving problems are needed. Activity 4 is an optional card sort.</li> <li>▶ Combine Lesson 2 and Lesson 3: Students should represent and reason about contexts using tape diagrams. They should use tape diagrams to find unknown amounts in given situations. There are digital versions of Lesson 2, Activity 3 and Lesson 3, Activity 3. Grouping may need to be adjusted for situations.</li> </ul>	<ul> <li>Assessment Suggestions:</li> <li>➤ Check Your Readiness assessment: Administer all items within the first or second day of this section. Use the guidance provided with each problem to adjust instruction so that students can access the math in the unit.</li> <li>&gt; Lesson 1 cool-down</li> <li>&gt; Lesson 2 cool-down</li> <li>&gt; Lesson 3 cool-down</li> </ul>

- I can draw a tape diagram to represent a situation where there is a known amount and several copies of an unknown amount and explain what the parts of the diagram represent.
  - I can find a solution to an equation by reasoning about a tape diagram or about what value would make the equation true.
  - I can draw a tape diagram to represent a situation where there is more than one copy of the same sum and explain what the parts of the diagram represent.

### Activity Suggestions:

Explore. Play, and Discuss

Deep Dive

Combine Lesson 4 and Lesson 5: Focus on drawing and finding solutions to an equation by reasoning about tape diagrams. In Lesson 4, students primarily use the form of the equation px + q = r while in Lesson 5, students

#### Assessment Suggestions:

- Lesson 4 cool-down
- Lesson 5 cool-down

to solve for unknown amounts. Lesson 4, Activity 2 and Lesson 5, Activity 2 have a digital version.	use the form of the equation $p(x+q) = r$
Lesson 4, Activity 2 and Lesson 5, Activity 2 have a digital version.	to solve for unknown amounts.
2 have a digital version.	Lesson 4, Activity 2 and Lesson 5, Activity
	2 have a digital version.

- I understand the similarities and differences between the two main types of equations we are studying in this unit.
- When I have a situation or a tape diagram, I can represent it with an equation

	<ul> <li>Activity Suggestions:</li> <li>▶ Lesson 6: The purpose of this lesson is to distinguish equations of the form px + q = r and p(x + q) = r.</li> <li>Corresponding tape diagrams are used as tools in this work, along with situations that these equations can represent. Lesson 6, Activity 2 is a card sort that may need to be adjusted for groupings.</li> <li>▶ Teach and encourage students to study the lesson summaries (at the end of every lesson) and refer back to them.</li> </ul>	<ul> <li>Assessment Suggestions:</li> <li>&gt; Lesson 6 cool-down</li> <li>&gt; revisions to previous assessment prompts</li> <li>&gt; Students use learning targets to decide what additional practice they need.</li> </ul>
--	--	---

- Assign one or more of the distributed practice problem sets from Lessons 1–6 to be completed over the time period that the section is being worked on.
  - These could also be lagging, so that students are working on practice problems from the previous section or unit during this section or unit.
  - Specify which problems students should submit, or let them choose.
  - Note: Several existing platforms already have IM's practice problems loaded so that students can complete and submit them online. Some can be autoscored.

- Delve into any of the skipped optional activities of <u>Lesson 2</u>, <u>Lesson 3</u>, <u>Lesson 4</u>, and <u>Lesson 5</u>.
- Use any of the lessons from <u>Grade 6, Unit 6</u> that focus on solving equations.

## Lessons 7–12: Solving Equations of the Form px + q = r and p(x+q) = rand Problems That Lead to Those Equations

cuss	<ul> <li>I can explain how a balanced hanger and</li> <li>I can find an unknown weight on a hange represents the diagram.</li> <li>I can write an equation that describes the</li> </ul>	an equation represent the same situation. r diagram and solve an equation that e weights on a balanced hanger.
Explore, Play, and Dis	Activity Suggestions: Combine Lesson 7 and Lesson 8: In Lesson 7, focus on approaching equations of the form px + q = r by subtracting $q$ from each side and dividing each side by $p$ (or multiplying by $\frac{1}{p}$ ). In Lesson 8, focus on the two different ways to solve an equation of the form $p(x+q) = r$ efficiently. Grouping options may need to be adapted in Lesson 7, Activity 2.	Assessment Suggestions: → Lesson 7 cool-down → Lesson 8 cool-down

Dive Deep	<ul> <li>I can use the idea of doing the same to enumbers or solutions.</li> <li>For an equation like 3(x+2) = 15, I can so each side by 3, or by first rewriting 3(x+2).</li> <li>For equations with more than one way to on the numbers in the equation.</li> </ul>	ach side to solve equations that have negative olve it in two different ways: by first dividing 2) using the distributive property. 5 solve, I can choose the easier way depending
	Activity Suggestions:	Assessment Suggestions: ≻ Lesson 9 cool-down

© 2020 Illustrative Mathematics, Licensed CC-BY 4.0 https://creativecommons.org/licenses/by/4.0/

➤ Combine Lesson 9 and Lesson 10: Focus on solving equations of the form $px + q = r$ or $p(x + q) = r$ with negative numbers and practice finding the most efficient way to solve equations based on the numbers in the equation. There is a digital version of Activity 3.	≻ <u>Lesson 10 cool-down</u>
---	------------------------------

d Apply	<ul> <li>I can solve story problems by drawing and reasoning about a tape diagram or by writing and solving an equation.</li> <li>I can solve story problems about percent increase or decrease by drawing and reasoning about a tape diagram or by writing and solving an equation.</li> </ul>	
Synthesize and	<ul> <li>Activity Suggestions:</li> <li>➤ Combine Lesson 11 and Lesson 12: Focus on strategies for solving word problems in Lesson 11 and percent increase or decrease in Lesson 12. Groupings may need to be adjusted.</li> </ul>	<ul> <li>Assessment Suggestions:</li> <li>&gt; Lesson 11 cool-down</li> <li>&gt; Lesson 12 cool-down</li> <li>&gt; revisions to previous assessment prompts</li> <li>&gt; Students use learning targets to decide what additional practice they need.</li> </ul>

<b>Ongoing Practice</b>	<ul> <li>Assign one or more of the distributed practice problem sets from Lessons 7–12 to be completed over the time period that the section is being worked on.</li> <li>These could also be lagging, so that students are working on practice problems from the previous section or unit during this section or unit.</li> <li>Specify which problems students should submit, or let them choose.</li> <li>Note: Several existing platforms already have IM's practice problems loaded so that students can complete and submit them online. Some can be autoscored.</li> </ul>

Anytime Resources

• Delve into any of the skipped activities of Lessons 1–12.

© 2020 Illustrative Mathematics, Licensed CC-BY 4.0 https://creativecommons.org/licenses/by/4.0/

### Lessons 13–17: Inequalities

- I can explain what the symbols  $\leq$  and  $\geq$  mean.
- I can represent an inequality on a number line.
- I understand what it means for a number to make an inequality true.
- I can describe the solutions to an inequality by solving a related equation and then reasoning about values that make the inequality true.
- I can write an inequality to represent a situation.

Discuss

схрюге, глау, апи	<ul> <li>Activity Suggestions:</li> <li>Combine Lesson 13 and Lesson 14: In Lesson 13, reintroduce &lt; and &gt; from Grade 6 and build on this knowledge to introduce ≤ and ≥. Focus on substitution to determine whether given values of x satisfy inequalities. In Lesson 14, build on this knowledge having students write inequalities representing given situations.</li> </ul>	Assessment Suggestions: ➤ Lesson 13 cool-down ➤ Lesson 14 cool-down
-------------------	---	---

đ	<ul> <li>I can graph the solutions to an inequality on a number line.</li> <li>I can solve inequalities by solving a related equation and then checking which values are solutions to the original inequality.</li> </ul>	
Dive Deep	Activity Suggestions: ► Lesson 15: Focus on solving inequalities using a number line. Emphasize reasoning asking, "Does this make sense?"	Assessment Suggestions: ➤ Lesson 15 cool-down

٠	I can match an inequality to a situation it represents, solve it, and then explain what the
	solution means in the situation.
•	If I have a situation and an inequality that represents it I can explain what the parts of

- If I have a situation and an inequality that represents it, I can explain what the parts of the inequality mean in the situation.
- I can use what I know about inequalities to solve real-world problems.

#### Activity Suggestions:

Synthesize and Apply

### Combine Lesson 16 and Lesson 17: Students apply their knowledge of solving inequalities to real word problems. Group presentations may need to be modified for individual learning. Lesson 17, Activity 3 involves problem and data cards. Activity may need to be modified for grouping.

#### Assessment Suggestions:

- Lesson 16 cool-down
- Lesson 17 cool-down
- revisions to previous assessment prompts
- Students use <u>learning targets</u> to decide what additional practice they need.

Ongoing Practice	<ul> <li>Assign one or more of the distributed practice problem sets from Lessons 13–17 to be completed over the time period that the section is being worked on.</li> <li>These could also be lagging, so that students are working on practice problems from the previous section or unit during this section or unit.</li> <li>Specify which problems students should submit, or let them choose.</li> <li>Note: Several existing platforms already have IM's practice problems loaded so that students can complete and submit them online. Some can be autoscored.</li> </ul>
------------------	--

S	•	Delve into any of the skipped activities of <u>Lesson 13</u> , <u>Lesson 14</u> , <u>Lesson 16</u> , or <u>Lesson 17</u> .
ource		
e Res		
ytime		
An		

# Lessons 18–23: Writing Equivalent Expressions

Explore, Play, and Discuss	<ul> <li>I can organize my work when I use the distributive property.</li> <li>I can rewrite subtraction as adding the opposite and then rearrange terms in an expression.</li> <li>I can use the distributive property to rewrite expressions with positive and negative numbers.</li> <li>I understand that factoring and expanding are words used to describe using the distributive property to write equivalent expressions.</li> </ul>		
	<ul> <li>Activity Suggestions:</li> <li>▶ Lesson 18: This lesson builds on using the equations px + q = r and p(x + q) = r. Focus on the pitfalls when the expression has negative numbers or subtraction.</li> <li>▶ Lesson 19: Some of the expressions in this lesson are in preparation for understanding combining like terms in terms of the distributive property, coming up in the next lesson.</li> </ul>	Assessment Suggestions: ≻ Lesson 18 cool-down ≻ Lesson 19 cool-down	

	<ul> <li>I can figure out whether two expressions are equivalent to each other.</li> <li>When possible, I can write an equivalent expression that has fewer terms.</li> <li>I am aware of some common pitfalls when writing equivalent expressions, and I can avoid them.</li> </ul>		
Dive Deep	<ul> <li>Activity Suggestions:</li> <li>➤ Combine Lesson 20 and Lesson 21: Students should focus on gaining fluency in writing expressions. Highlight the common pitfall of mishandling subtraction in an expression. Grouping in Lesson 20, Activity 3 may need to be adjusted.</li> </ul>	Assessment Suggestions:	

- When I look at an expression, I can notice if some parts have common factors and make the expression shorter by combining those parts.
- I can write algebraic expressions to understand and justify a choice between two options.

<ul> <li>Activity Suggestions:</li> <li>➤ Lesson 22: Encourage students to make use of structure to apply the distributive property in more sophisticated ways.</li> <li>➤ Lesson 23: Students should apply their strategies to help them solve real world strategies. Focus on making connections between these situations and the previously used equations.</li> </ul>	<ul> <li>Assessment Suggestions:</li> <li>&gt; Lesson 22 cool-down</li> <li>&gt; revisions to previous assessment prompts</li> <li>&gt; Students use learning targets to decid what additional practice they need.</li> </ul>
---	---

<b>Ongoing Practice</b>	<ul> <li>Assign one or more of the distributed practice problem sets from Lessons 18-23 to be completed over the time period that the section is being worked on.</li> <li>These could also be lagging, so that students are working on practice problems from the previous section or unit during this section or unit.</li> <li>Specify which problems students should submit, or let them choose.</li> <li>Note: Several existing platforms already have IM's practice problems loaded so that students can complete and submit them online. Some can be autoscored.</li> </ul>
-------------------------	--

SS	• Delve into any of the skipped activities of <u>Lesson 20</u> or <u>Lesson 21</u> .
source	
Res	
time	
Any	